

KATHOLIEKE UNIVERSITEIT
LEUVEN

SUMMER SCHOOL BINARY STARS

University of Leuven, Belgium
10-15 September 2012

MAIN TOPICS

The binary zoo
Observations and data analysis
High-energy phenomena
Theory of binary evolution
Statistics of main-sequence binaries and substellar companions

EXTERNAL LECTURERS

Alain JORISSEN - Université Libre de Bruxelles, Belgium
Tom MARSH - University of Warwick, UK
Tsevi MAZEH - Tel Aviv University, Israel
Gijs NELEMANS - Radboud University Nijmegen, The Netherlands
Lionel SIESS - Université Libre de Bruxelles, Belgium

INFO www.fys.kuleuven.be/ster/summerschool - summerschool@ster.kuleuven.be

SOC Christofel WAEKENS - Steven BLOEMEN - Nadya GORLOVA - Roy OSTENSEN

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Institute of
Astronomy



Faculty of
Sciences

The binary zoo

Alain Jorissen

Institut d'Astronomie et d'Astrophysique

UNIVERSITÉ LIBRE DE BRUXELLES,
UNIVERSITÉ D'EUROPE



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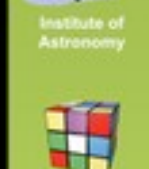
Alain JORISSEN - Université Libre de Bruxelles, Belgium
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Institute of
Astronomy



Faculty of
Sciences

The binary zoo

Inventaire

Une pierre
deux maisons
trois ruines
quatre fossoyeurs
un jardin
des fleurs

un raton laveur

une douzaine d'huîtres un citron un pain
un rayon de soleil
une lame de fond
six musiciens
une porte avec son paillasson
un monsieur décoré de la légion d'honneur



J. Prévert un autre raton laveur

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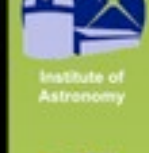
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Institute of
Astronomy



Faculty of
Sciences

The binary zoo

Inventaire

RS CVn

W UMa

Ba

DQ Her

S (no Tc)

metal-deficient post-AGB

CH

one Algol

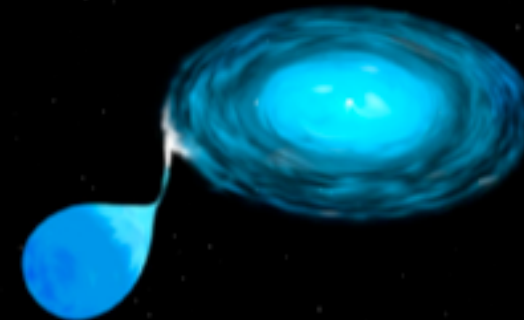
CEMPs

LMXRB

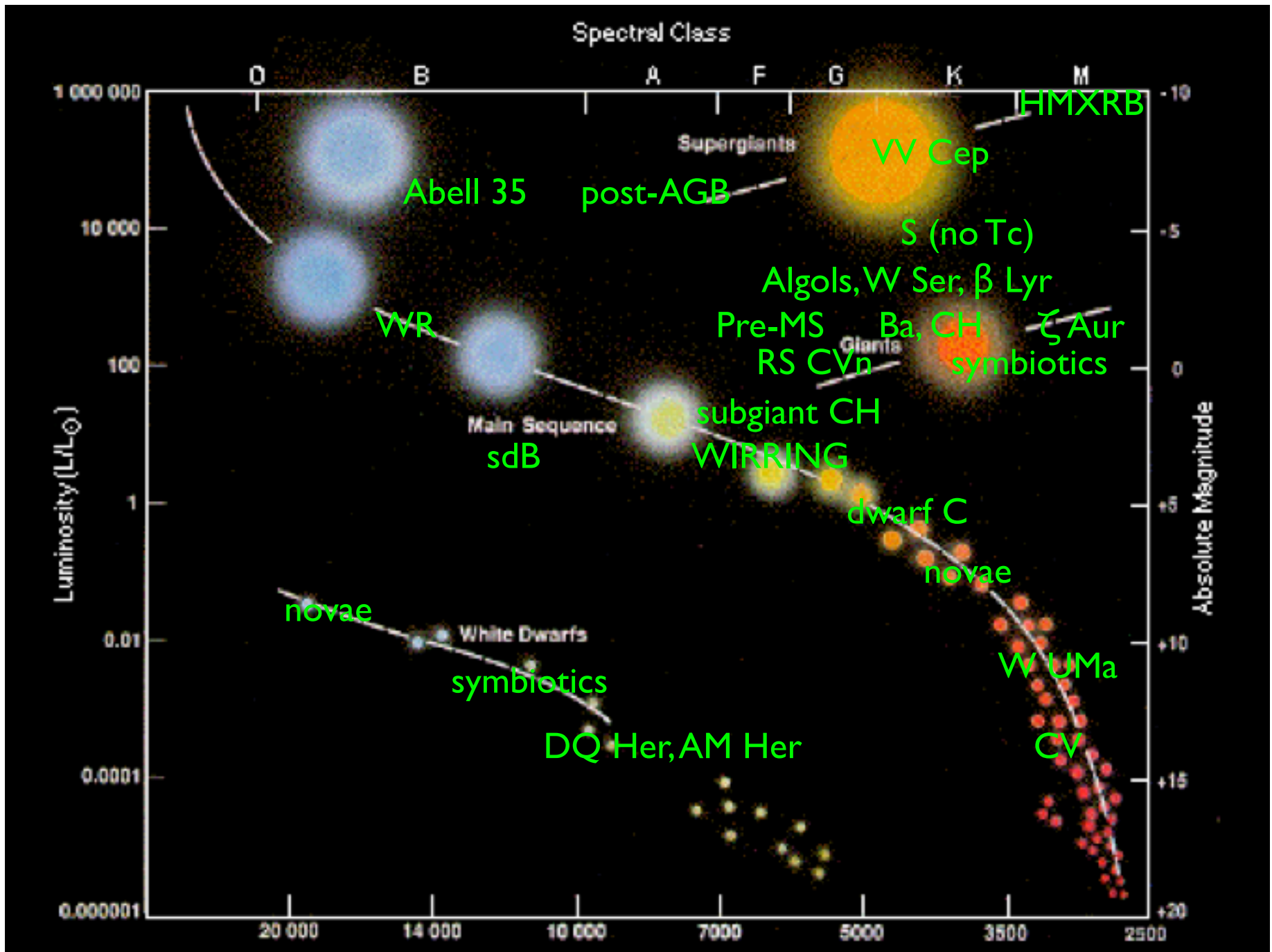
novae

SNIa

symbiotics



A. Jorissen and another Algol



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Institute of Astronomy



Faculty of Sciences

The binary zoo

Conducting line :

Classification of binary stars

- i) Mass transfer**
- ii) Evolutionary stage**
- iii) Observational properties**

The binary zoo

Classification of binary stars:

There are three possible ways to classify binary stars, based on:

- i) Mass transfer** [→ Lionel Siess, Gijs Nelemans]
- ii) Evolutionary stage** [→ Lionel Siess]
- iii) Observational properties** [→ Tom Marsh, Tsevi Mazeh]

The binary zoo

Classification of binary stars:

There are three possible ways to classify binary stars, based on:

- i) Mass transfer** [→ Lionel Siess, Gijs Nelemans]
- ii) Evolutionary stage** [→ Lionel Siess]
- iii) Observational properties** [→ Tom Marsh, Tsevi Mazeh]

Knowing the location of the binary in all 3 schemes often is the goal of binary-star research !

= The 'guiding line' for my 5 lectures ...

The binary zoo

Classification of binary stars

Contents

i) Mass transfer classes: detached, semi-detached, contact

(W UMa)

Technical intermezzi about *Roche lobes*, *mass-radius exponents*, *mass-transfer rates* (Bondi-Hoyle), *time scales* (adiabatic, thermal, nuclear), *stability of mass transfer* [→ Lionel Siess]

ii) Evolutionary-stage classes

Two examples: - **post-AGB stars**
- **Barium stars**

Technical intermezzo : *Heavy-element synthesis*

Eggleton's classification: evolutionary class and mass transfer modes A, B, C

Important diagnostics of mass transfer modes: (a) eccentricity - period diagrams

(b) mass-function distributions

→ constraints on companion masses

→ The **Algol** paradox

(**Algols**, β Lyr, SV Cen/ W Ser)

The binary zoo

Classification of binary stars

Contents

iii) Observational-property classes [→ Tsevi Mazeh, Tom Marsh]

Technical intermezzo : Orbital elements

visual/interferometric, astrometric, spectroscopic (SB1, SB2)

Technical intermezzo : Masses

difficulties with spectroscopy : - the case of binaries involving long-period variables
- MACHO : the puzzle of sequence D (all ellipsoidal?)

photometric: (a) geometry (eclipses: **Algols** - β Lyr, ζ Aur - **VV Cep**, **ellipsoidal** : **W UMa**)

(b) dust (sequence D?, ϵ Aur)

(c) spots (**RS CVn**)

confusion between **RS CVn** and **pre-main sequence** binaries (e - P again)

(d) eruptive: [→ Tom Marsh]

(d.1) **novae** : MS + WD (slow mass accretion)

(d.2) **dwarf novae and cataclysmic variables** [→ T. Marsh, G. Nelemans]

MS + WD (fast mass accretion, accretion disk, magnetic field or not)

DQ Her, AM Her

(d.3) **symbiotics**: giant + WD

(d.4) **SNIa** : WD + WD (?)

(e) X -rays : **HMXRB** (neutron stars, black holes), **LMXRB = CV** [→ G. Nelemans]

The binary zoo

Classification of binary stars

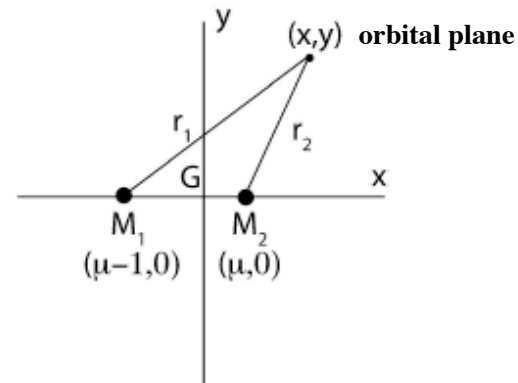
i) Mass transfer

A technical parenthesis first about **Roche lobes**

Roche lobe (I)

The Roche model (E. Roche 1820–1883) of a binary system:

- two point masses
- circular orbits
- synchronous rotation with the orbital motion (so-called 'corotation').



→ binary system at rest in a frame corotating with the orbital motion.

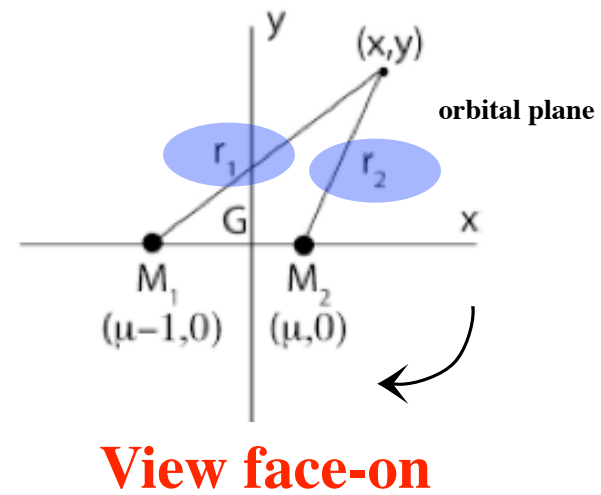
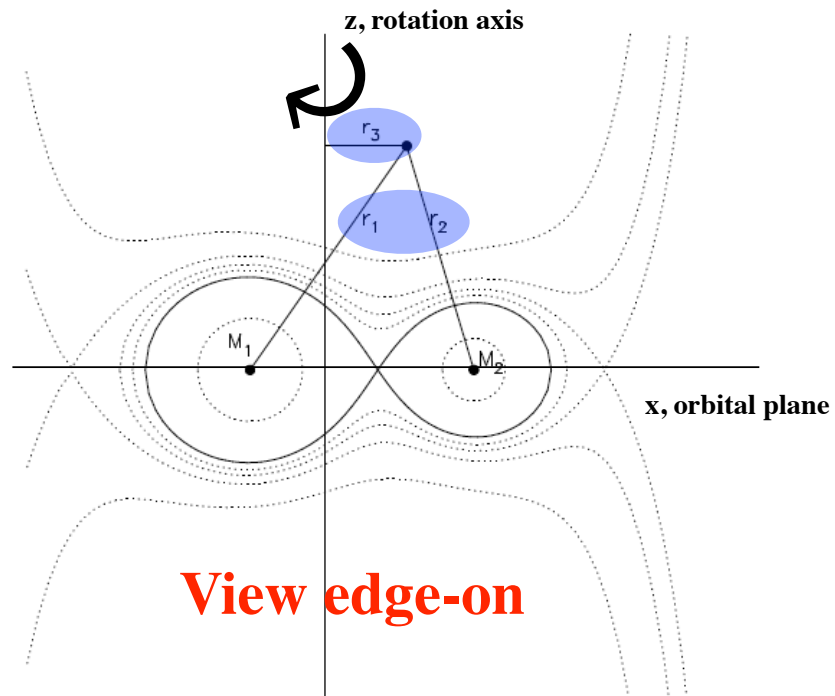
In this frame, define effective equipotential surfaces for the gravitational potential corrected for centrifugal effects :

$$\Phi = -\frac{\mu}{r_1} - \frac{1-\mu}{r_2} - \frac{r_3^2}{2} = \text{constant}$$

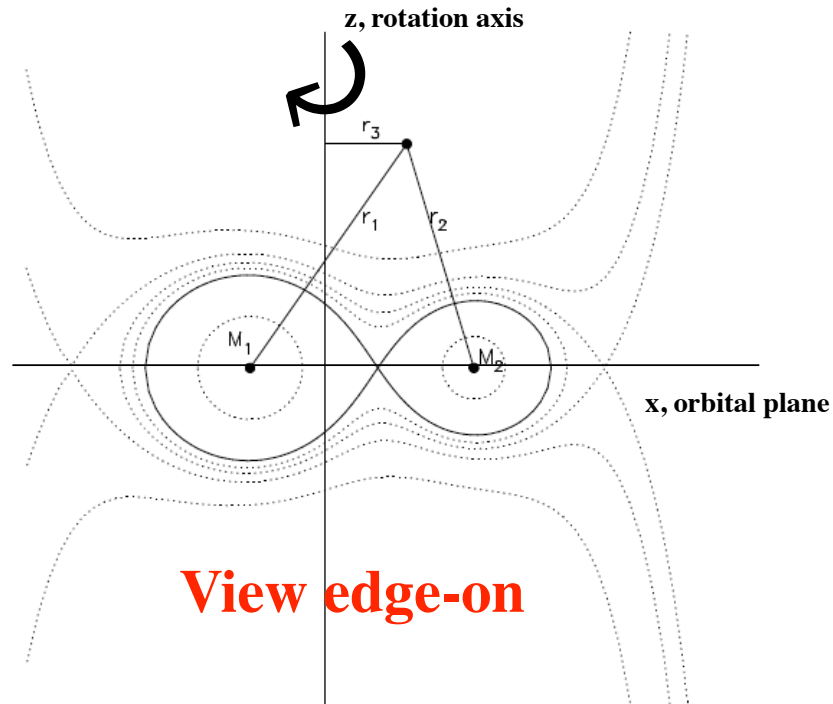
$$\text{with } \mu = \frac{M_1}{M_1 + M_2}$$

in units where the orbital period and separation are taken as unit time and distance, and total mass as unit mass.

Roche lobe (II)

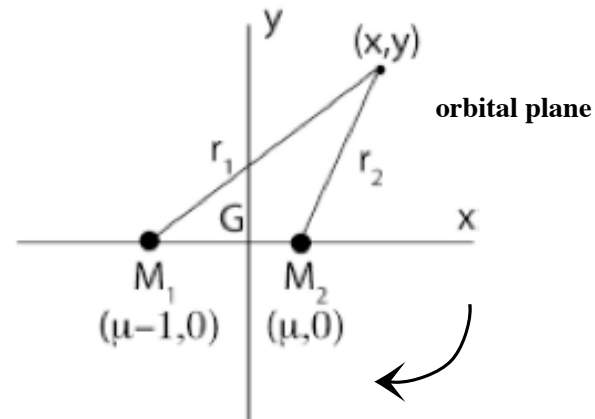


Roche lobe (III)



$$\Phi = -\frac{\mu}{r_1} - \frac{1-\mu}{r_2} - \frac{r_3^2}{2} = \text{constant}$$

with $\mu = \frac{M_1}{M_1 + M_2}$



$$r_1 = \left[(x - (\mu - 1))^2 + y^2 + z^2 \right]^{1/2}$$

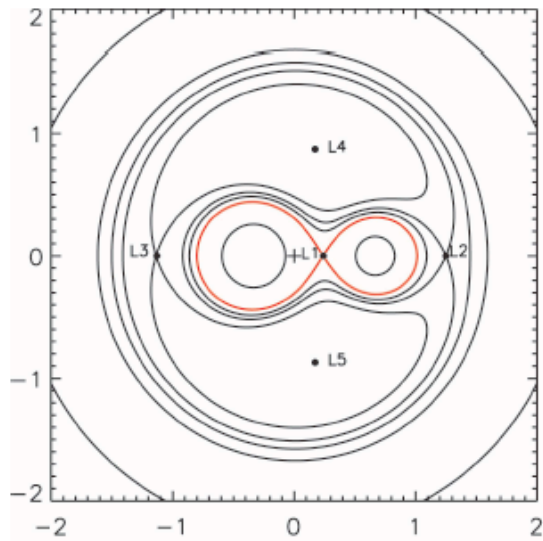
$$r_2 = \left[(x - \mu)^2 + y^2 + z^2 \right]^{1/2}$$

$$r_3 = \left[x^2 + y^2 \right]^{1/2}$$

in units where the orbital period and separation are taken as unit time and distance, and total mass as unit mass.

Roche lobe (IV)

Critical surfaces whose intersection with the orbital plane form a figure eight = **Roche lobes**



$$R_{R,2}/a = \begin{cases} 0.38 + 0.2 \log q, & 0.5 \leq q \leq 20, \\ 0.462 \left(\frac{q}{1+q} \right)^{1/3}, & 0 < q < 0.5, \end{cases}$$

where $q = M_2/M_1$,
and a is the orbital separation.

asymmetric !

Paczynski 1971, ARA&A 9, 183

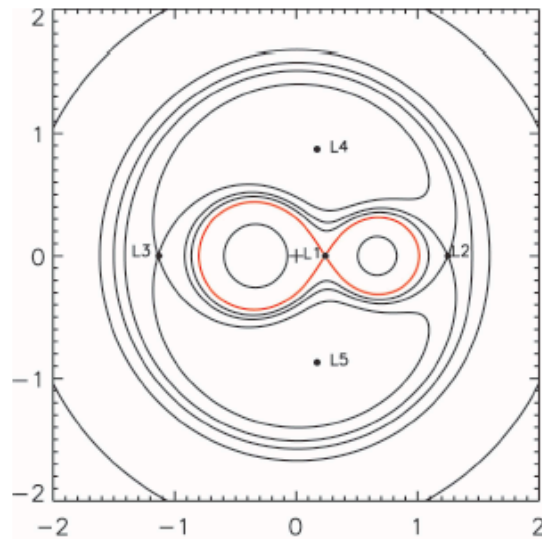
An alternative expression, valid for all q , is

$$R_{R,2}/a = \frac{0.49 q^{2/3}}{0.6 q^{2/3} + \ln(1 + q^{1/3})}$$

Eggleton, 1983, ApJ 268, 368

Roche lobe (IV)

Critical surfaces whose intersection with the orbital plane form a figure eight = **Roche lobes**



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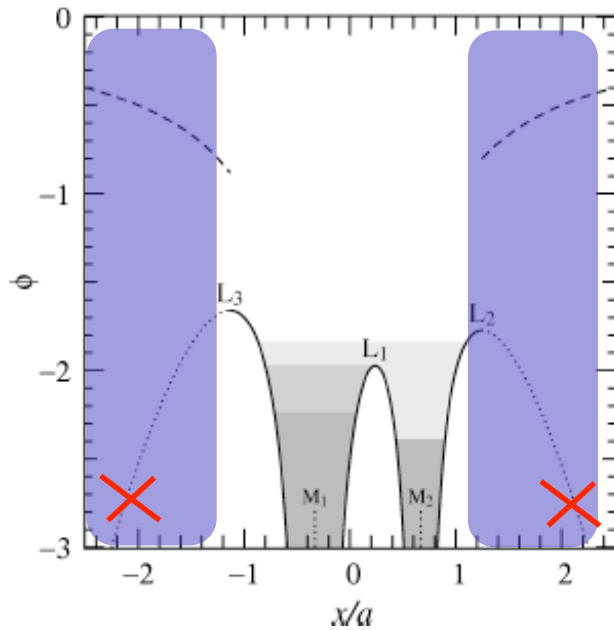
Do not confuse radius of Roche lobe $R_{R,2}$ with distance between star(s) and L_1 :

$$r(M_1 \text{ to } L_1) = a (0.50 + 0.227 \log q)$$

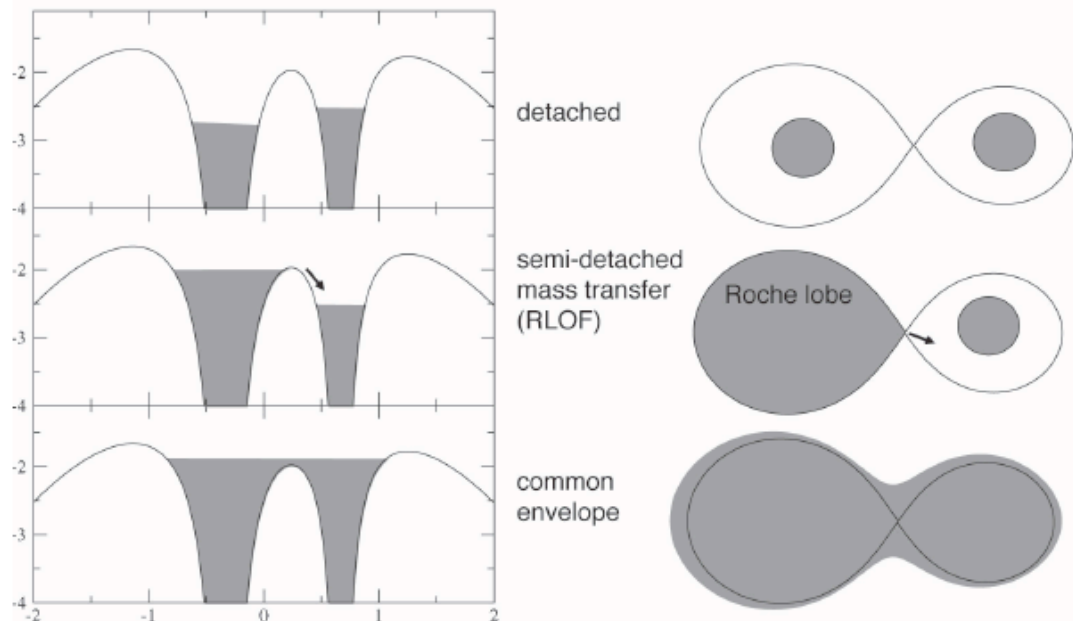
$$r(M_2 \text{ to } L_1) = a (0.50 - 0.227 \log q)$$

Roche lobe (V)

Note that co-rotation cannot be maintained outside the potential wells !



Different situations are possible:



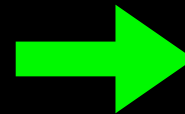
The binary zoo

Classification of binary stars

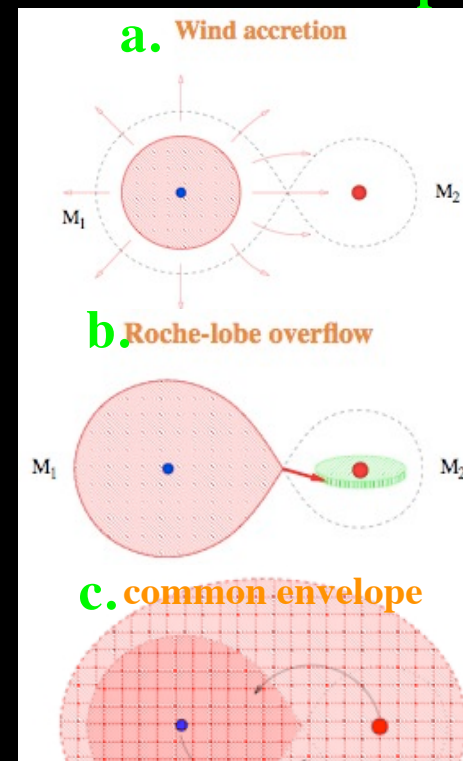
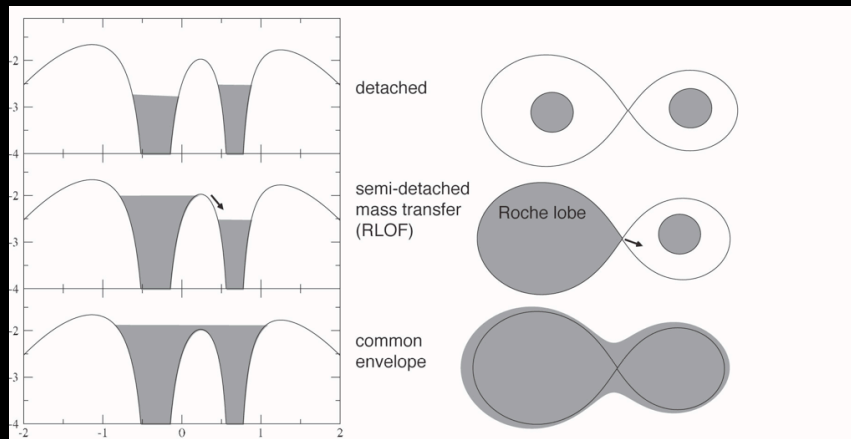
i)

- a. Detached system
- b. Semi-detached system
- c. Contact system

Mass transfer:



- a. wind accretion
- b. Roche-lobe overflow
- c. common envelope (transient or stationary)



The binary zoo

Classification of binary stars

i) Mass transfer

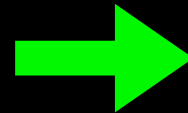
A technical parenthesis about

[→ Lionel Siess]

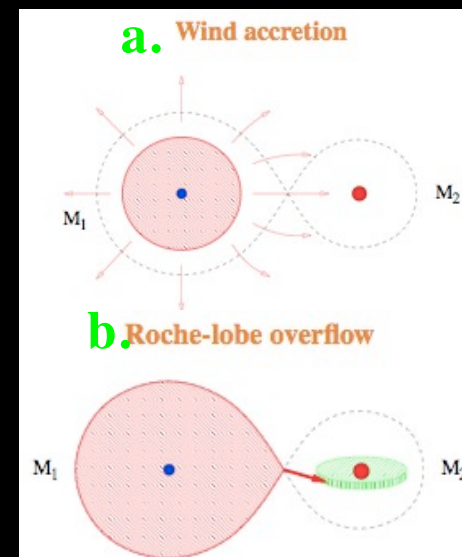
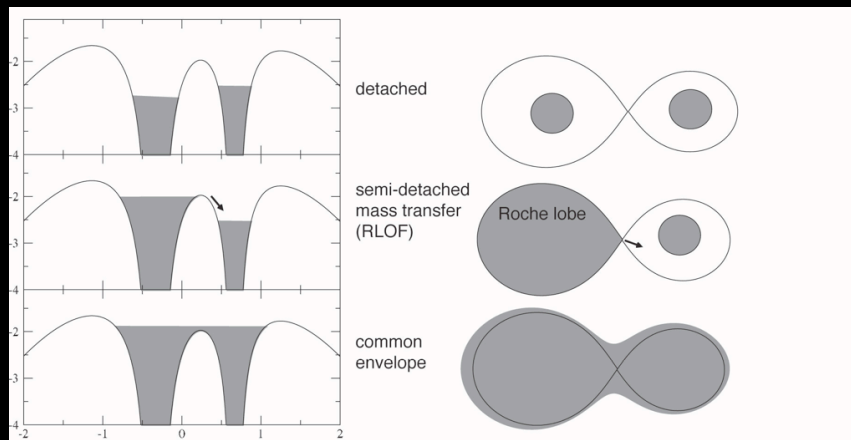
mass transfer rates and their associated time scales

- a. Detached system
- b. Semi-detached system
- c. Contact system

Mass transfer:



- a. wind accretion
- b. Roche-lobe overflow

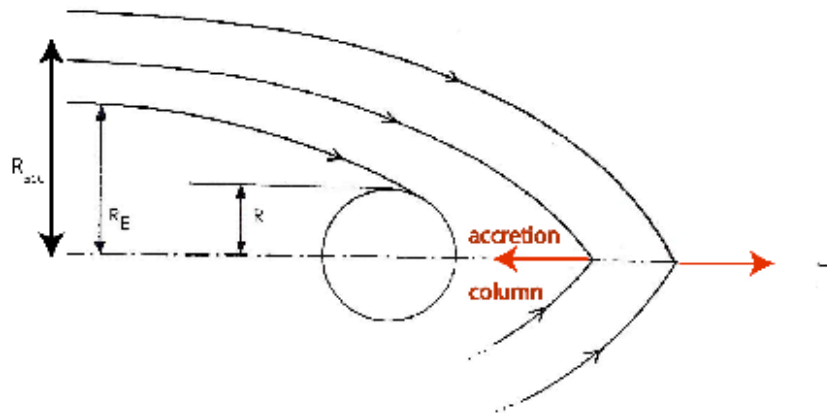


mass transfer rates

Wind accretion: $R < R_R$

1. Hoyle-Lyttleton formalism for a **single star** accreting matter flowing at a velocity v_∞ , with gas pressure unimportant (hence cool gas):

Accretion radius: $v_\infty^2/2 = GM/R_{H-L}$



Hoyle & Lyttleton 1939, Proc. Cam. Phil. Soc. 35, 405

Bondi 1952, MNRAS 114, 195

Bondi & Hoyle 1944, MNRAS 104, 273

mass transfer rates

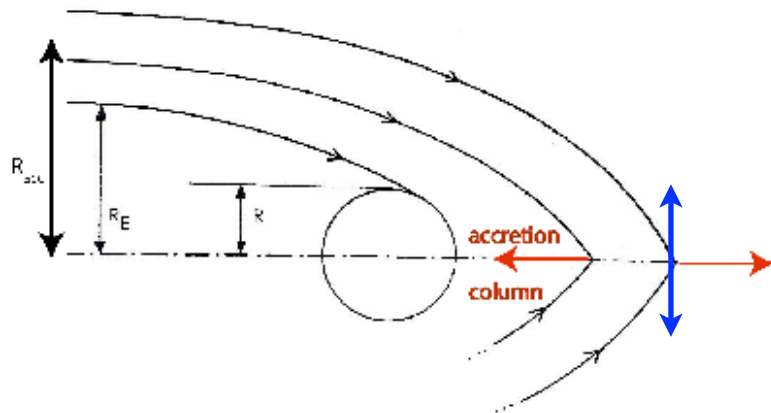
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Accretion rate:

$$\dot{M}_{H-L} = \pi R_{H-L}^2 v_\infty \rho_\infty = 2\pi \frac{(GM)^2}{v_\infty^3} \rho_\infty$$



Note that there is no accretion of angular momentum because the **tangential velocity components** cancel out

Hoyle & Lyttleton 1939, Proc. Cam. Phil. Soc. 35, 405

Bondi 1952, MNRAS 114, 195

Bondi & Hoyle 1944, MNRAS 104, 273

mass transfer rates

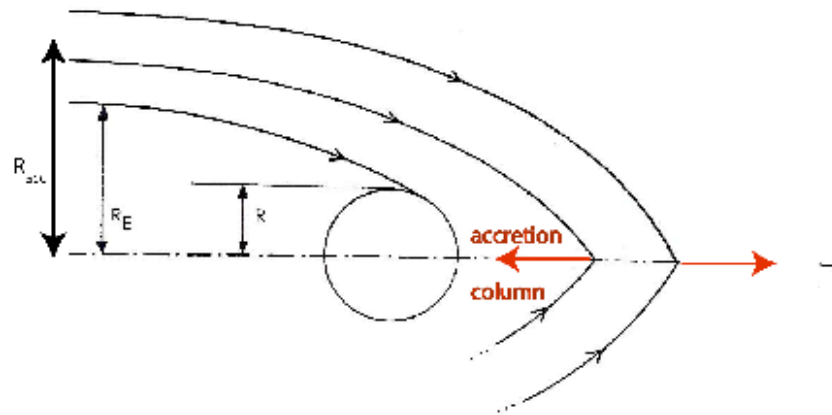
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2. Bondi formalism for accretion dominated by gas pressure, with zero relative gas-star velocity:

Accretion radius: $c^2/2 = GM/R_B$

Accretion rate: $\dot{M}_B = \beta \pi R_B^2 c \rho_\infty$

where c = sound speed, β is a parameter of order unity depending on the polytropic index of the gas.

Hoyle & Lyttleton 1939, Proc. Cam. Phil. Soc. 35, 405

Bondi 1952, MNRAS 114, 195

Bondi & Hoyle 1944, MNRAS 104, 273

mass transfer rates

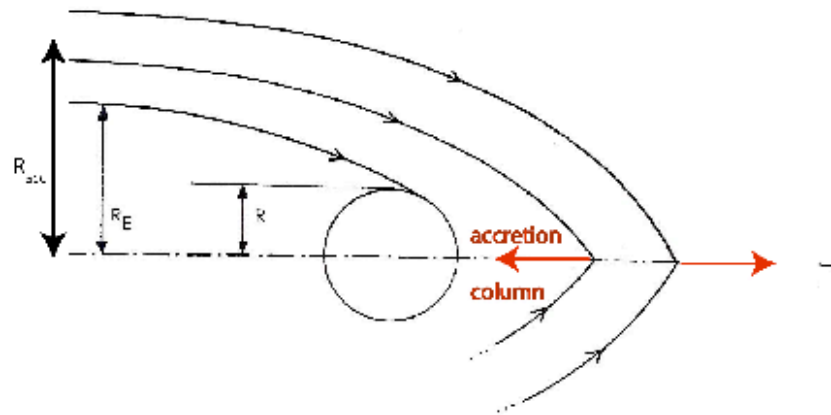
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3. Bondi-Hoyle formalism is an interpolation between these two extreme cases:

Accretion rate:

$$\dot{M}_{B-H} =$$

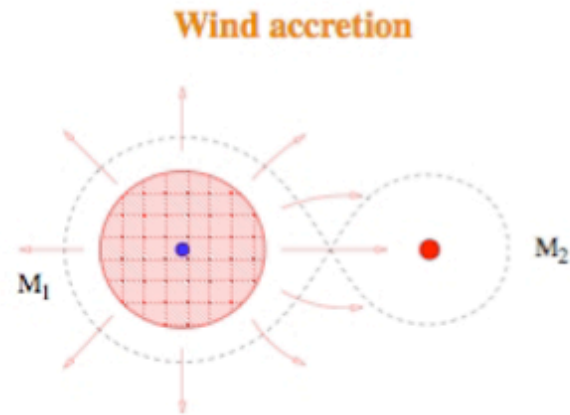
$$\beta \pi R_{H-L}^2 v_\infty \rho_\infty \left(\frac{(v_\infty/c)^2}{1+(v_\infty/c)^2} \right)^{3/2}$$

Hoyle & Lyttleton 1939, Proc. Cam. Phil. Soc. 35, 405

Bondi 1952, MNRAS 114, 195

Bondi & Hoyle 1944, MNRAS 104, 273

mass transfer rates
Wind accretion: $R < R_R$



In a **binary system**:

- ρ_∞ from $\dot{M}_{\text{wind}} = 4\pi r^2 \rho(r) v_{\text{wind}}$,

with r set to a

- v_∞ replaced by $v_{\text{orb}} + v_{\text{wind}}$.

Thus:

$$\dot{M}_{\text{acc}} / \dot{M}_{\text{wind}} = -2\pi \frac{\beta}{a^2} \left(\frac{(G M_{\text{acc}})^2}{v_{\text{wind}}^2} \right)^2 \frac{1}{[1 + (v_{\text{orb}}/v_{\text{wind}})^2 + (c/v_{\text{wind}})^2]^{3/2}}$$

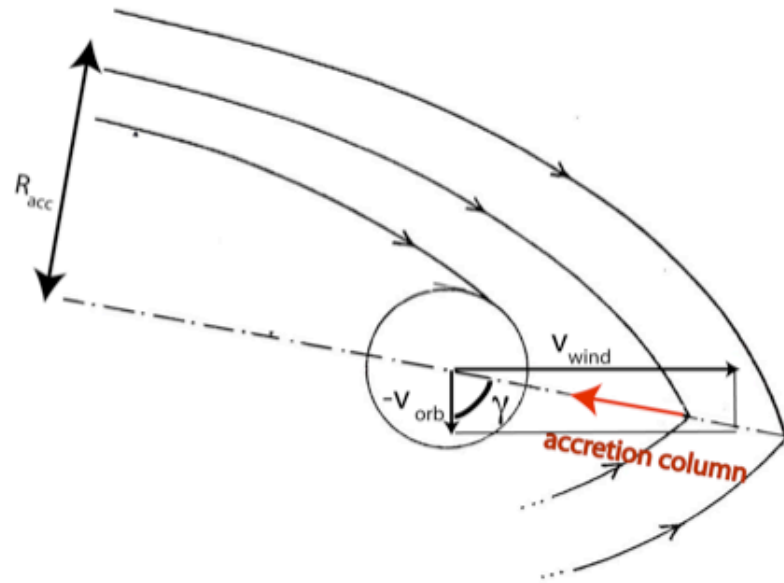
or using Kepler's third law:

$$\dot{M}_{\text{acc}} / \dot{M}_{\text{wind}} = -\beta \mu^2 \frac{k^4}{[1 + k^2 + (c/v_{\text{wind}})^2]^{3/2}},$$

where $\mu \equiv M_{\text{accretor}} / (M_{\text{accretor}} + M_{\text{loser}})$, $k = \frac{v_{\text{orb}}}{v_{\text{wind}}}$

mass transfer rates

Wind accretion: $R < R_R$

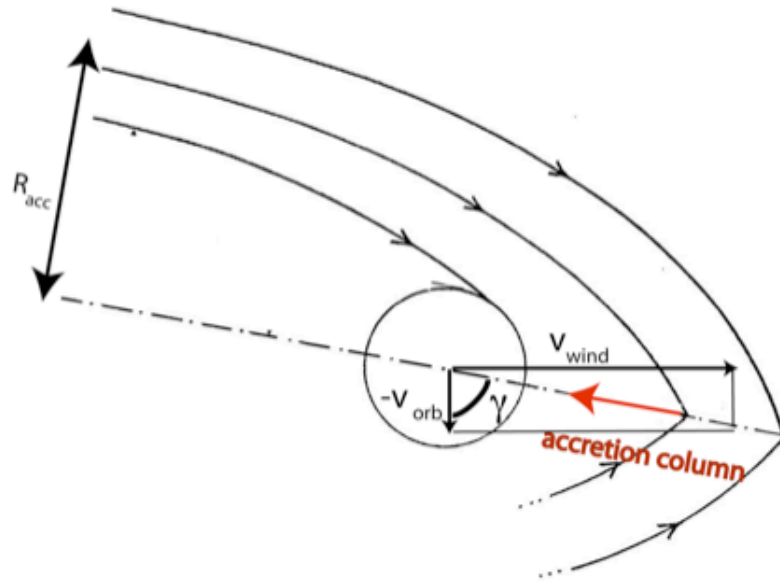


- **Fast winds** (binaries with OB stars):
 $k \equiv v_{\text{orb}}/v_{\text{wind}} \ll 1$

Accretion column, tilted by an angle $\gamma = \arctan v_{\text{wind}}/v_{\text{orb}}$ with respect to the orbital motion, with matter falling onto the compact star from its rear side (as viewed from the mass-losing star) with a rate \dot{M}_{B-H}

mass transfer rates

Wind accretion: $R < R_R$

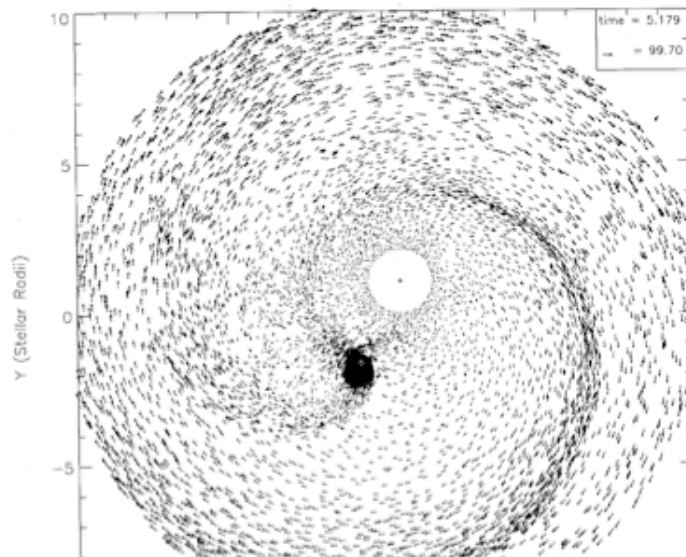


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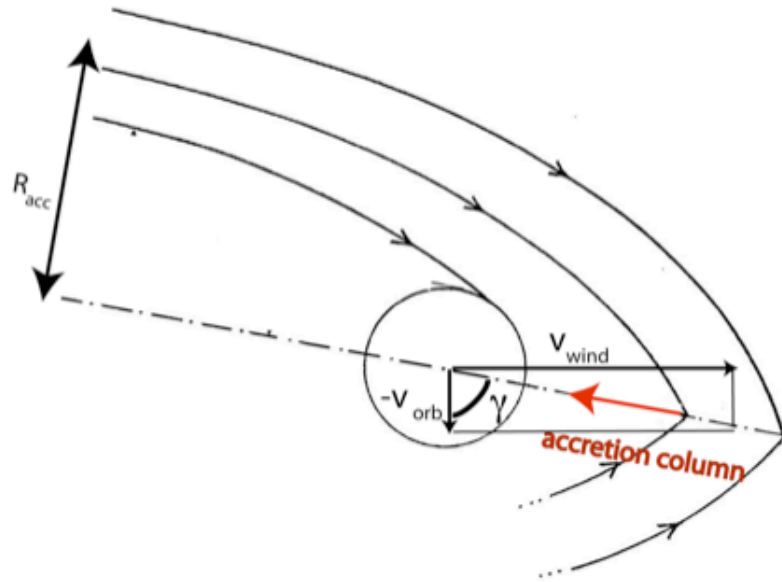
- **Slow winds** (detached binary systems involving an AGB star):
 $k \equiv v_{\text{orb}}/v_{\text{wind}} \gg 1$

Accretion column distorted by Coriolis effect, must be investigated numerically.



mass transfer rates

Wind accretion: $R < R_R$



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Accretion column distorted by Coriolis effect, must be investigated numerically.

Accretion rates $\leq 0.1 \dot{M}_{B-H}$

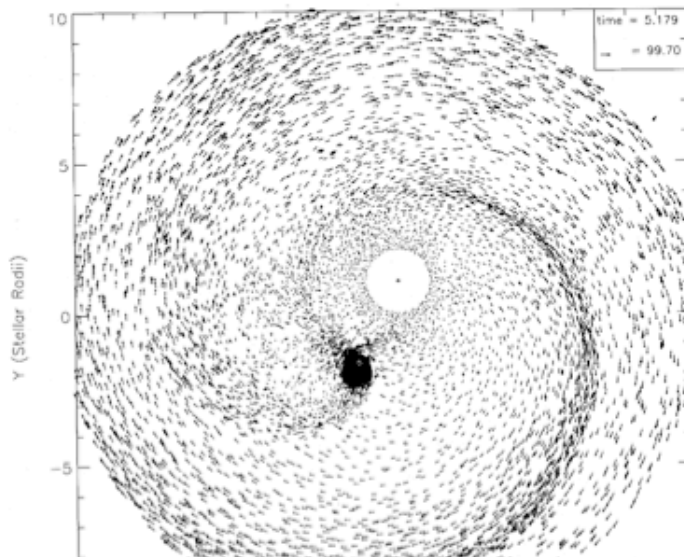
Theuns & Jorissen 1993, MNRAS 265, 946

Mastrodemos & Morris 1998, ApJ 497, 303

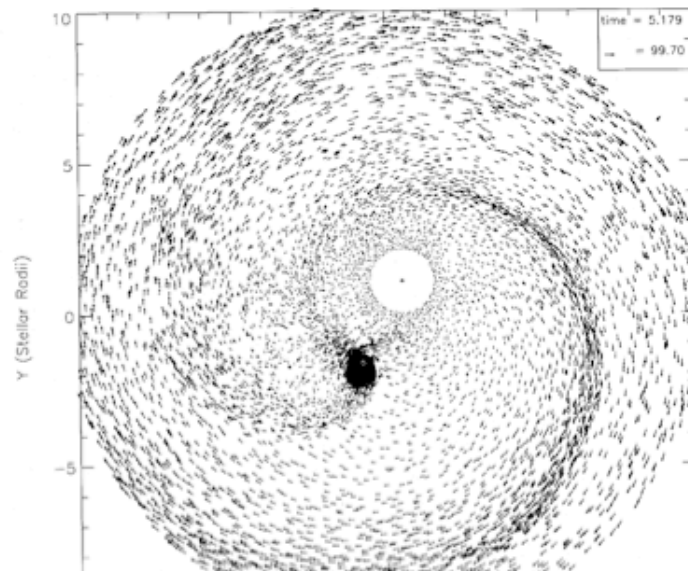
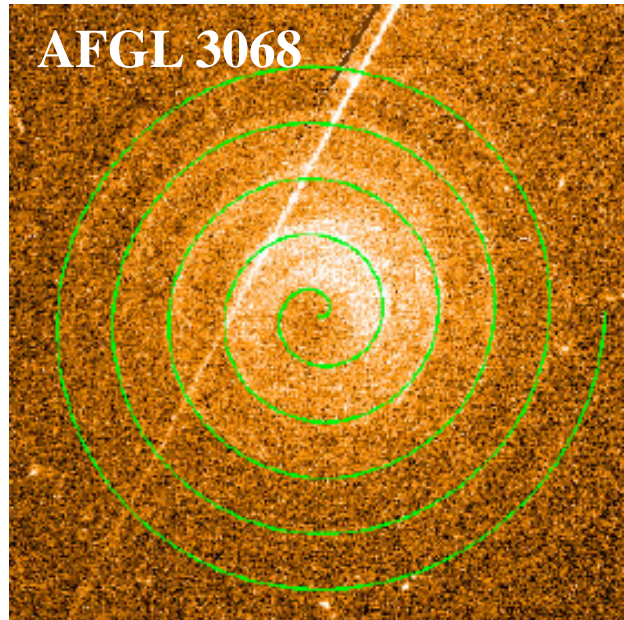
Folini & Walder 2000, Ap&SS 274, 189

Nagae et al. 2004, A&A 419, 335

Jahanara et al., 2005, A&A 441, 589



mass transfer rates
Wind accretion: $R < R_R$



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Theuns & Jorissen 1993, MNRAS 265, 946

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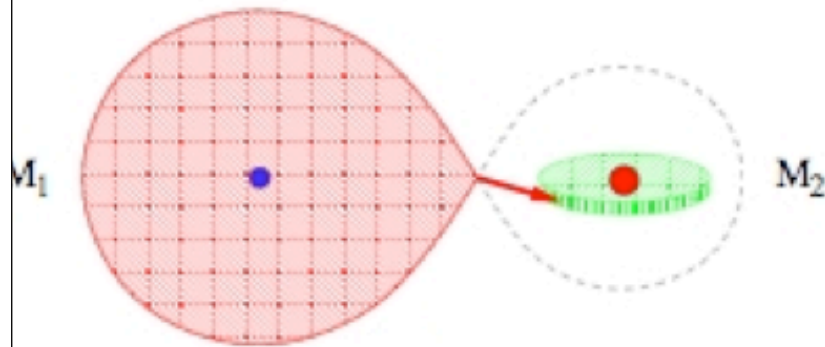
‘Spiral arm’ feature has been observed in some binary systems: AFGL 3068, R Scl

mass transfer rates

$$\text{RLOF} : R = R_R$$

conservative mass transfer $\dot{M}_{\text{acc}} = \dot{M}_{\text{RLOF}}$

Roche-lobe overflow



\dot{M}_{RLOF} is limited by the flow compression through the inner Lagrangian point, where it flows at sound speed with a rate:

$$-\dot{M}_{\text{RLOF}} = \dot{M}_{\text{loser}} e^{\left(\frac{-(R_R - R)}{H_P}\right)},$$

where H_P is the pressure scale height in the mass-donor star, \dot{M}_{loser} is a characteristic mass-loss rate of the donor.

Lubow & Shu 1975, ApJ 198, 383

Ritter 1988, A&A 202, 93

Kolb & Ritter 1990, A&A 236, 385

The binary zoo

Classification of binary stars:

i) Mass transfer

- a. Detached system
- b. Semi-detached system
- c. Contact system



ii) Observational properties

a. Detached system

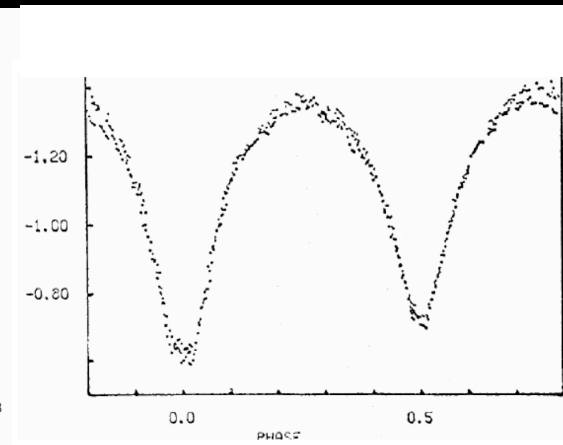
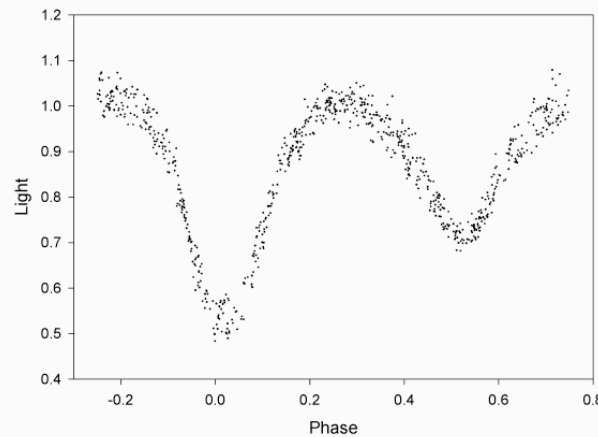
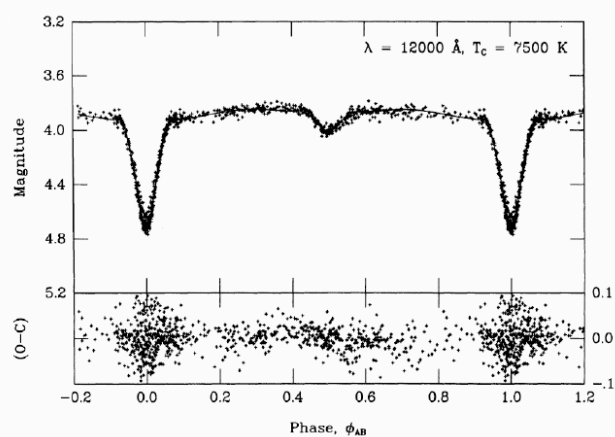
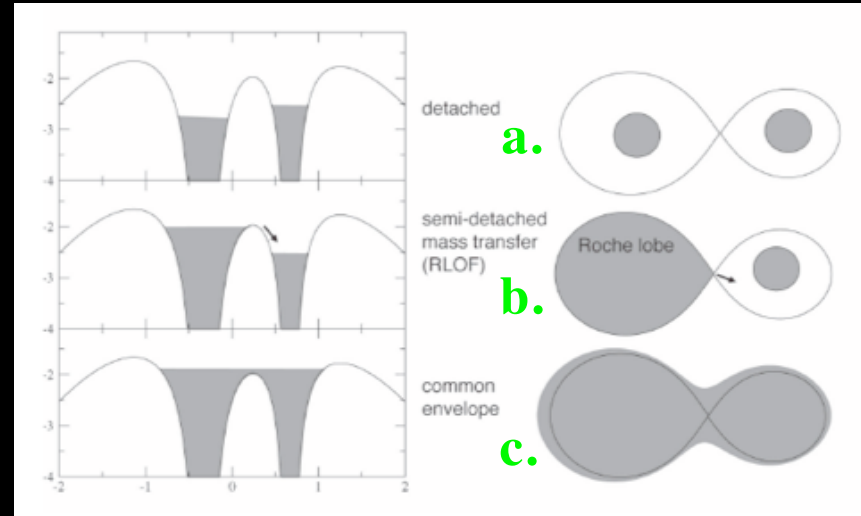
photometric binary [eclipses]

b. Semi-detached system

c. Contact system

β Lyr

W UMa



The binary zoo

Classification of binary stars:

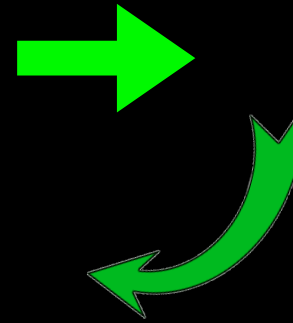
There are three possible ways to classify binary stars, based on:

i)

Mass transfer:

- a. Detached system
- b. Semi-detached system
- c. Contact system

- a. wind accretion
- b. Roche-lobe overflow

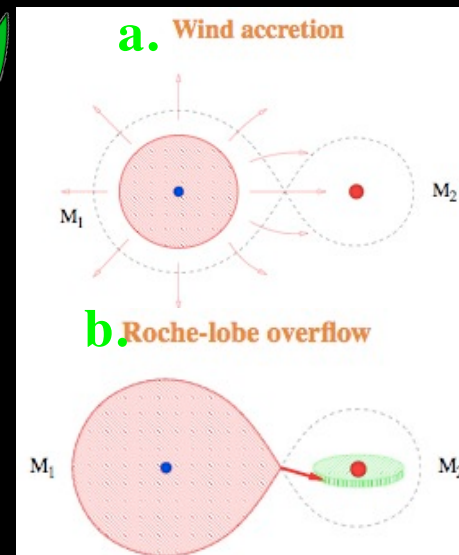


ii) Observational properties

- a. photometric binary Ex: Algols
- b. X-ray binary Ex: Algols
- c. [peculiar] 'abundance' binary

Ex: Algols (CNO)

iii) Evolutionary stage

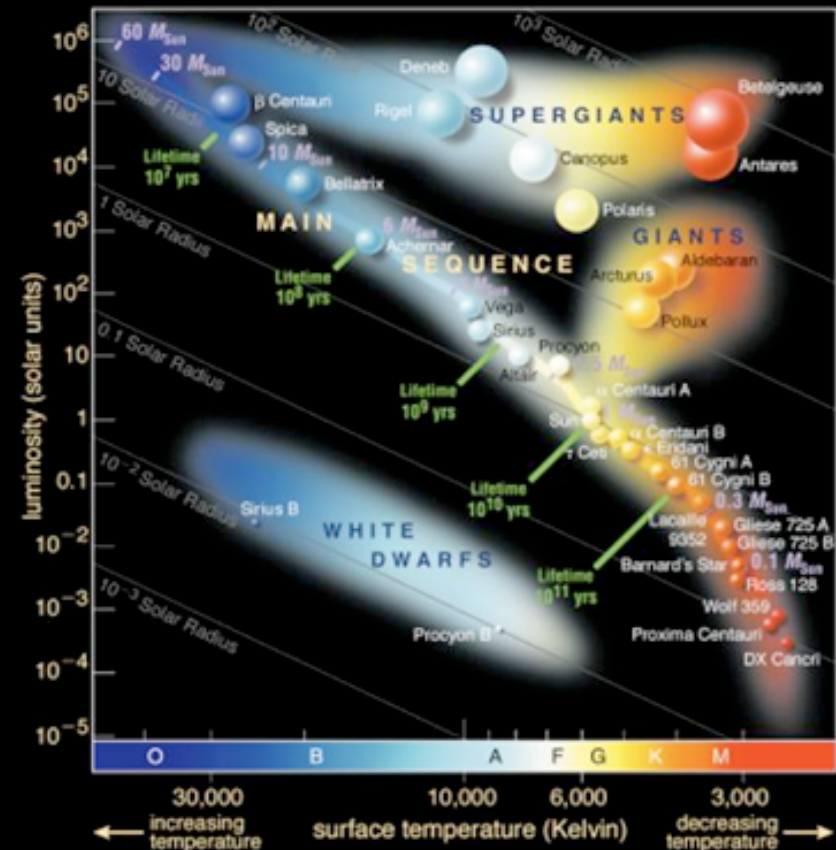


The binary zoo

Classification of binary stars:

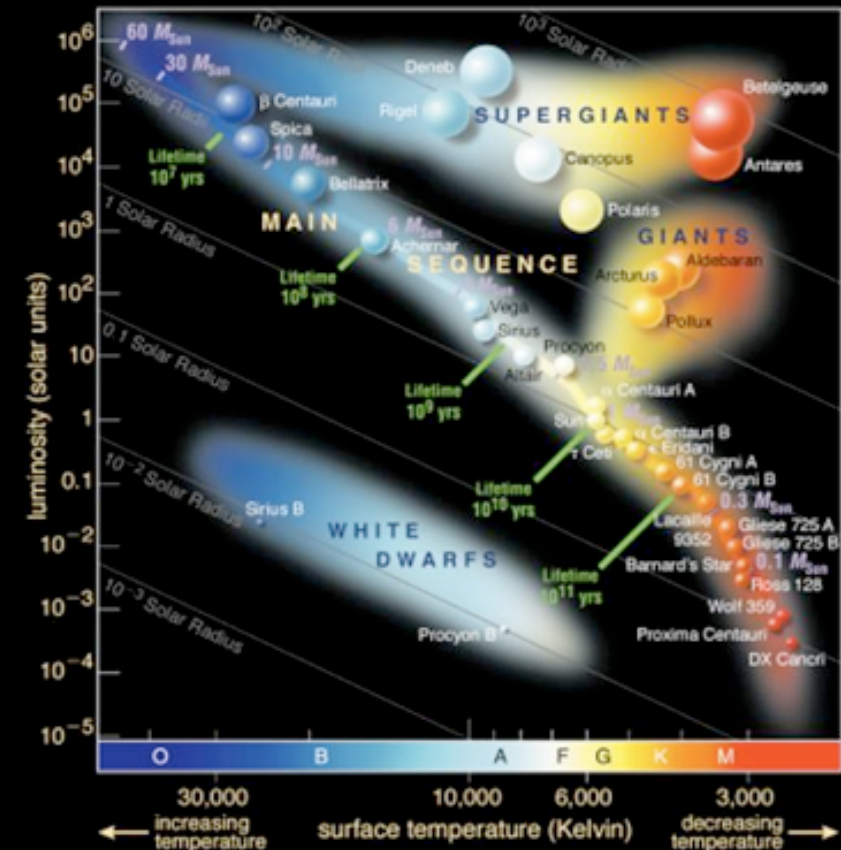
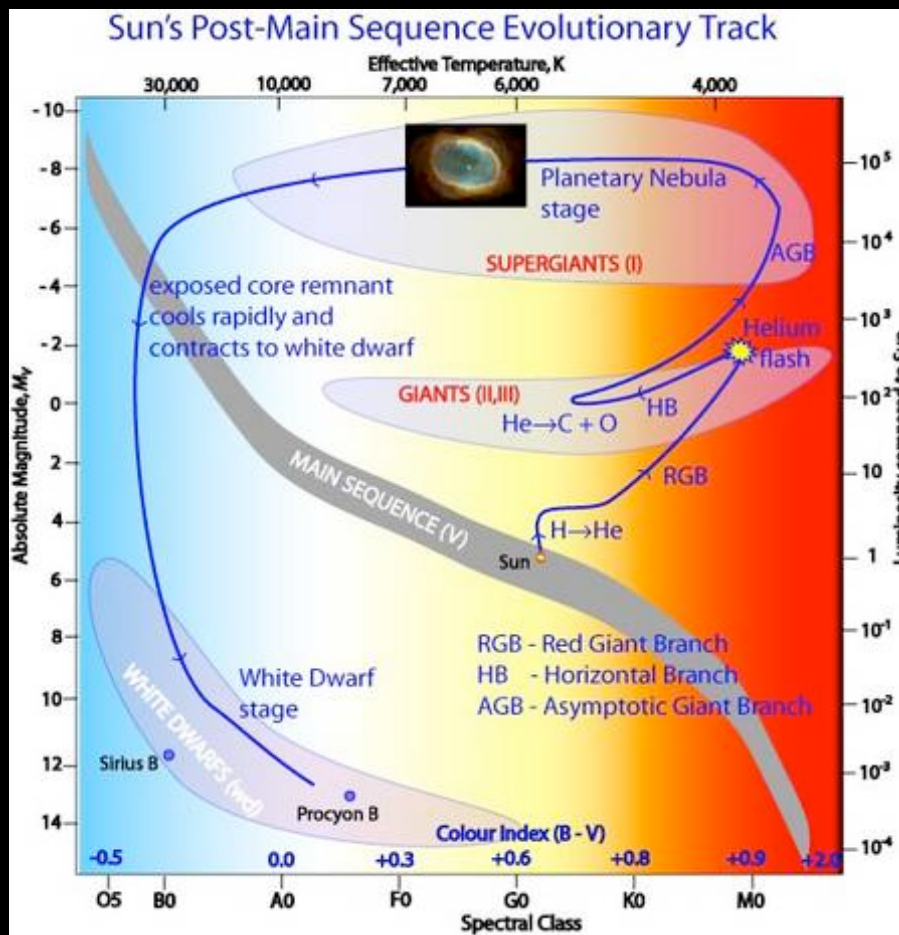
There are three possible ways to classify binary stars, based on:

iii) Evolutionary stage



There are three possible ways to classify binary stars, based on:

iii) Evolutionary stages, connected through stellar-evolution tracks [→ Siess]



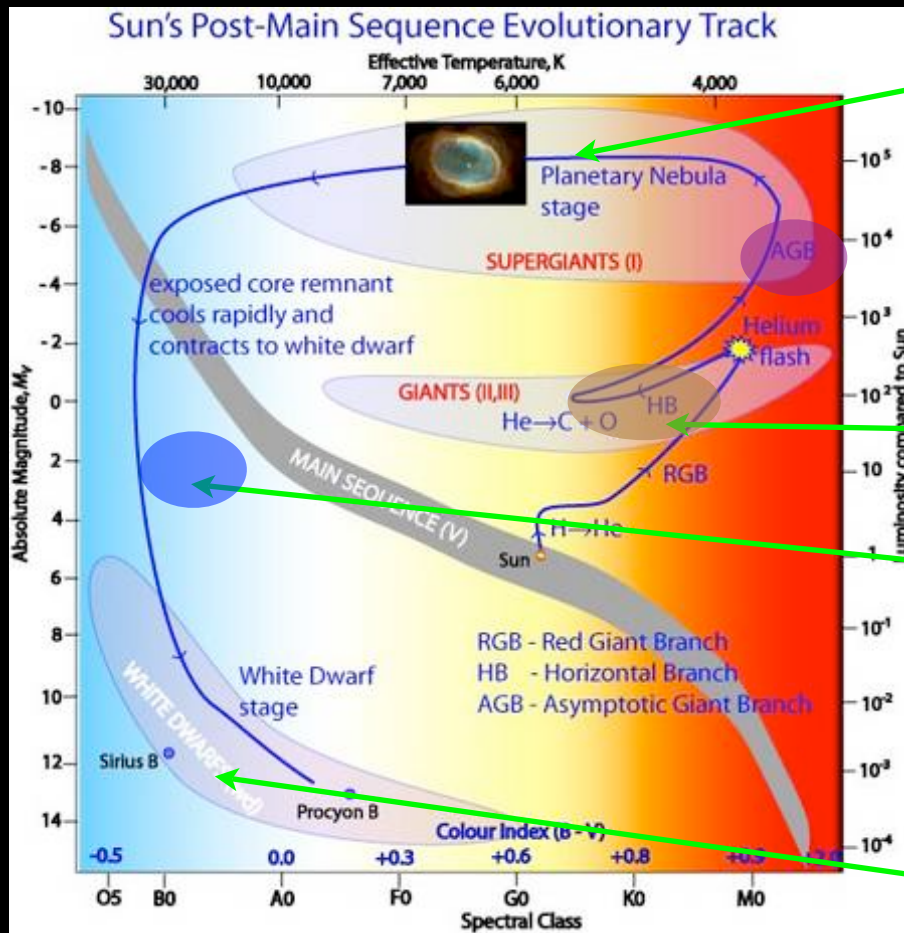
There are three possible ways to classify binary stars, based on:

iii) Evolutionary stage

A few examples of binaries defined by their evolutionary stages

[peculiar] 'abundance' binary:

- metal-depleted post-AGB star



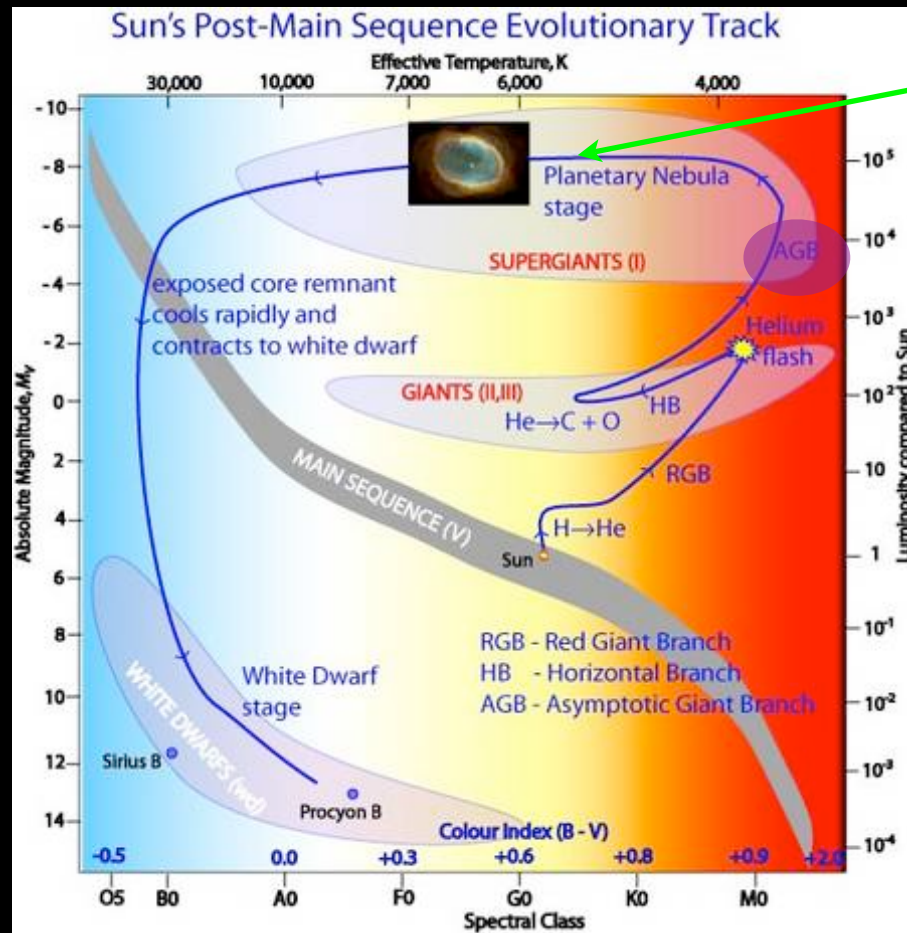
- K giant with strong barium lines
[= Barium star]

- sdB

- binary with compact companion
(BH, WD) [\rightarrow Nelemans]

iii) Evolutionary stage

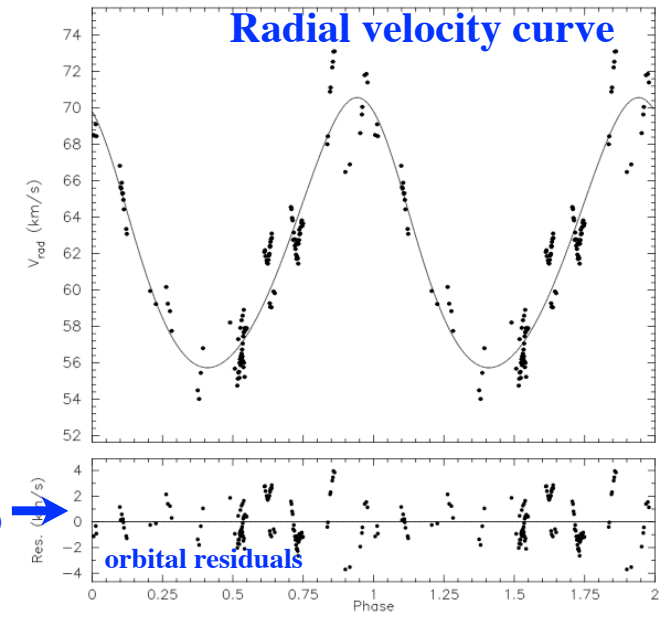
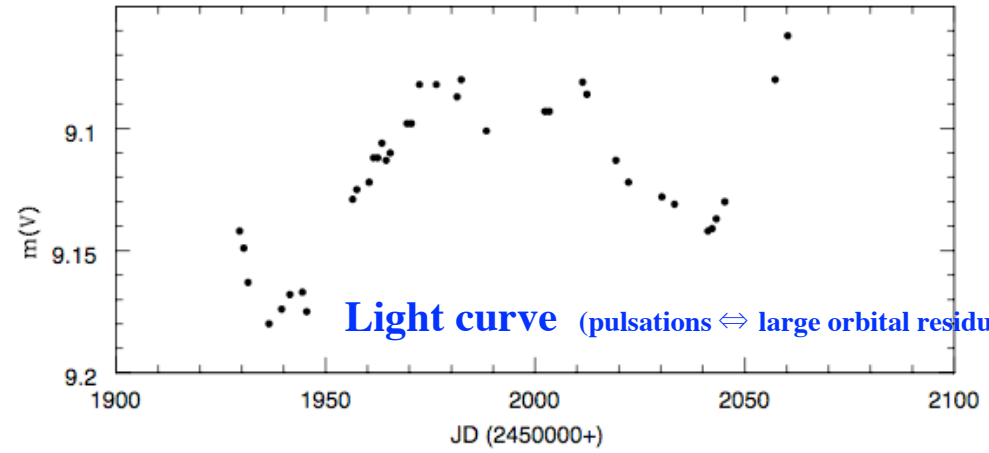
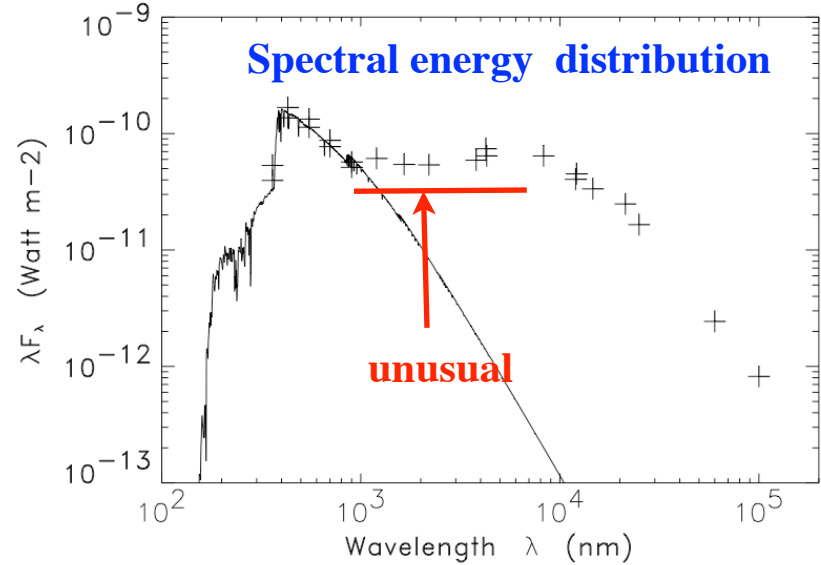
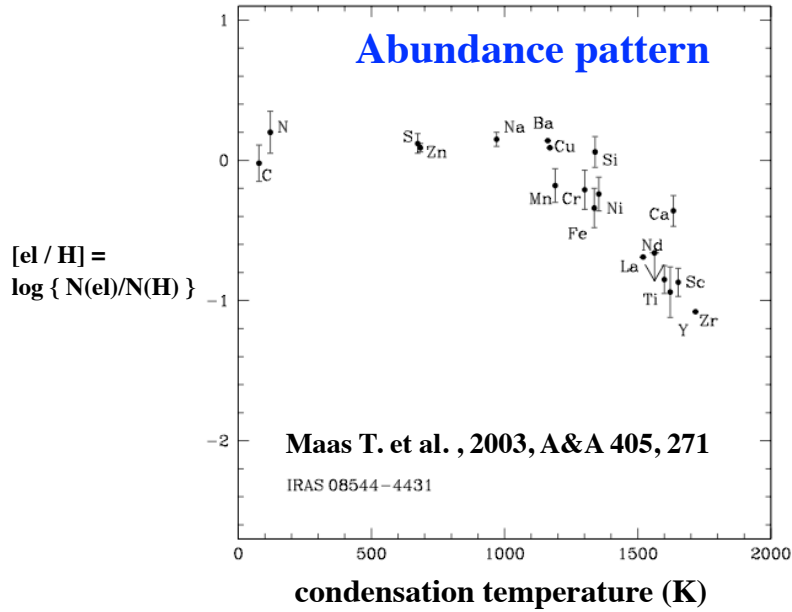
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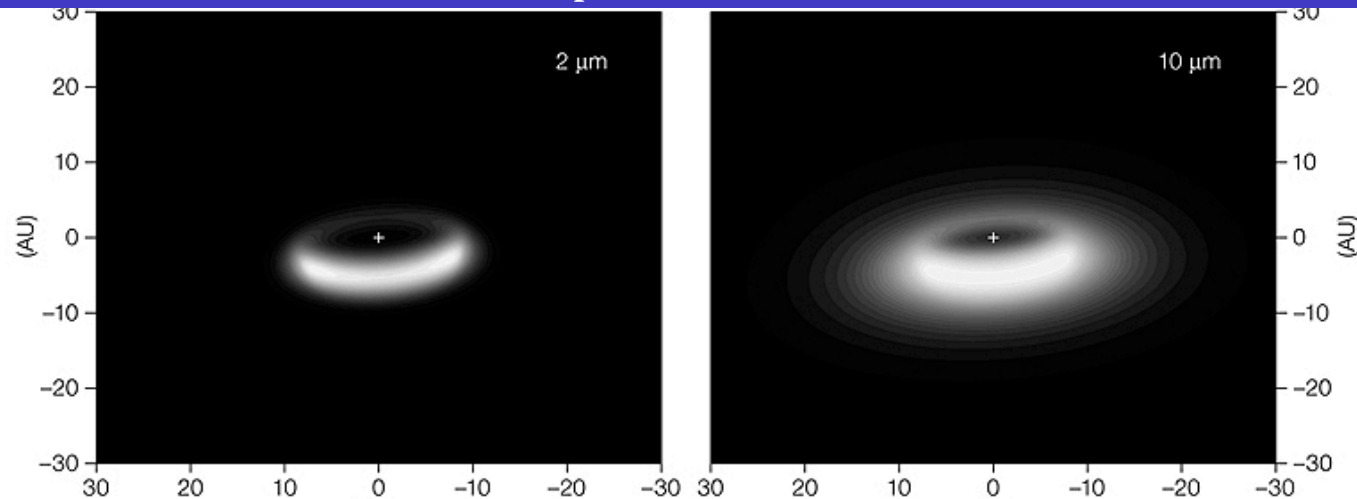
[peculiar] ‘abundance’ binary:
- metal-depleted post-AGB star

Plus the correlation with the post-AGB nature

Four correlated observational properties :

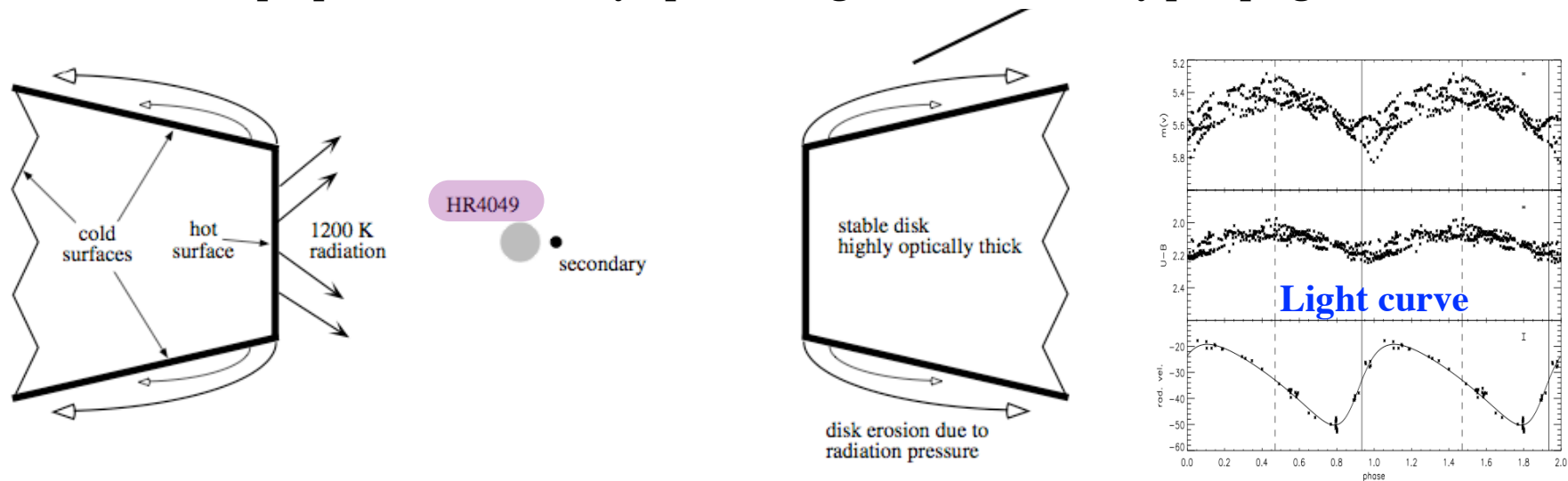


post-AGB stars



The circumbinary disc accounts:

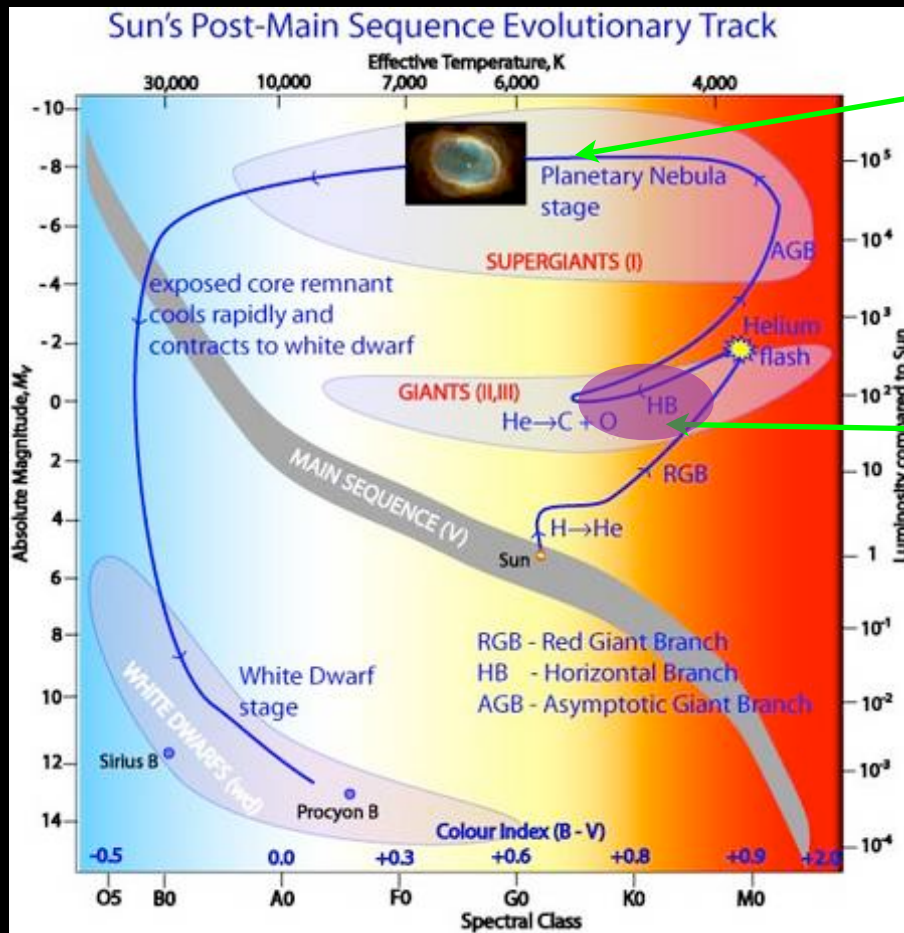
- for the peculiar spectral energy distribution (warm dust is stored in the inner part of the disc)
- for the depletion pattern (re-accretion of refractory-depleted gas)
- for the orbital modulation of the light curve (in the absence of pulsations)
- for the orbital properties (eccentricity - period diagram ; “eccentricity pumping”)



There are three possible ways to classify binary stars, based on:

iii) Evolutionary stage

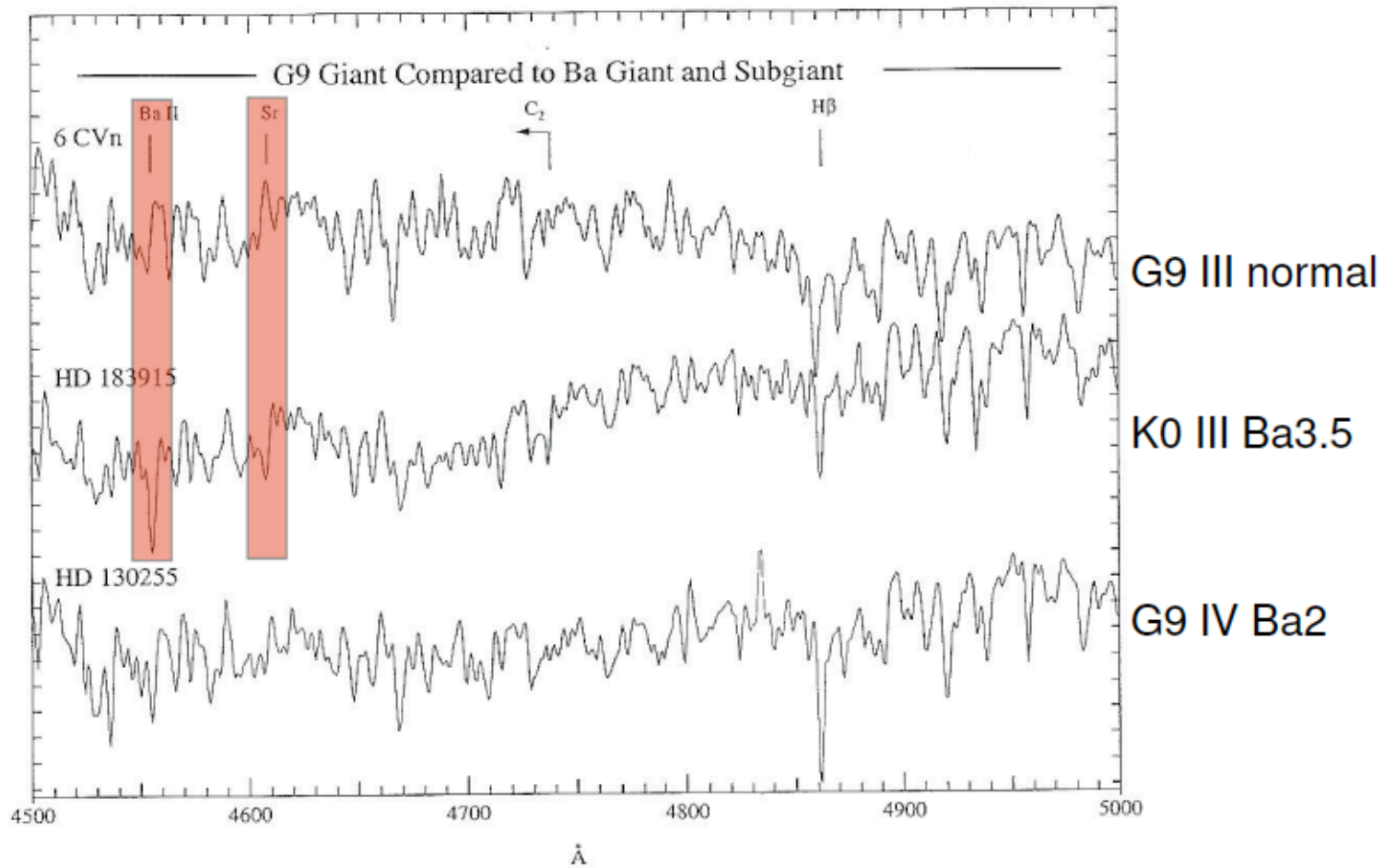
[peculiar] 'abundance' binary:
- metal-depleted post-AGB star



- K giant with strong barium lines
[= Barium star]

Barium stars

Ba stars: A class of chemically-peculiar giants known since the 50's

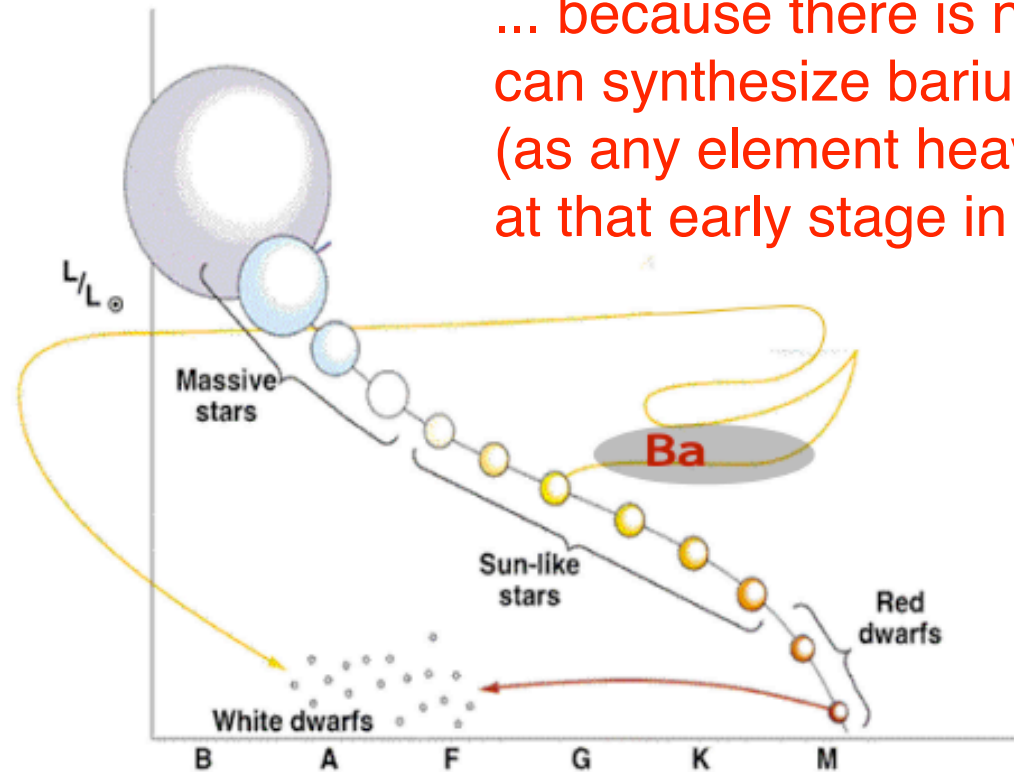


Barnbaum (1996), ApJS 105, 419

Barium stars


Ba stars: A class of chemically-peculiar giants known since the 50's
Chemical peculiarities attributed to mass transfer...

... because there is no way a star can synthesize barium
(as any element heavier than Fe)
at that early stage in the evolution



© 1997 Wadsworth Publishing Company/ITP

Barium stars

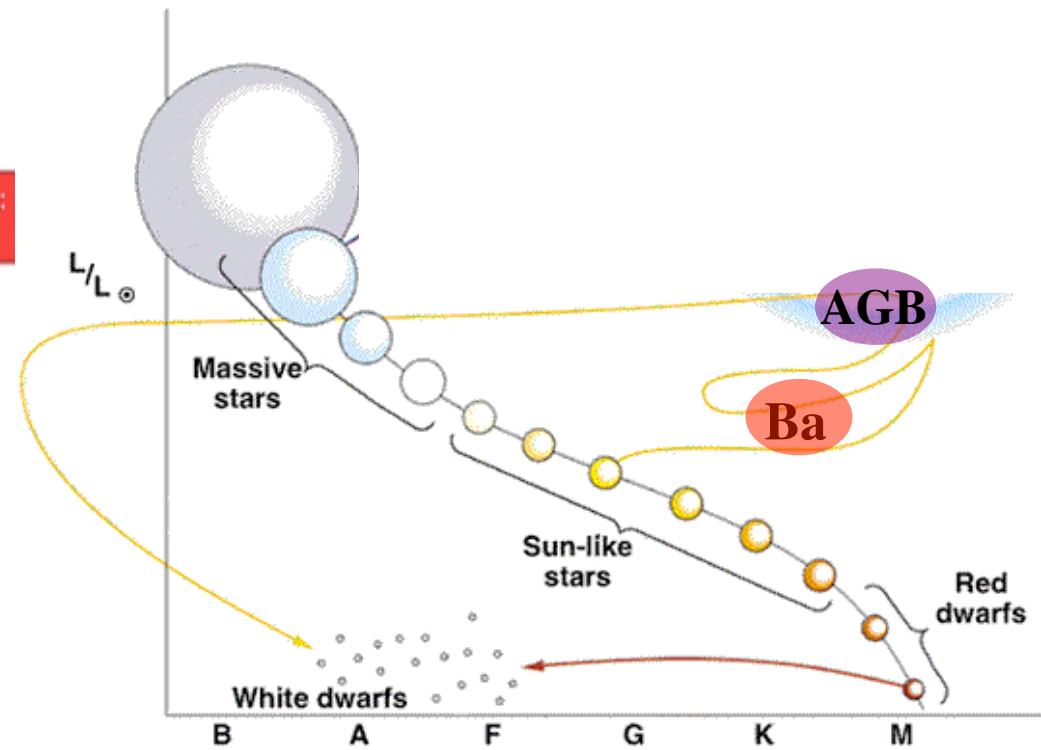
Main sequence 

RGB 

Synthesis of He-burning nucleosynthesis products:
12C, 19F, s-process elements (Sr, Ba, Tc, Pb...)

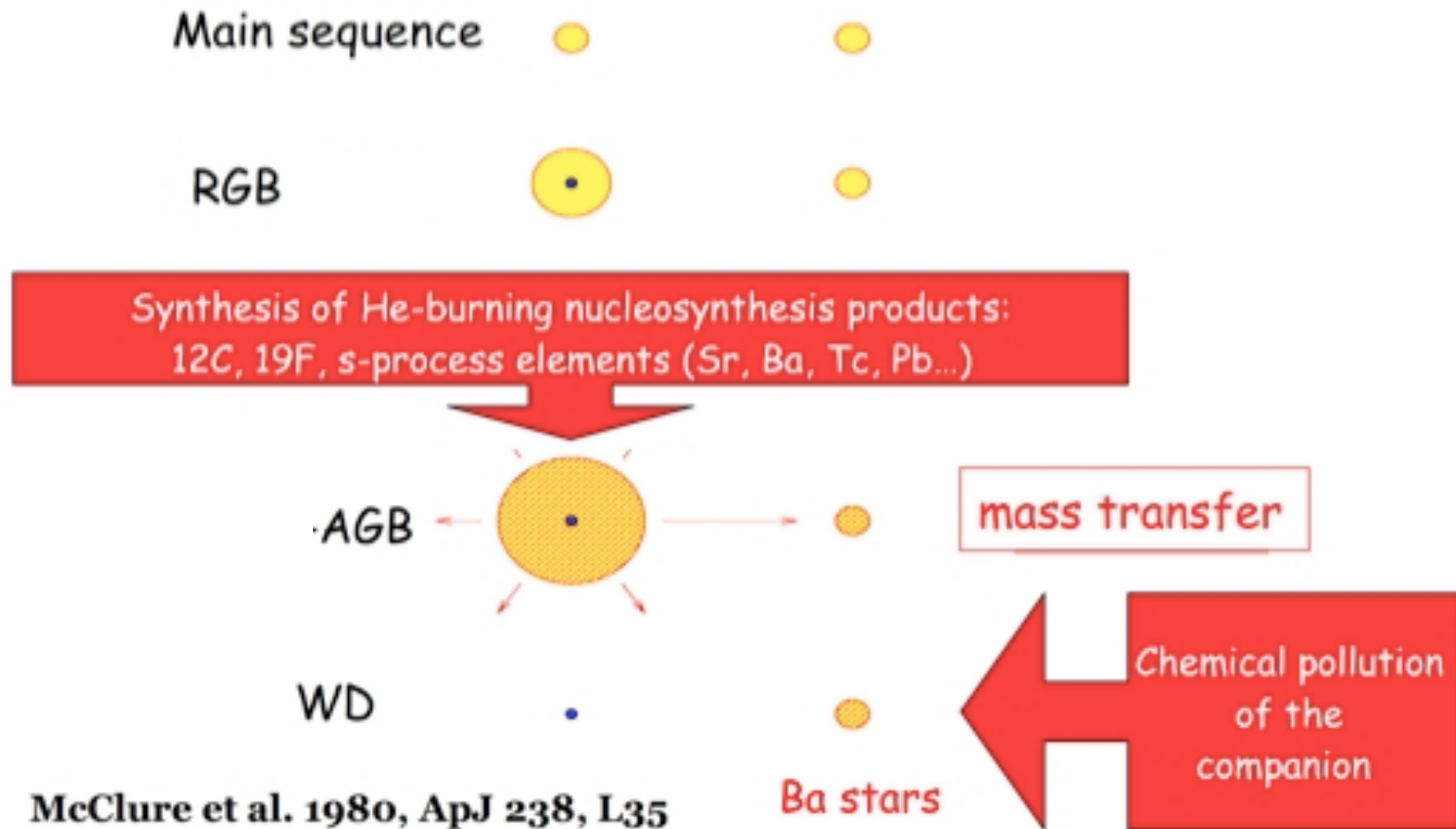


WD 



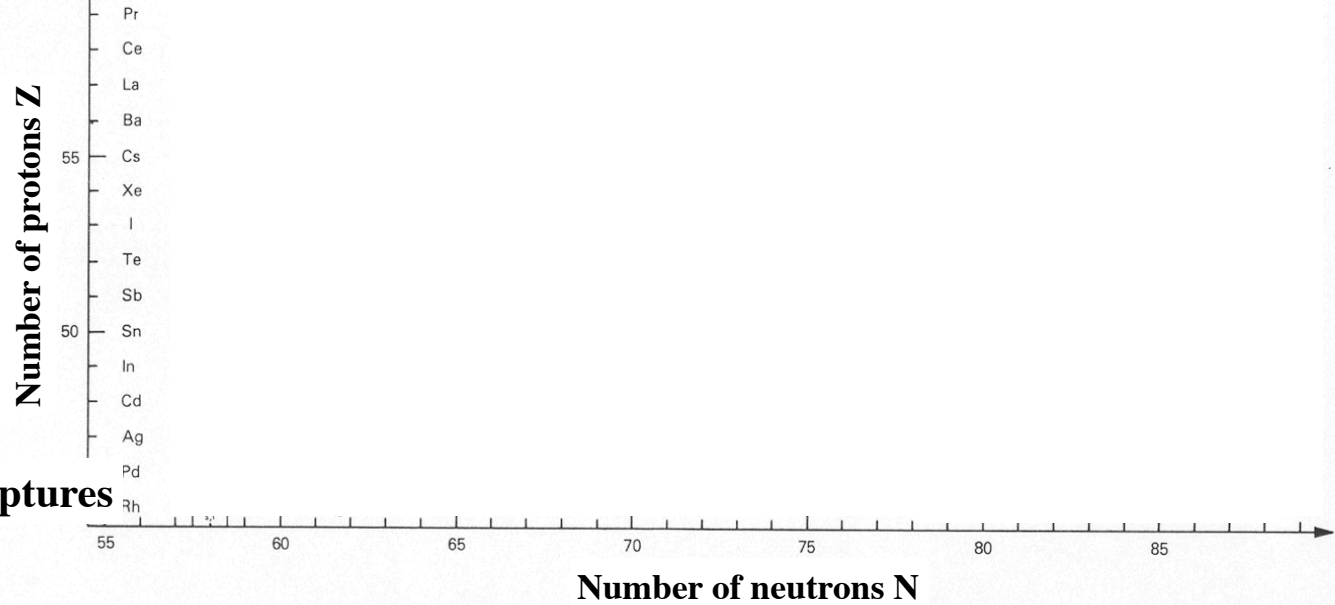
Barium stars

A technical parenthesis about the synthesis of heavy elements

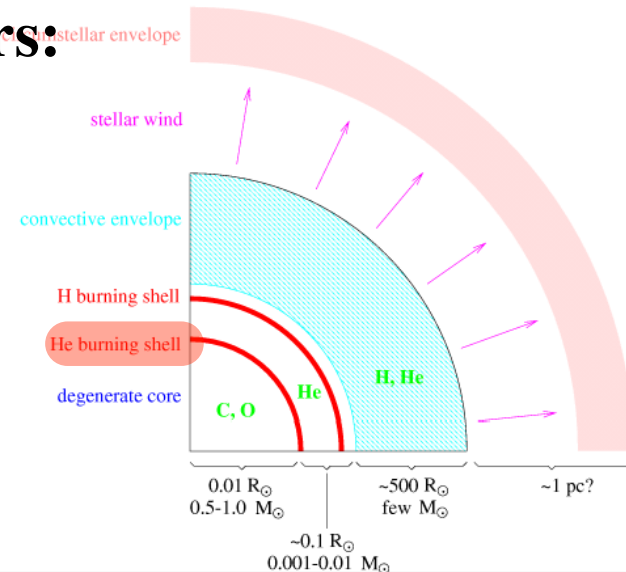
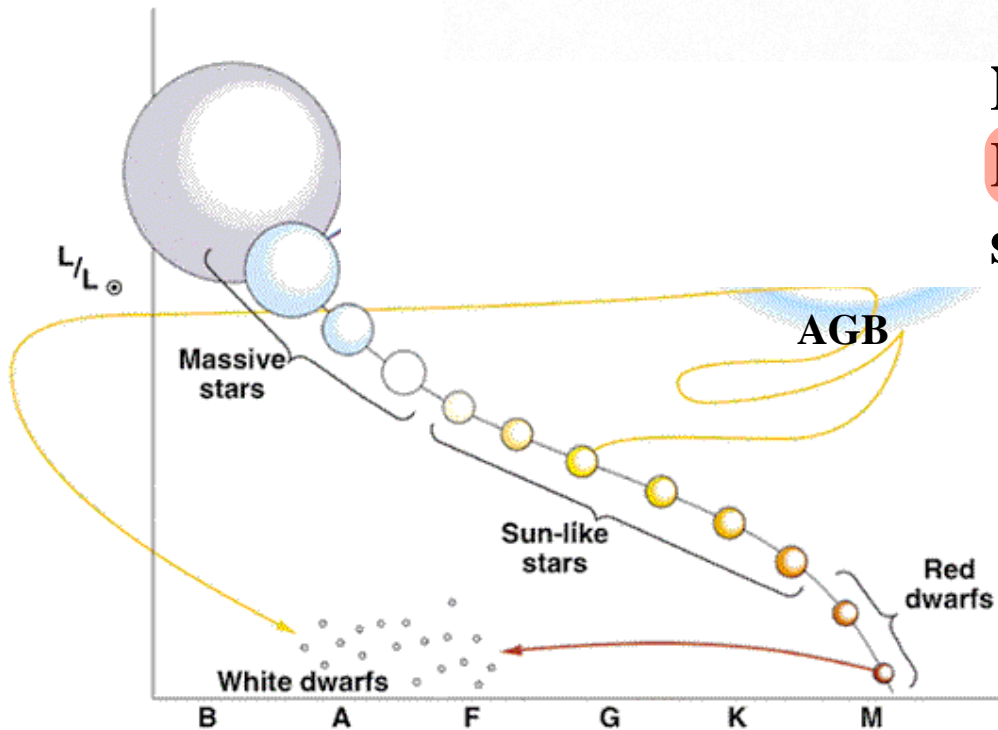


A technical parenthesis about the synthesis of heavy elements

= a chain of neutron captures

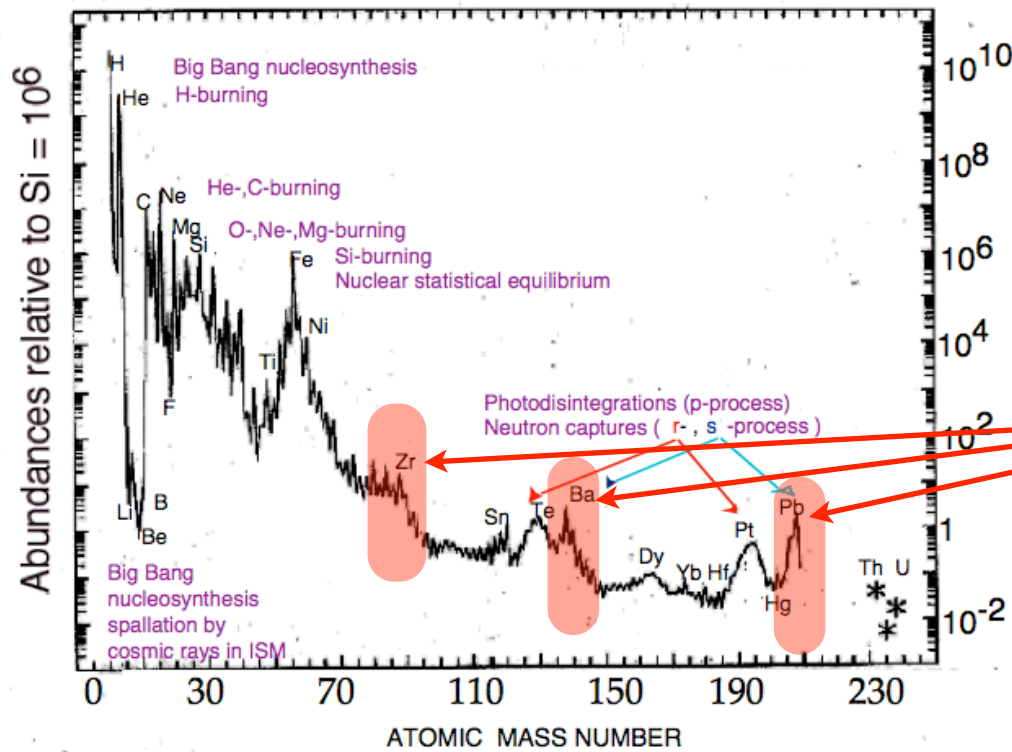
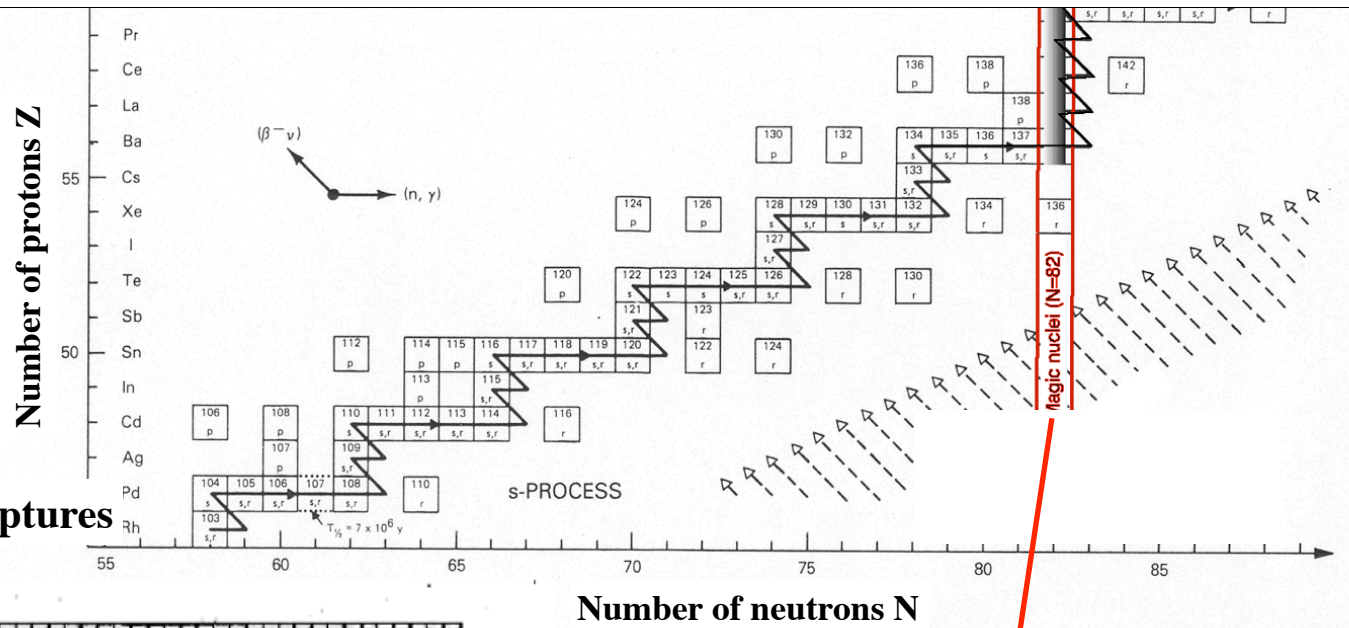


Neutrons are produced in the He-burning shell of AGB stars:



A technical parenthesis about the synthesis of heavy elements

= a chain of neutron captures



Nuclei with closed neutron shell ("magic nuclei")

**Small cross section
 → piles up
 → abundance peaks**

Main sequence ●

RGB ●

Synthesis of He-burning nucleosynthesis products:
12C, 19F, s-process elements (Sr, Ba, Tc, Pb...)

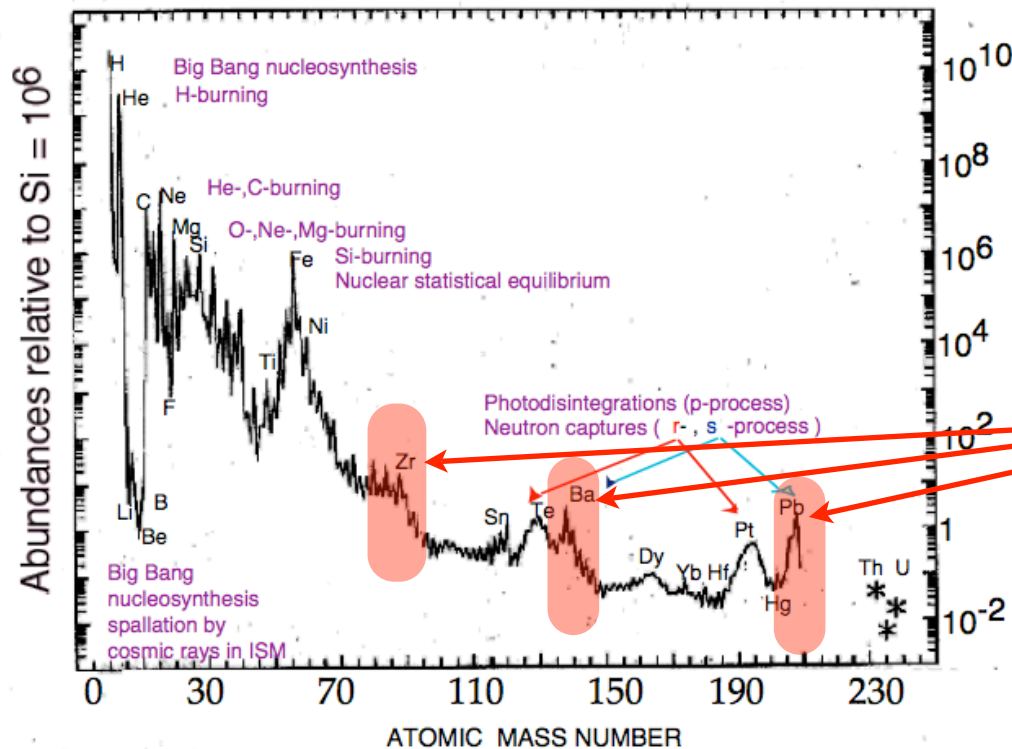
AGB

WD ●

Hence AGB stars become enriched in heavy elements, e.g. Zr

For instance, S stars = AGB stars

→ ZrO bands in S stars



Nuclei with closed neutron shell (“magic nuclei”)

Small cross section

→ piles up

→ abundance peaks

Main sequence ●

RGB ●

Synthesis of He-burning nucleosynthesis products:
12C, 19F, s-process elements (Sr, Ba, Tc, Pb...)

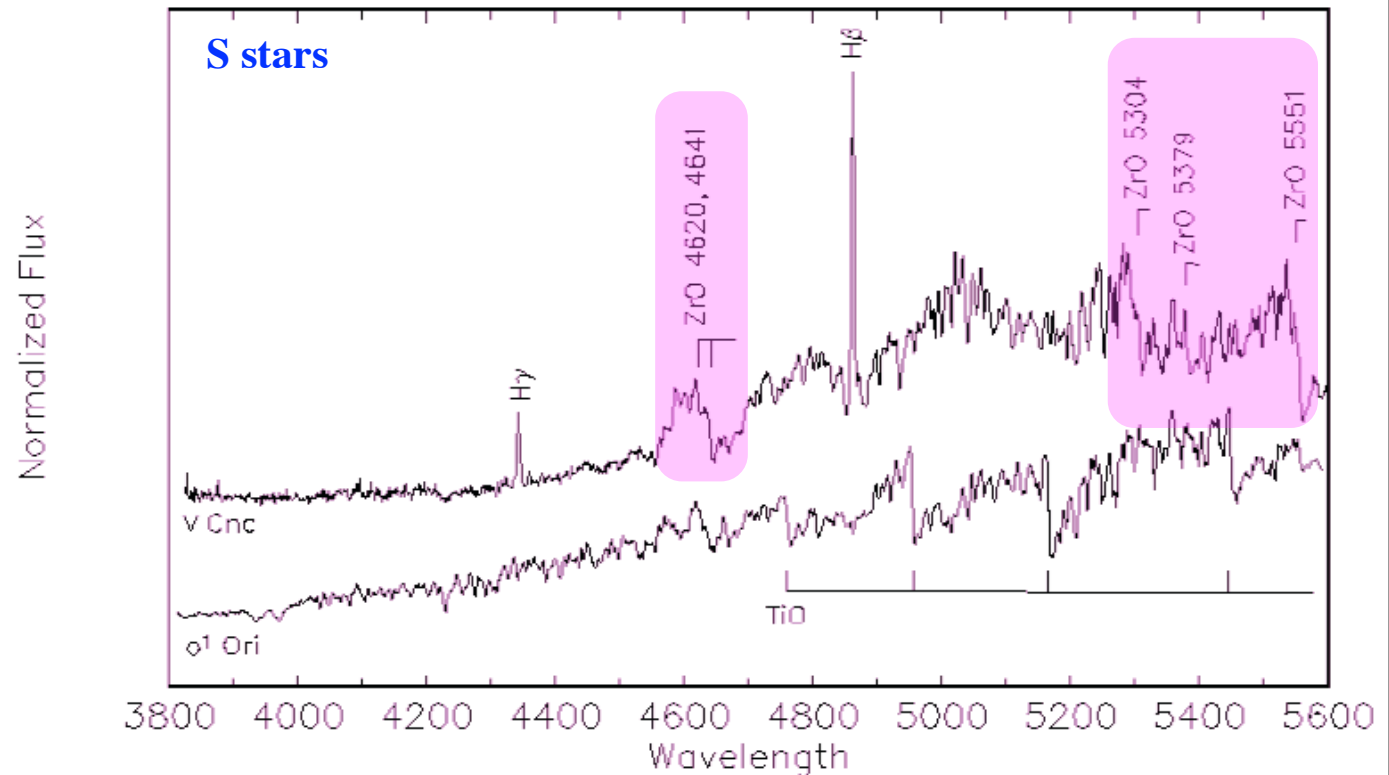
AGB

WD

Hence AGB stars become enriched in heavy elements, e.g. Zr

For instance, S stars = AGB stars

→ ZrO bands in S stars



Main sequence

RGB

Synthesis of He-burning nucleosynthesis products:
12C, 19F, s-process elements (Sr, Ba, Tc, Pb...)

AGB

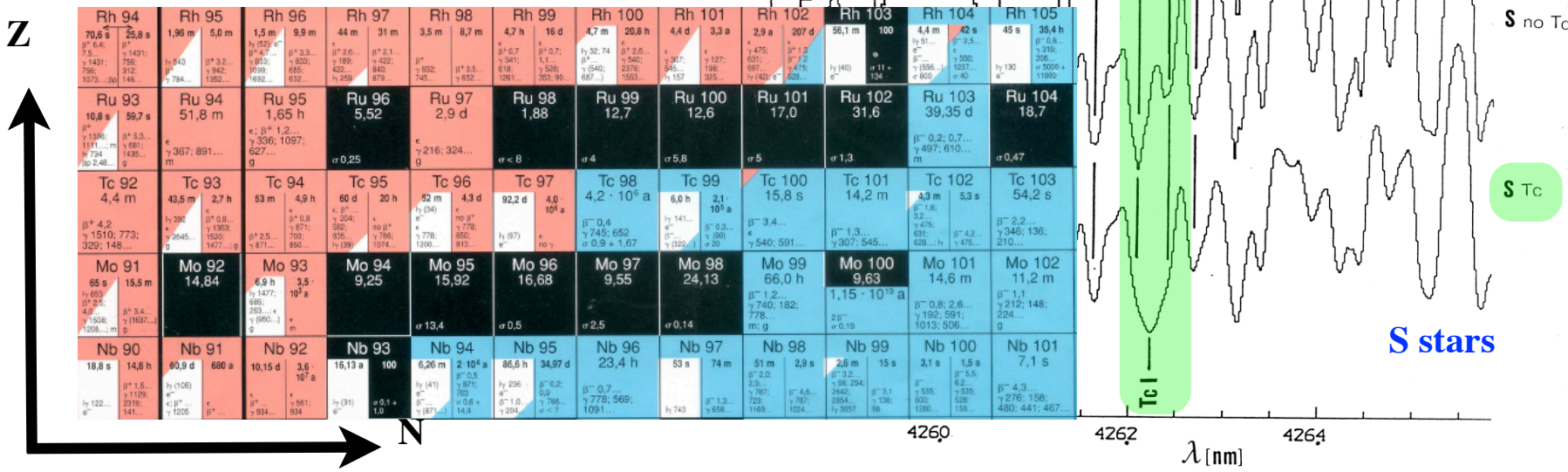
WD

Hence AGB stars become enriched in heavy elements, e.g. Zr

For instance, S stars = AGB stars

→ ZrO bands and Tc lines in S stars

Tc has no stable isotopes:
 ^{99}Tc ($\tau_{1/2,\beta} = 3 \cdot 10^5 \text{ yr}$)



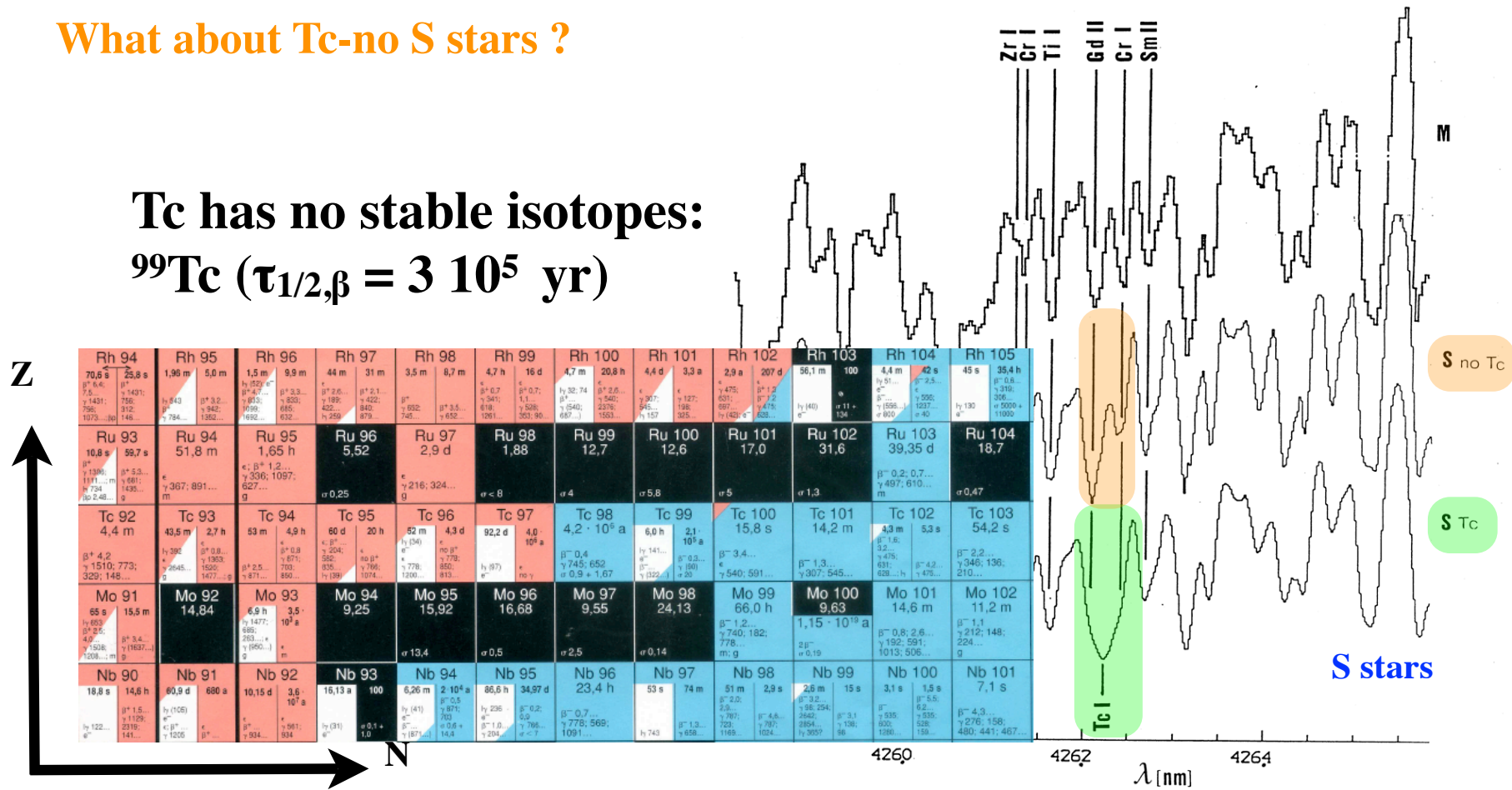
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For instance, S stars = AGB stars

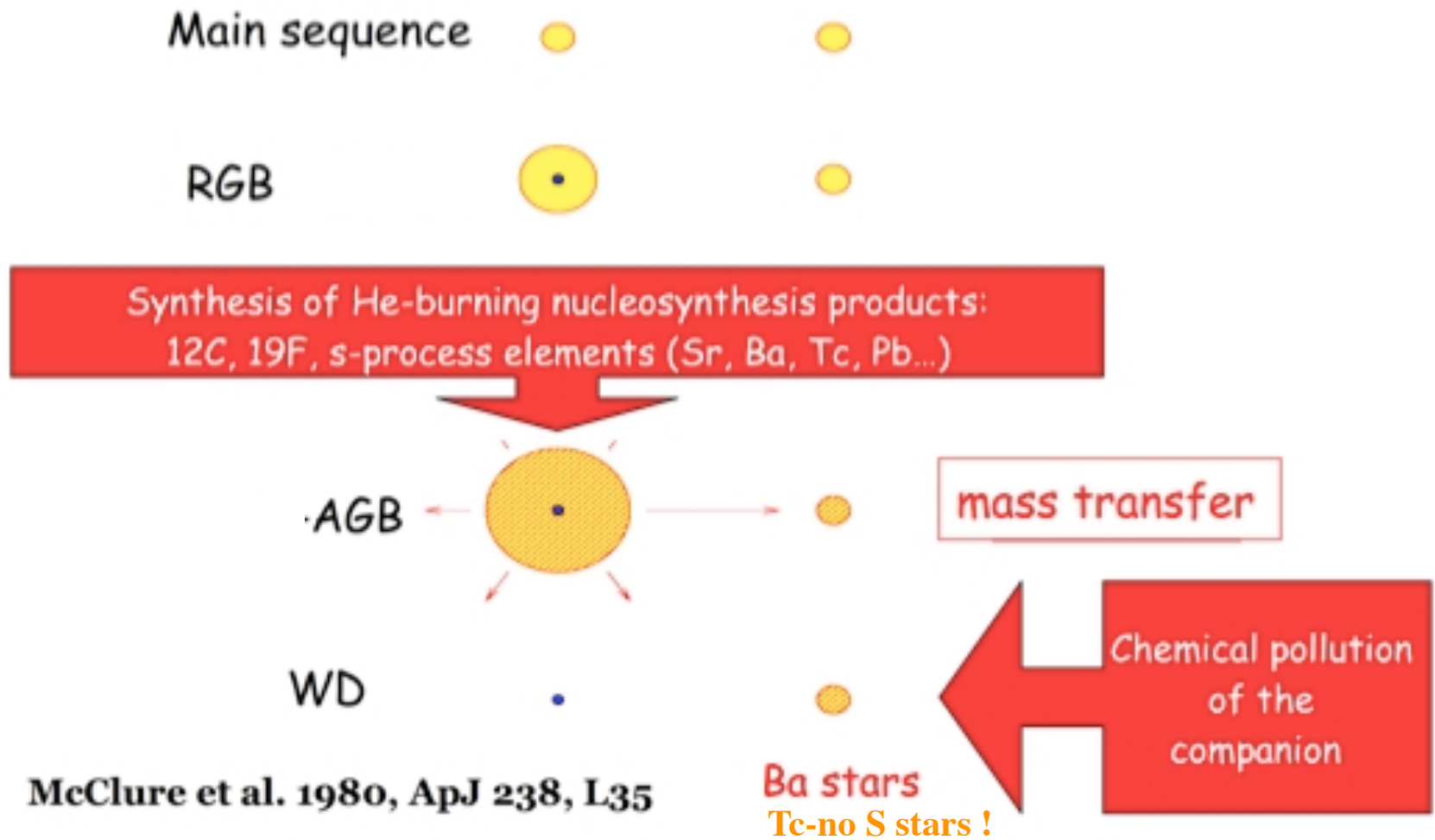
→ ZrO bands and Tc lines in S stars

What about Tc-no S stars ?

Tc has no stable isotopes:
 ^{99}Tc ($\tau_{1/2,\beta} = 3 \cdot 10^5 \text{ yr}$)



Tc-no S stars are all binaries!



McClure et al. 1980, ApJ 238, L35

The binary zoo

Classification of binary stars:

- i) Mass transfer
- ii) Observational properties
- iii) Evolutionary stage

A given binary has a location in each 3 classification schemes;
however, often its classification is only known in 1 or 2 schemes:

Knowing the location of a binary (family) in all 3 schemes often is the
goal of binary-star research !

Nice achievements in that respect have just been discussed :

Post-AGB stars (KULeuven !)

Barium and Tc-no S stars (ULB !)

Knowing the location of a binary (family) in all 3 schemes often is the goal of binary-star research !

Often a very difficult problem...

To help this process, a complex classification scheme merging schemes *i* (D/S/C) and *iii* (Evol.) has been proposed by P. Eggleton (Evolutionary Processes in Binary and Multiple Stars, Cambridge Univ. Press, 2001):

Knowing the location of a binary (family) in all 3 schemes often is the goal of binary-star research !

Table 3.5. Abbreviations for evolutionary states

Evolutionary state	Sub-type	
<i>P</i> pre-main-sequence	<i>TT</i>	T Tau
	<i>Be/Ae</i>	Herbig emission-line stars
	<i>BD</i>	Brown dwarf $\sim 0.01\text{--}0.08 M_{\odot}$
	<i>JMP</i>	Jupiter-mass planet $\lesssim 0.01 M_{\odot}$
<i>M</i> main sequence	<i>UMS</i>	Upper main sequence $\gtrsim 8 M_{\odot}$
	<i>IMS</i>	Intermediate main sequence $\sim 2\text{--}8 M_{\odot}$
	<i>LMS</i>	Lower main sequence $\sim 0.08\text{--}2 M_{\odot}$
	<i>HG</i>	He not yet ignited; star expanding on thermal timescale
<i>H</i> Hertzsprung gap	<i>CHeB</i>	Core He-burning
	<i>HB</i>	Horizontal branch
	<i>BL</i>	Blue loop
	<i>δC</i>	Cepheid
	<i>GKGC</i>	G/K-giant clump: core He-burning, shallow convective envelope
	<i>post-AGB</i>	post-asymptotic-giant-branch
	<i>FGB</i>	First giant branch: non-burning He core, deep convective envelope
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	<i>UHeMS</i>	Upper He main sequence ($M \gtrsim 1.4 M_{\odot}$)
<i>C</i> hot core	<i>SDB</i>	pre-He-WD
	<i>SDO</i>	pre-C/O-WD
<i>E</i> He-burning star	<i>PNN</i>	Planetary nebula nucleus
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<i>W</i> white dwarf	<i>HeWD</i>	He white dwarf
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To help this process, a complex classification scheme merging schemes ***i*** (D/S/C) and ***iii*** (Evol.) has been proposed by P. Eggleton (Evolutionary Processes in Binary and Multiple Stars, Cambridge Univ. Press, 2001):

Then, a given evolutionary path will be characterized by :

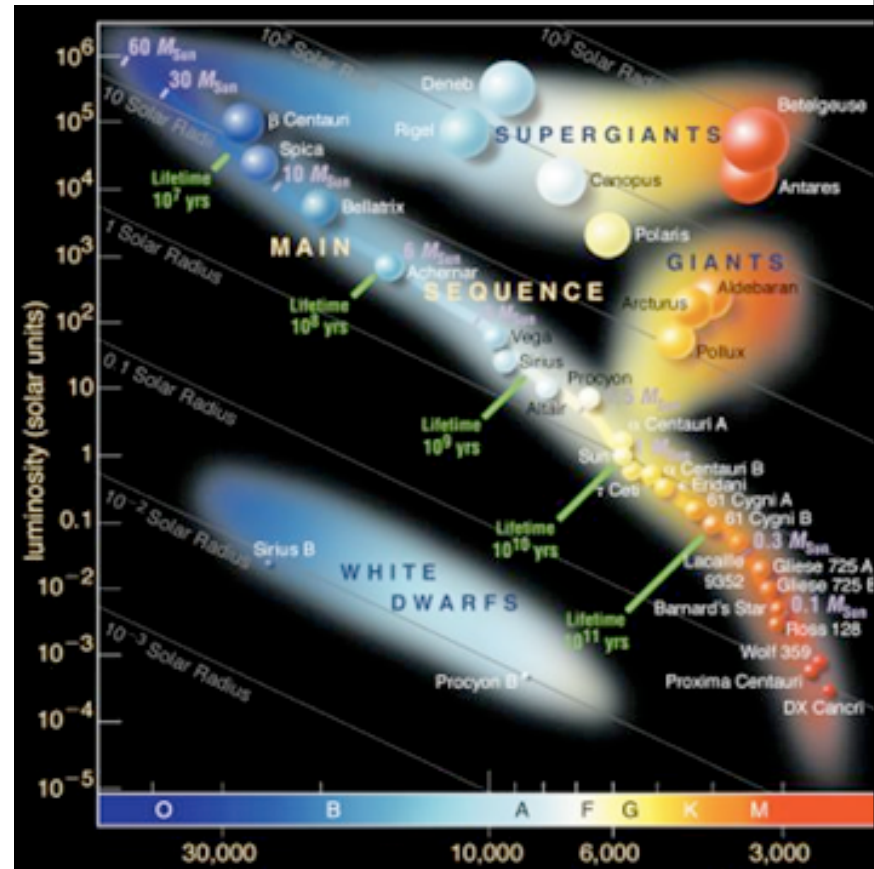
- a chain of evolutionary states

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Then, a given evolutionary path will be characterized by :

- a chain of evolutionary states

- a mass-transfer mode [\rightarrow Siess]
(simplest 'case A.', 'B.', 'C..')

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	<i>C</i> hot core	<i>SDB</i>
<i>SDO</i>		pre-C/O-WD
<i>PNN</i>		Planetary nebula nucleus
<i>E</i> He-burning star	<i>LHeMS</i>	Lower He main sequence ($M \lesssim 1.4 M_{\odot}$)
	<i>EHB</i>	Extreme horizontal branch
	<i>SDOB</i>	Sub-dwarf OB
	<i>SDB</i>	Possibly the same as <i>EHB</i> or <i>SDOB</i>
<i>W</i> white dwarf	<i>HeWD</i>	He white dwarf
	<i>COWD</i>	C/O white dwarf
	<i>NeWD</i>	Ne white dwarf
<i>N</i> neutron star	<i>NS</i>	normally-rotating neutron star
	<i>XRP</i>	X-Ray pulsar
	<i>MSP</i>	Millisecond pulsar; rapidly-rotating neutron star
<i>B</i> black hole	<i>BH</i>	Black hole

To help this process, a complex classification scheme merging schemes ***i*** (D/S/C) and ***iii*** (Evol.) has been proposed by P. Eggleton (Evolutionary Processes in Binary and Multiple Stars, Cambridge Univ. Press, 2001):

Then, a given evolutionary path will be characterized by :

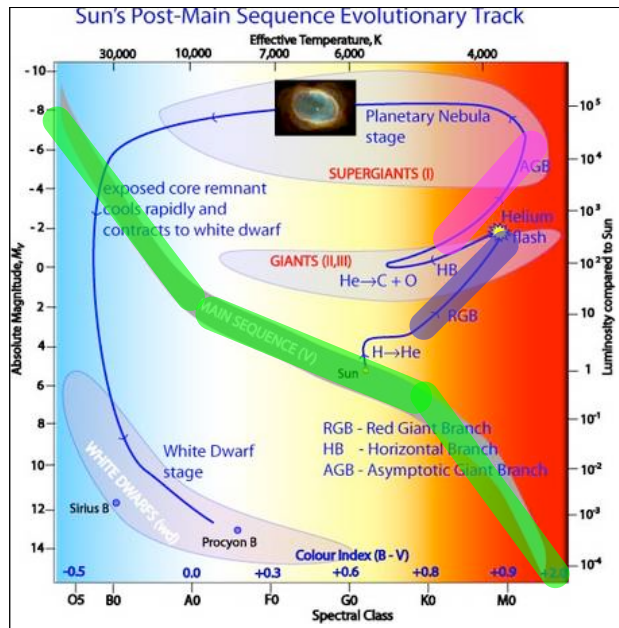
- a chain of evolutionary states

- a mass-transfer mode

(simplest 'case A.', 'B.', 'C..')

Example:

case AD = case A with Dynamic RLOF:
MMD \rightarrow MMS \rightarrow (M \rightarrow H \rightarrow G \rightarrow W)MC



**Mass-transfer modes :
cases A, B and C**

**case A = RLOF during
main sequence**

**case B = RLOF during
first giant branch**

**case C = RLOF during
asymptotic giant branch**

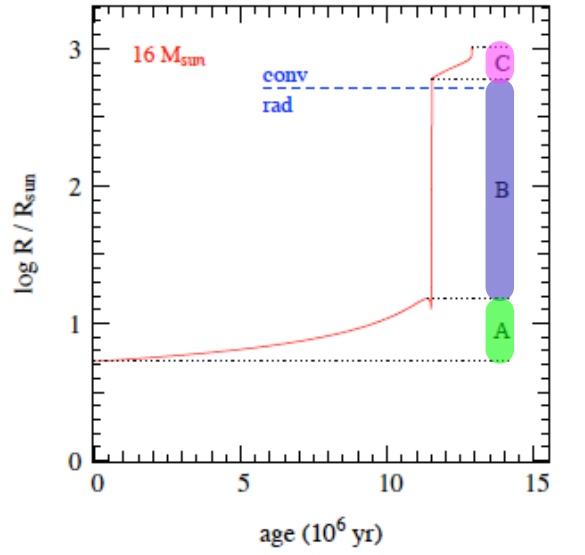
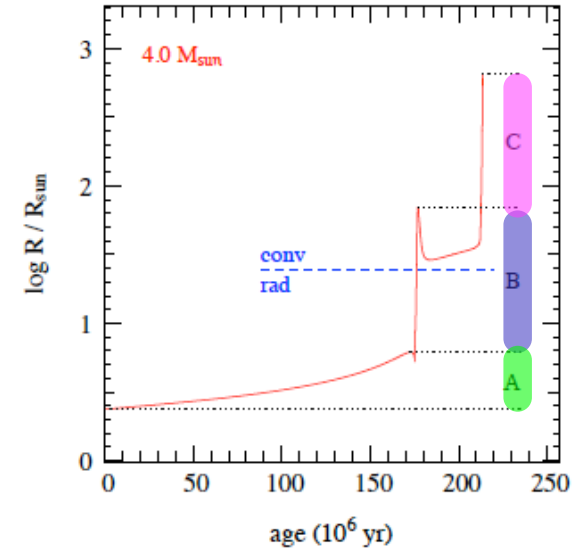
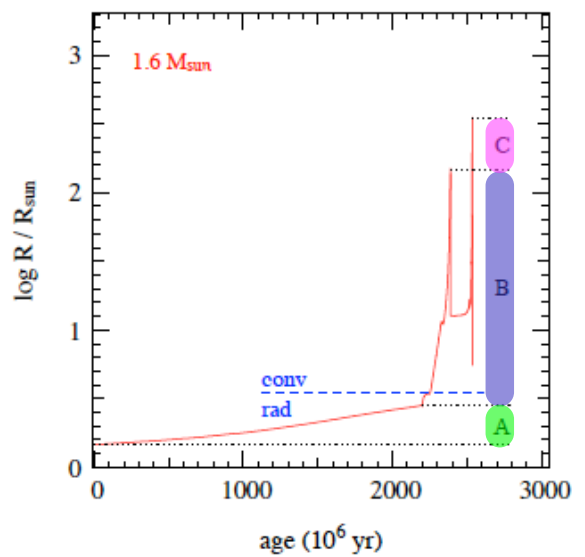
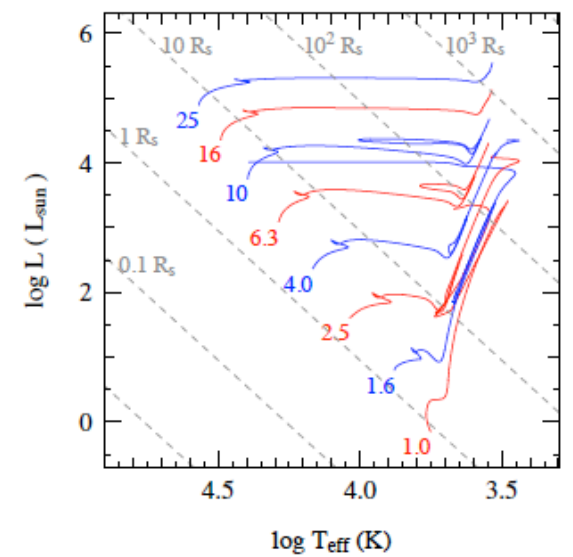


Figure 6.2. Evolution in the H-R diagram (panel a) of single stars with masses between 1.0 and $25 M_{\odot}$, as indicated, together with lines of constant radii (in solar radii, dashed lines). The other panels show the variation of the radii of stars of (b) $1.6 M_{\odot}$, (c) $4 M_{\odot}$ and (d) $16 M_{\odot}$ between the ZAMS and either the end of the AGB (1.6 and $4 M_{\odot}$) or carbon burning ($16 M_{\odot}$). The models have been calculated for a metallicity $Z = 0.02$ and a moderate amount of overshooting. The dotted lines indicate the radii at the ZAMS, the end of the MS, the ignition of He, and the maximum radius. The dashed blue line shows the radius at which the stars develop a deep convective envelope on the giant branch.

[From O. Pols]

Then, a given evolutionary path will be characterized by :

- a mass-transfer mode
simplest 'case A.', 'B.', 'C.'

Table 3.7. *Some major modes of evolution*

0 – NE – Nuclear evolution
1 – F1, R1 – RLOF: mass transfer, forward (F) or reverse (R), slow (Nuclear or MB) timescale; Section 3.3
2 – F2, R2 – RLOF: ditto, fast (thermal) timescale; Section 3.3

} cases A, B, or C

Then, a given evolutionary path will be characterized by :

- a mass-transfer mode

simplest 'case A..', 'B..', 'C..'

But the full picture is generally much more complex:

Table 3.7. *Some major modes of evolution*

0 – NE – Nuclear evolution
1 – F1, R1 – RLOF: mass transfer, forward (F) or reverse (R), slow (Nuclear or MB) timescale; Section 3.3
2 – F2, R2 – RLOF: ditto, fast (thermal) timescale; Section 3.3
3 – F3, R3 – RLOF: ditto, very fast (dynamical) timescale; Section 3.3
All six modes above apply to semidetached evolution (SF, SR) and also to evolution in contact (CF, CR).
The following modes are non-conservative: see later
4 – GR – gravitational radiation; Section 4.1
5 – TF – tidal friction; Section 4.2
6 – NW, PC, SW – normal (single-star) wind; Sections 2.4, 4.3: copious subtypes P Cyg, superwind
7 – MB – orbital angular momentum loss by stellar wind, magnetic braking and tidal friction; Section 4.5
8 – PA – partial accretion from stellar wind; Sections 4.3, 6.4
9 – EW – companion-enhanced stellar wind; Section 4.6
10 – BP – bi-polar re-emission; Section 4.7
11 – TB – influence of a third body; Section 4.8
12 – DI – tidal friction with Darwin instability; Section 5.1
13 – CE – common envelope evolution with spiral-in; Section 5.2
14 – EJ – rapid envelope ejection, common envelope without spiral-in; Section 5.2
15 – SN – supernova explosion; Section 5.3
16 – DE – dynamical encounters in dense clusters; Section 5.4
17 – IR – irradiation of the loser by accretion luminosity from the gainer; Section 6.2
We sometimes use 1, 2, 3 to qualify Modes GR–DE, indicating roughly the timescale, e.g. TF1, PC2, CE3.

} cases A, B, or C

18 - ID - Interaction with circumbinary disc

Eccentricity - period (e - P) diagrams may provide clues to identify mass-transfer/interaction processes

Then, a given evolutionary path will be characterized by :

- a mass-transfer mode

simplest 'case A.', 'B.', 'C.'

But the full picture is generally much more complex.

Eccentricity - period (e - P) diagrams may provide clues to identify mass-transfer / interaction processes

because they rule the evolution of orbital elements [→ Siess] :

Then, a given evolutionary path will be characterized by :

- a mass-transfer mode

simplest 'case A.', 'B.', 'C.'

But the full picture is generally much more complex.

Eccentricity - period (e - P) diagrams may provide clues to identify mass-transfer / interaction processes

because they rule the evolution of orbital elements [\rightarrow Siess]:

$$\dot{a} = f_a(a, e, M, \dot{M})$$

$$\dot{P} = f_P(a, e, M, \dot{M})$$

$$\dot{e} = f_e(a, e, M, \dot{M})$$

$$\dot{M} = f_M(a, e, M)$$

$$\frac{a^3}{P^2} = M = M_1 + M_2$$

Canonical binary evolution

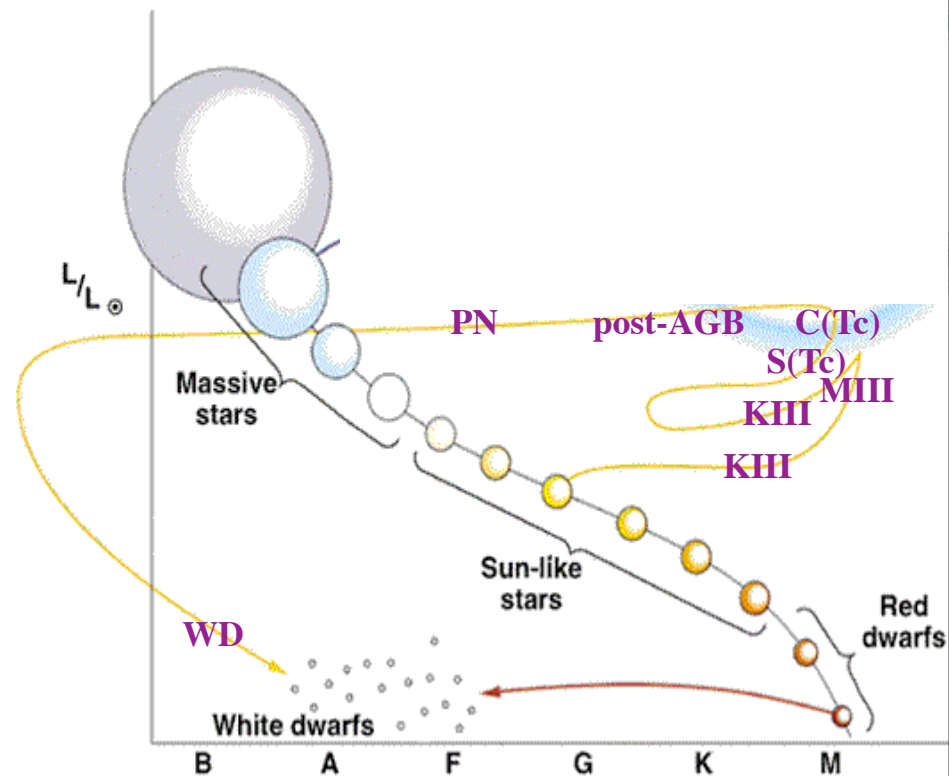
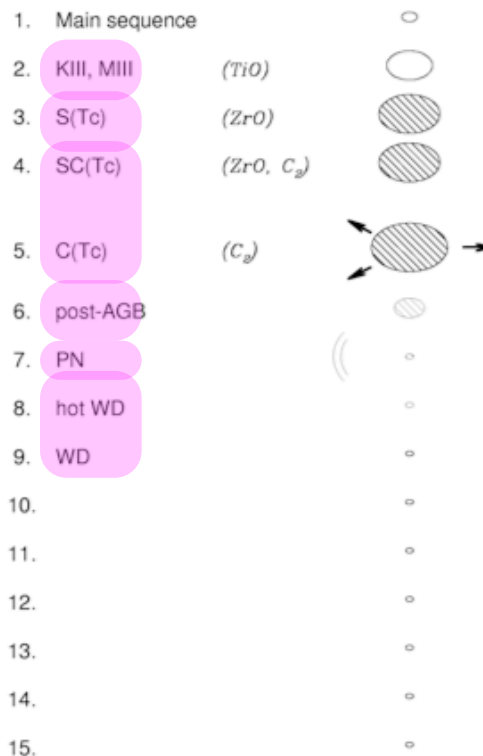
- Hurley, J. R., Tout, C. A., & Pols, O. R. 2002, MNRAS 329, 897

- P. Eggleton, Evolutionary Processes in Binary and Multiple Stars, Cambridge Univ. Press, 2001

Hence, from a_0 , P_0 , e_0 , M_0 , and these equations, it is possible to derive (e, P) for the current value of M.

Eccentricity - period ($e - P$) diagrams may provide clues to identify mass-transfer / interaction processes

For example:



Eccentricity - period (e - P) diagrams may provide clues to identify mass-transfer / interaction processes

For example:

1. Main sequence

2. KIII, MIII

(TiO)

3. S(Tc)

(ZrO)

4. SC(Tc)

(ZrO, C₂)

5. C(Tc)

(C₂)

6. post-AGB

7. PN

8. hot WD

9. WD

10.

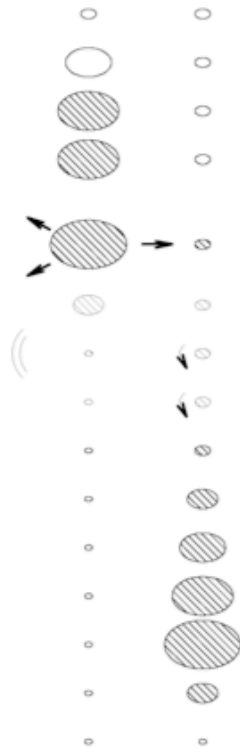
11.

12.

13.

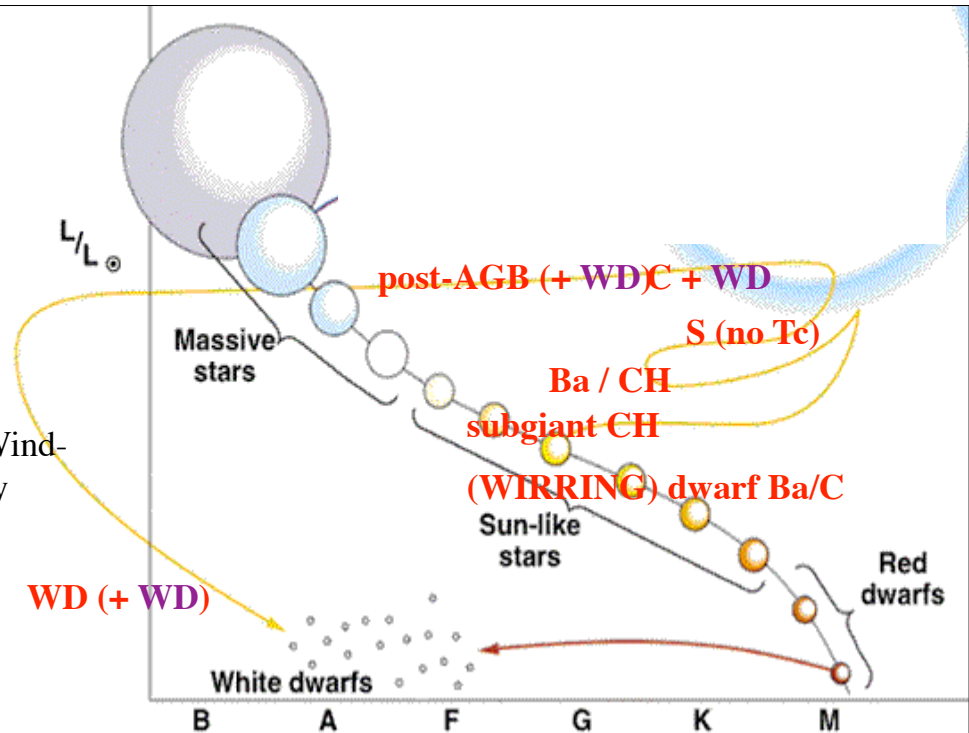
14.

15.

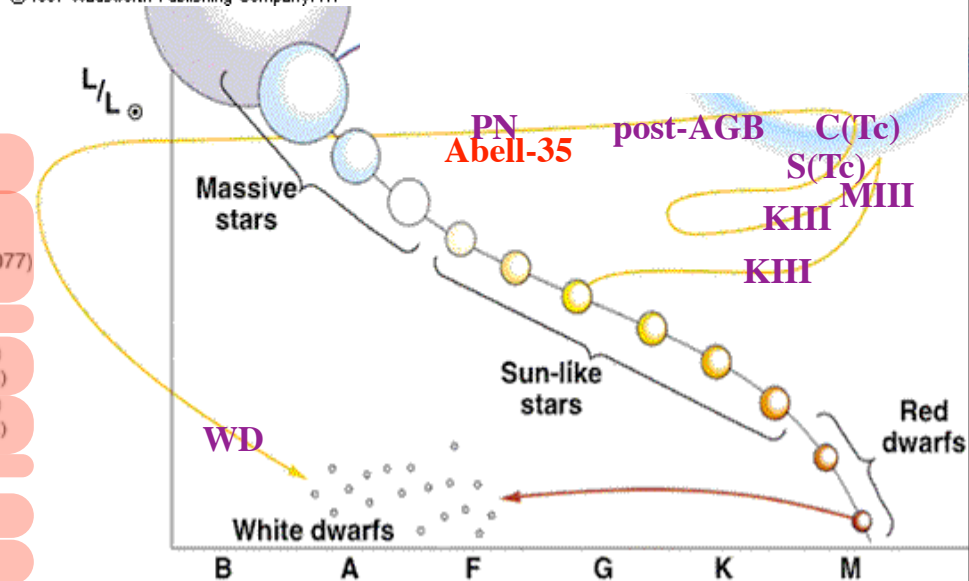


WIRING = 'Wind-Induced Rapidly RotatING'

- Abell 35-like
- WIRring (KVBa)
- dwarf Ba (F strong Sr4077)
C
- subgiant CH
- giant Ba (Pop.I)
CH (Pop.II)
- S or C (no Tc) (Pop.I)
yellow symbiotic (Pop.II)
- C (Tc) (+ WD)
- post-AGB (+ WD)
- wide WD pair



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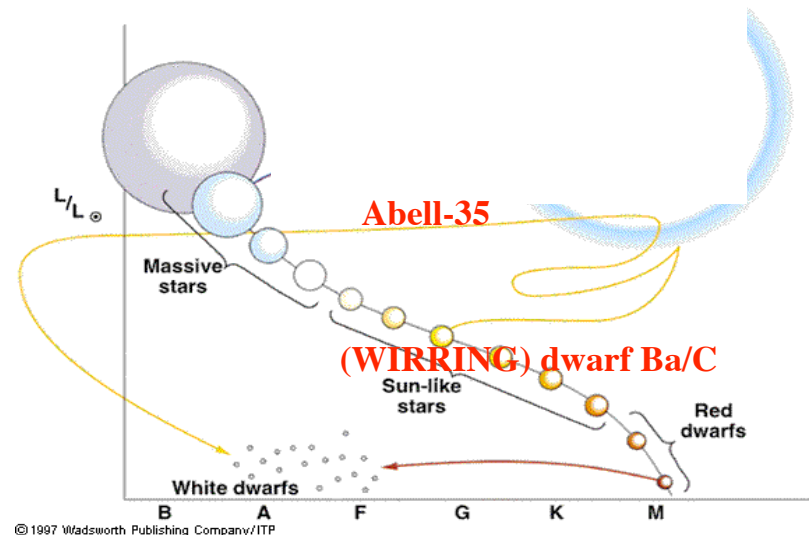
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I. About the possibility to accrete spin angular momentum in detached binaries

A hot debate...

From observations of **rapidly-rotating** post-mass-transfer stars (*in detached binaries?*): **YES**

WIRRING (KVBa) stars
Abell-35-like nuclei of PNs



About the possibility to accrete spin angular momentum in detached binaries:

A hot debate...

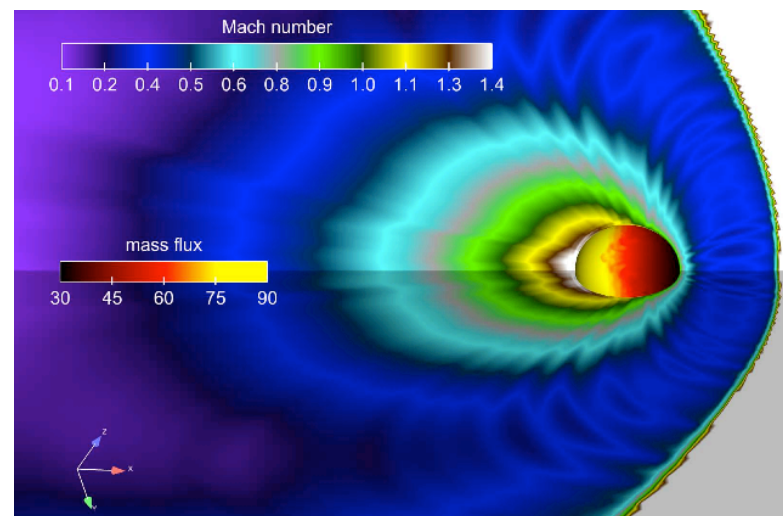
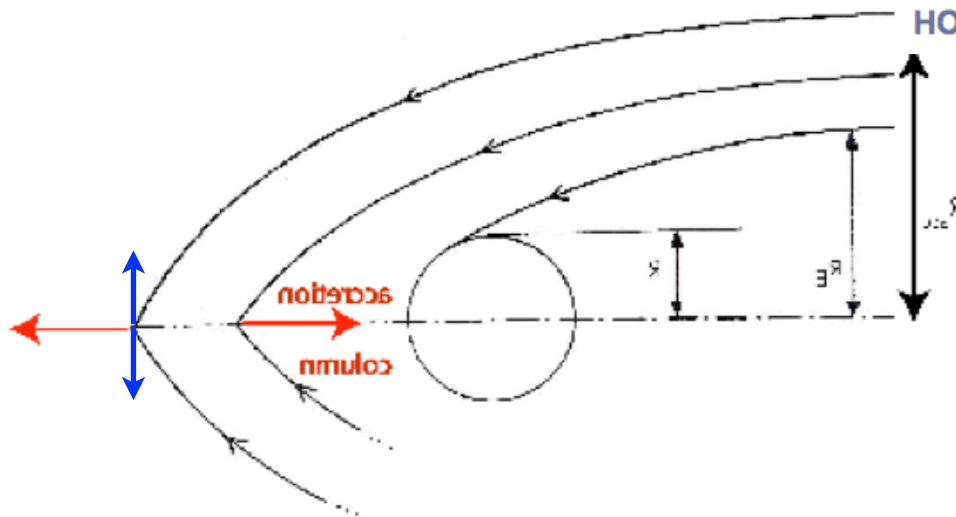
From **theory** of Hoyle-Lyttleton flows: **NO**

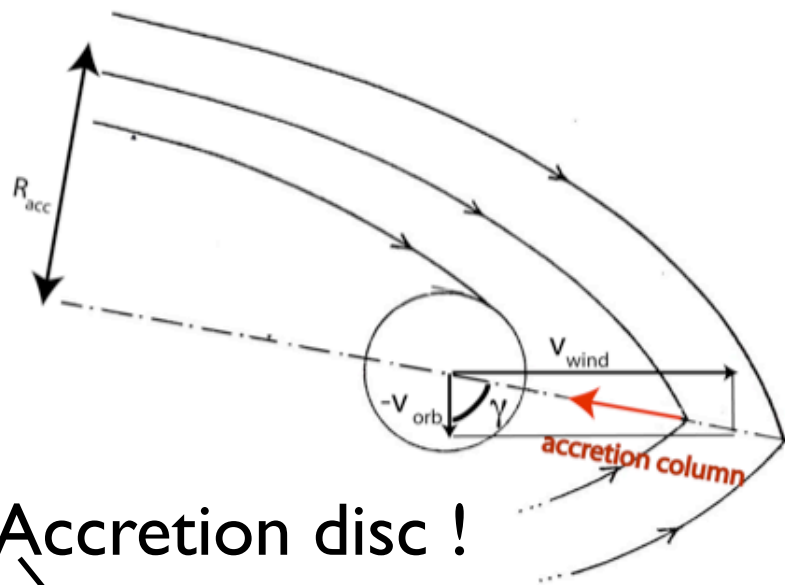
The flow is axisymmetric, which kills any transverse velocity component

The Astrophysical Journal > Volume 752 > Number 1

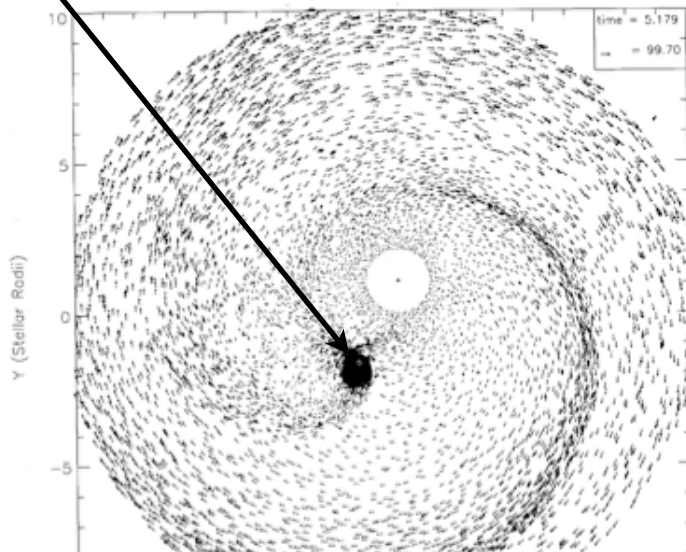
John M. Blondin and Eric Raymer 2012 *ApJ* 752 30 doi:10.1088/0004-637X/752/1/30

HOYLE-LYTTLETON ACCRETION IN THREE DIMENSIONS





Accretion disc !



- **Fast winds** (binaries with OB stars):

$$k \equiv v_{\text{orb}}/v_{\text{wind}} \ll 1$$

Accretion column, tilted by an angle $\gamma = \arctan v_{\text{wind}}/v_{\text{orb}}$ with respect to the orbital motion, with matter falling onto the compact star from its rear side (as viewed from the mass-losing star) with a rate \dot{M}_{B-H}

- **Slow winds** (detached binary systems involving an AGB star):

$$k \equiv v_{\text{orb}}/v_{\infty} \gg 1$$

Accretion column distorted by Coriolis effect, must be investigated numerically.

Accretion rates $\leq 0.1 \dot{M}_{B-H}$

Theuns & Jorissen 1993, MNRAS 265, 946

Mastrodemos & Morris 1998, ApJ 497, 303

Folini & Walder 2000, Ap&SS 274, 189

Nagae et al. 2004, A&A 419, 335

Jahanara et al., 2005, A&A 441, 589

Wind may be increased by tidal forces

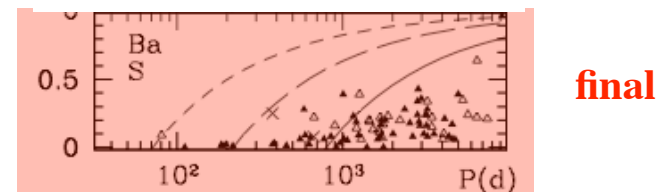
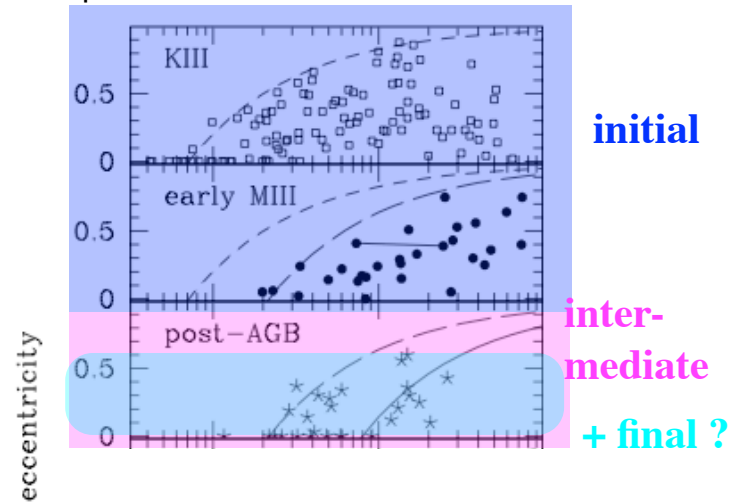
Tout & Eggleton 1988, MNRAS 231, 823

Frankowski & Tylenda 2001, A&A 367, 513

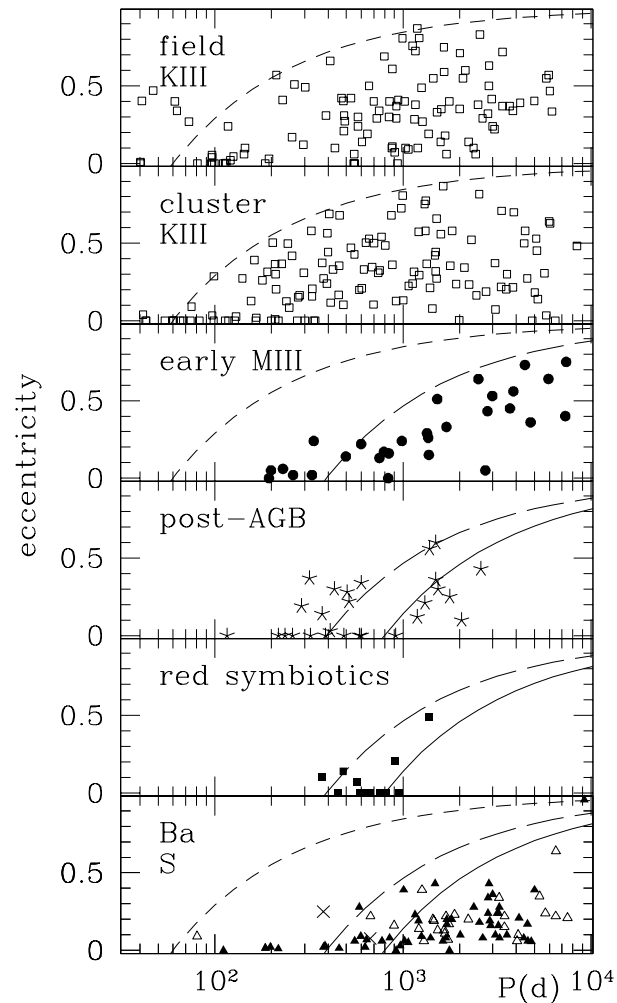
Eccentricity - period ($e - P$) diagrams may provide clues to identify mass-transfer / interaction processes

For example:

A compilation of ($e - \log P$) diagrams for several classes of pre- and post-mass-transfer binaries:
 Jorissen et al., 2009, A&A 498, 489



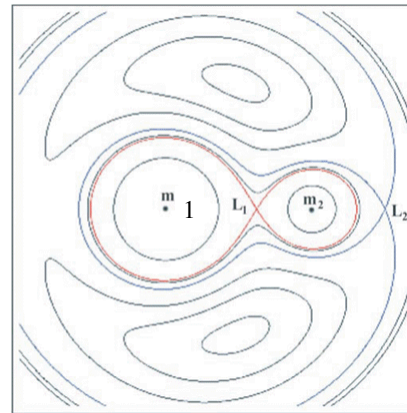
About the RLOF threshold in binaries



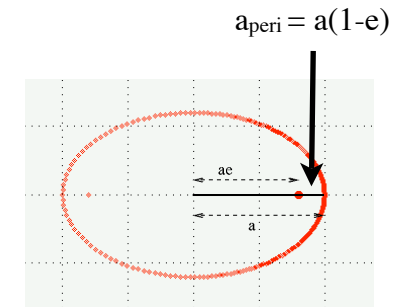
$$R_{R,2} = a (0.38 + 0.2 \log q) \quad \text{for } 0.5 \leq q = \frac{M_2}{M_1} \leq 20$$

$$r(M_1 \text{ to } L_1) = a (0.50 + 0.227 \log q)$$

$$r(M_2 \text{ to } L_1) = a (0.50 - 0.227 \log q)$$



$$r(M_1 \text{ to } L_1) = a_{\text{peri}} (0.50 + 0.227 \log q) \\ = a(1 - e) (0.50 + 0.227 \log q)$$



Fix the threshold by stating that $r(M_1 \text{ to } L_1) = R_*$:

$$R_* = a(1 - e) (0.50 + 0.227 \log q) \quad \text{where } a^3 = P^2 (M_1 + M_2)$$

$$\text{so } R_* = P^{2/3} (M_1 + M_2)^{1/3} (1 - e) (0.50 + 0.227 \log q)$$

About the “avoidance zone” in pre-mass-transfer, non-circularized binaries

**Binaries as
Tracers of
Stellar Formation**

or “*The e - log P conference*” !
Cambridge University Press, 1992

EDITED BY ANTOINE DUQUENNOY
and MICHEL MAYOR

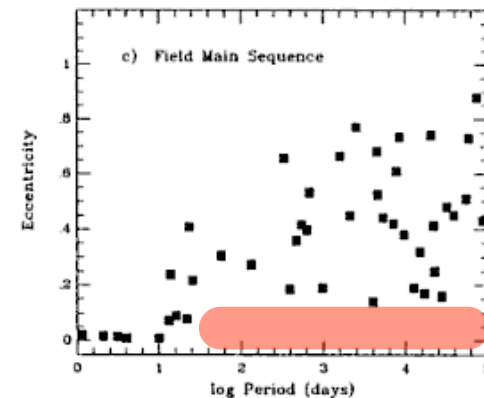
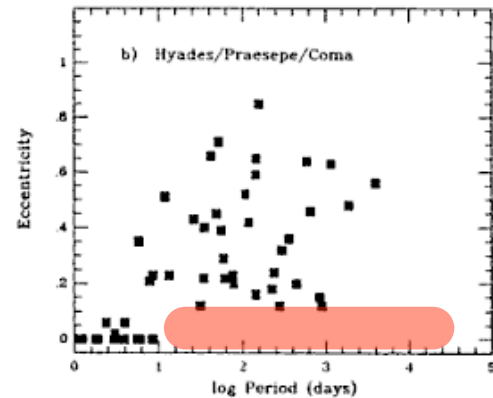
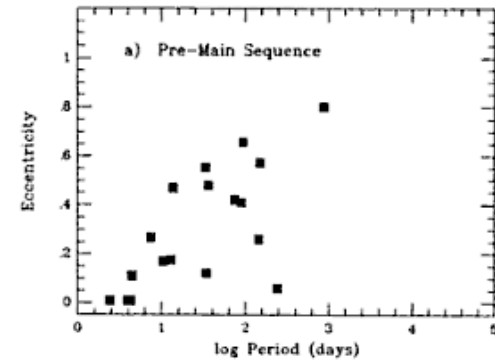


Figure 1. The period-eccentricity distribution for a) pre-main sequence binaries, b) main-sequence solar-mass binaries in the Hyades, Praesepe and Coma clusters [DMM92] and c) main-sequence solar-mass binaries in the field [DuM91].

About tidal circularization

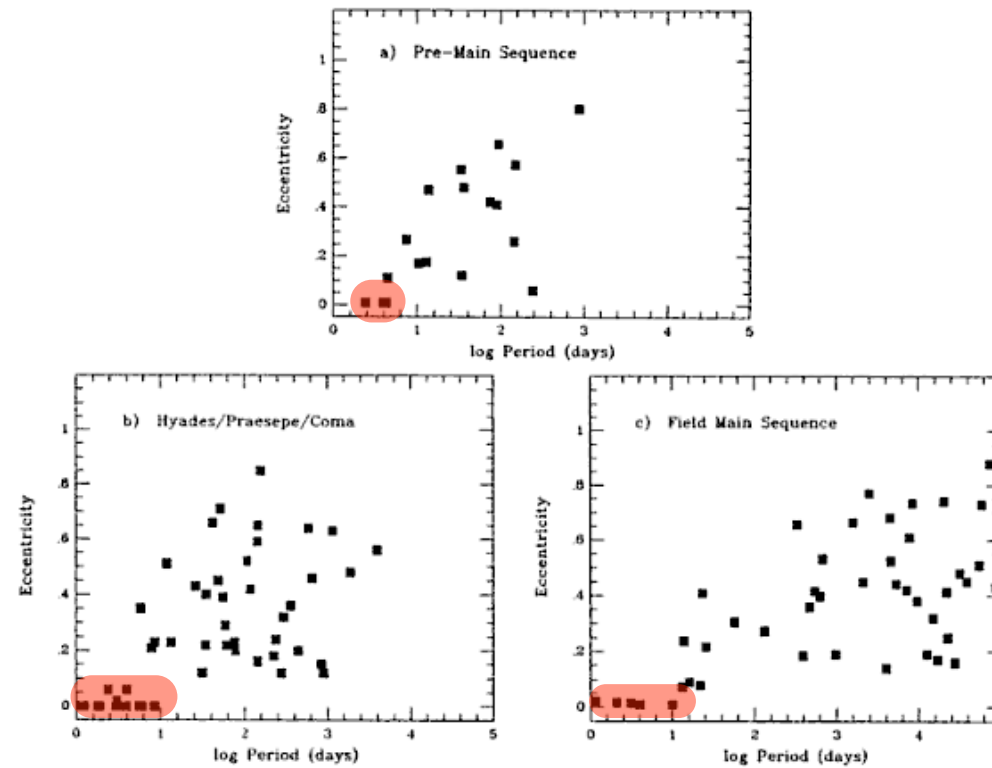
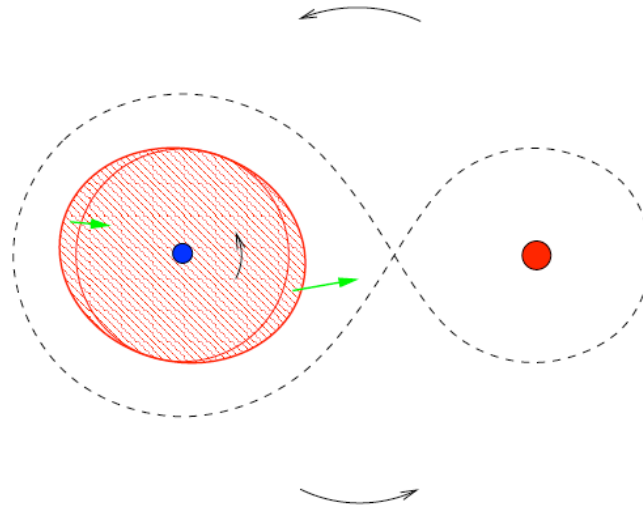


Figure 1. The period-eccentricity distribution for a) pre-main sequence binaries, b) main-sequence solar-mass binaries in the Hyades, Praesepe and Coma clusters [DMM92] and c) main-sequence solar-mass binaries in the field [DuM91].

Tidal interaction



- minimum energy at constant J_{tot} : $\Omega_{\text{spin}} = \Omega_{\text{orb}}$ and $e = 0$
- if $\Omega_{\text{spin}} \neq \Omega_{\text{orb}}$ or $e \neq 0$:
friction \rightarrow dissipation \rightarrow lag of tidal bulges \rightarrow torque
- timescale depends on dissipation mechanism
most efficient: **turbulent viscosity in convective envelope**

$$\frac{1}{\tau_{\text{circ}}} \propto \frac{f}{\tau_{\text{conv}}} \left(\frac{R}{a}\right)^8$$

$$\frac{1}{\tau_{\text{sync}}} \propto \frac{f}{\tau_{\text{conv}}} \left(\frac{R}{a}\right)^6 \quad \text{synchronization faster (since } R/a < 1)$$

- as star expands: $\Omega_{\text{spin}} < \Omega_{\text{orb}}$
tides transfer AM from orbit to star \rightarrow **separation reduced**
(and $e \rightarrow 0$)

Specific orbital energy $\varepsilon = \frac{E_{\text{tot}}}{\mu}$:

$$\varepsilon = \frac{v^2}{2} - \frac{\mu}{r} = -\frac{1}{2} \frac{\mu^2}{h^2} (1 - e^2) = -\frac{\mu}{2a}$$

h = specific angular momentum

= total relative angular momentum / reduced mass

$$\bar{h} = \bar{r} \times \bar{v} = \frac{\bar{J}_{\text{tot}}}{\mu} = \frac{\bar{J}_1 + \bar{J}_2}{\mu}$$

$$\begin{aligned} J &= \left(\frac{G M_1 M_2 a}{M_1 + M_2} \right)^{1/2} (1 - e^2)^{1/2} \\ &= \mu \left[G (M_1 + M_2) a (1 - e^2) \right]^{1/2} \\ &= \mu h \end{aligned}$$

$$h = \left[G (M_1 + M_2) a (1 - e^2) \right]^{1/2}$$

Hence, from

$$\varepsilon = -\frac{1}{2} \frac{\mu^2}{h^2} (1 - e^2),$$

minimum energy ε at constant angular momentum h

is reached when $e = 0$

Eccentricity - period (e - P) diagrams may provide clues to identify mass-transfer / interaction processes

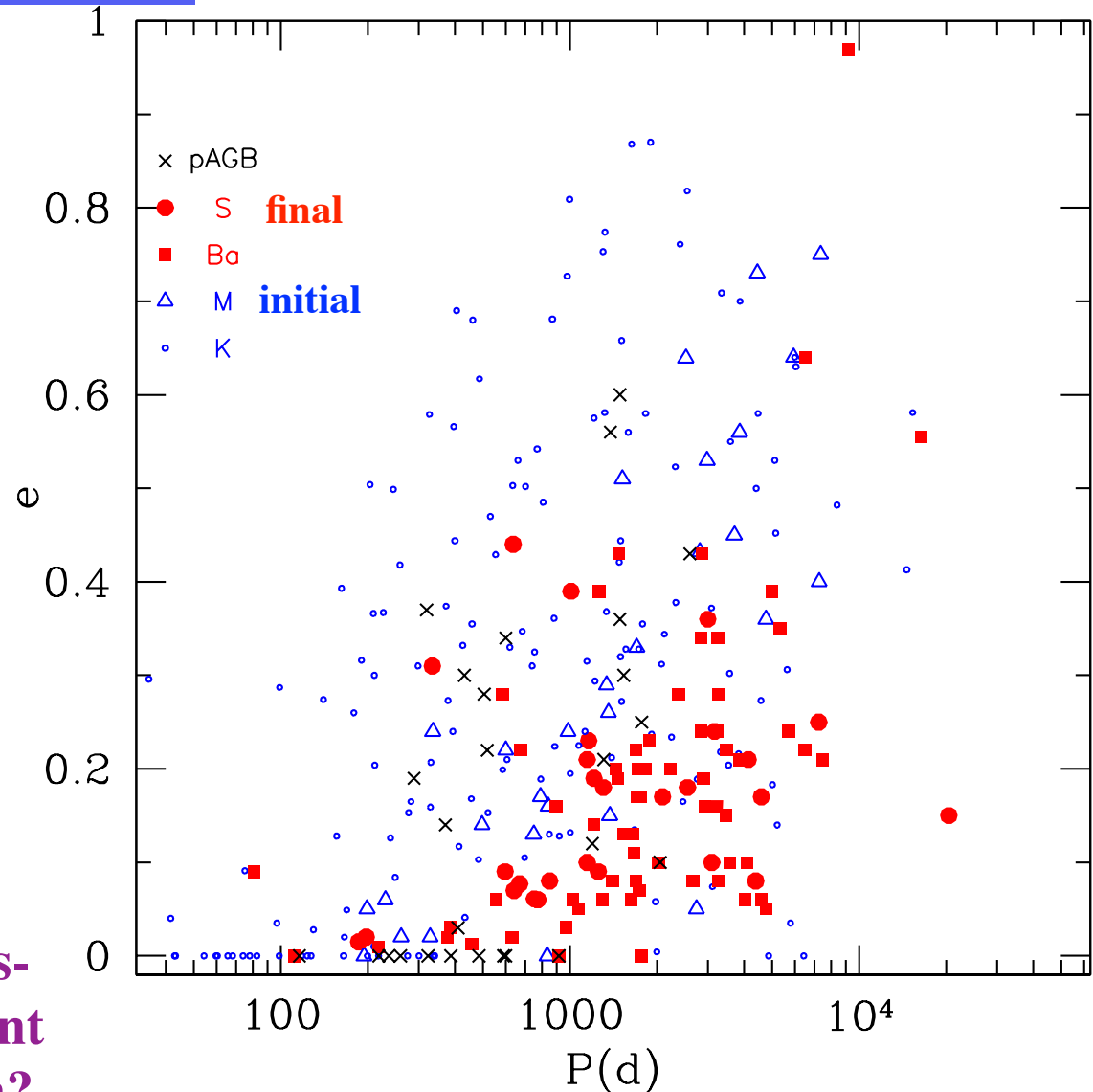
All in one :

From initial to final

- reduction in the average eccentricity

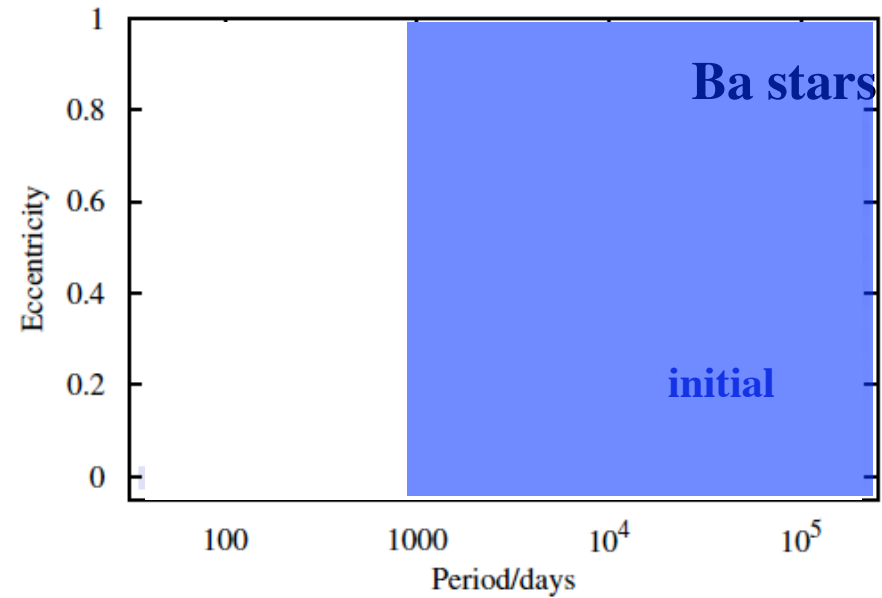
- increase of the period

Which interaction / mass-transfer processes account for this kind of evolution?



Canonical binary evolution

Hurley, J. R., Tout, C. A., & Pols, O. R. 2002,
MNRAS, 329, 897



Which interaction / mass-transfer processes account for this kind of evolution?

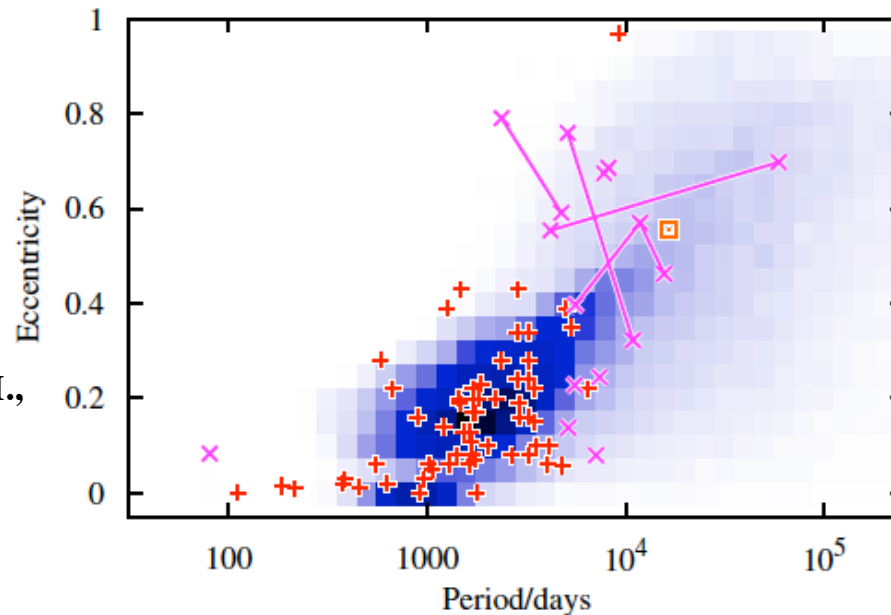
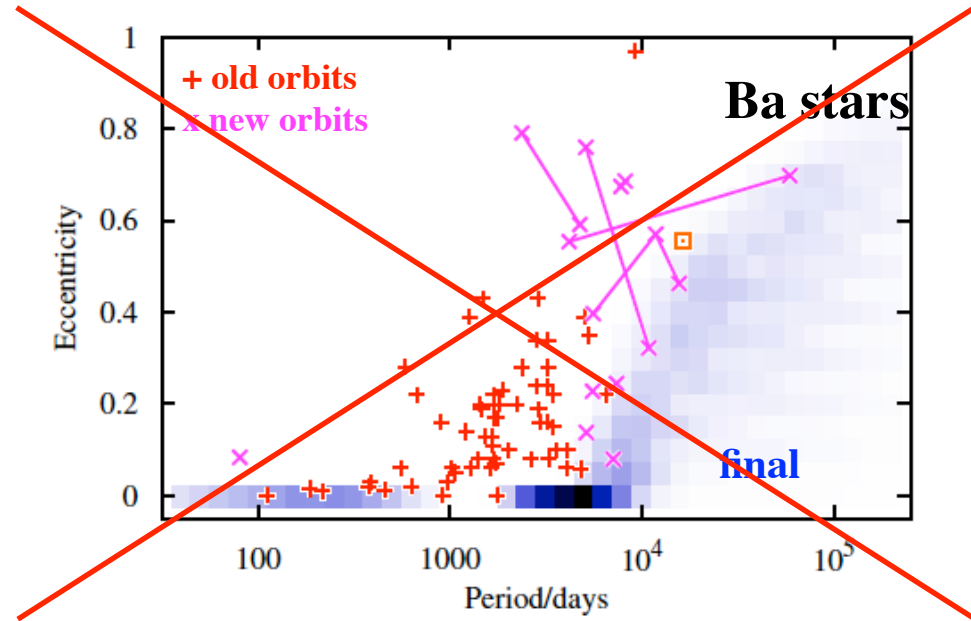
Canonical binary evolution

Hurley, J. R., Tout, C. A., & Pols, O. R. 2002,
MNRAS, 329, 897

+ WD kick,
disc-orbit interaction,
angular-momentum loss...

Izzard R., Dermine T., Church R.P.
2010, A&A 523, A10
Dermine T., Izzard R., Jorissen A., Van Winckel H.,
2012, ArXiv:1203.6471

**Which interaction / mass-
transfer processes account
for this kind of evolution?**

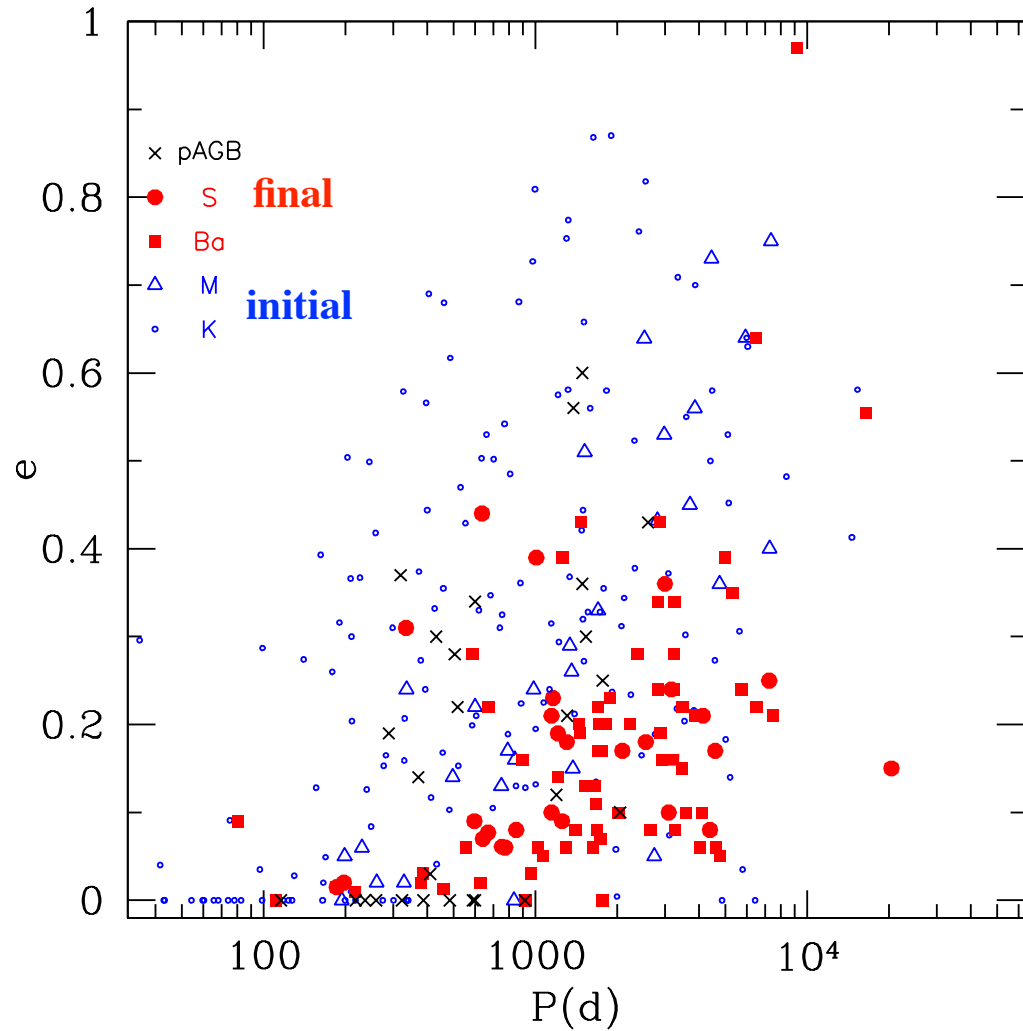


A significant difference between
initial and **final** samples : the (e, P) diagram

From **initial** to **final**

- reduction in the
average eccentricity

- increase of the period



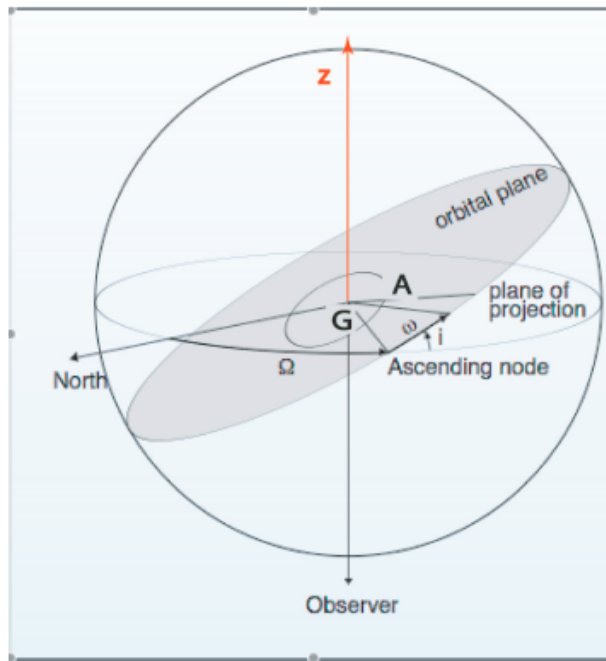
→ Eccentricity - period (e - P) diagrams provide clues to identify
mass-transfer / interaction processes at work during binary evolution

Another significant difference between **initial** and **final** samples : the mass functions

Mass functions for SB1:

[→ MazeH]

$$f(M) = \frac{(M_{\text{comp}} \sin i)^3}{(M_{\text{primary}} + M_{\text{comp}})^2}$$



Under the assumption that **the orbits are oriented at random in space**, the inclination angle i distributes as $\sin i$:

$$\text{Prob}(i) di = \sin i di$$

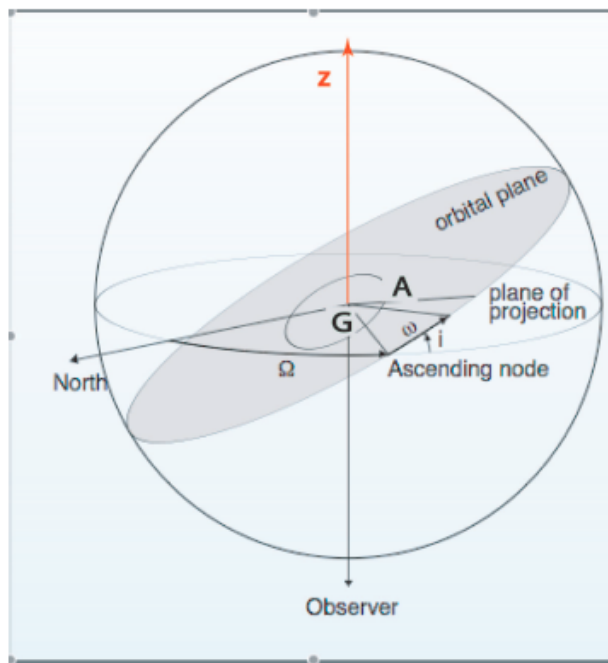
Hence, for a large sample of stars, **the distribution of $f(M)$ reflects the distributions of M_{primary} and $M_{\text{companion}}$**

Another significant difference between
initial and **final** samples : the mass functions

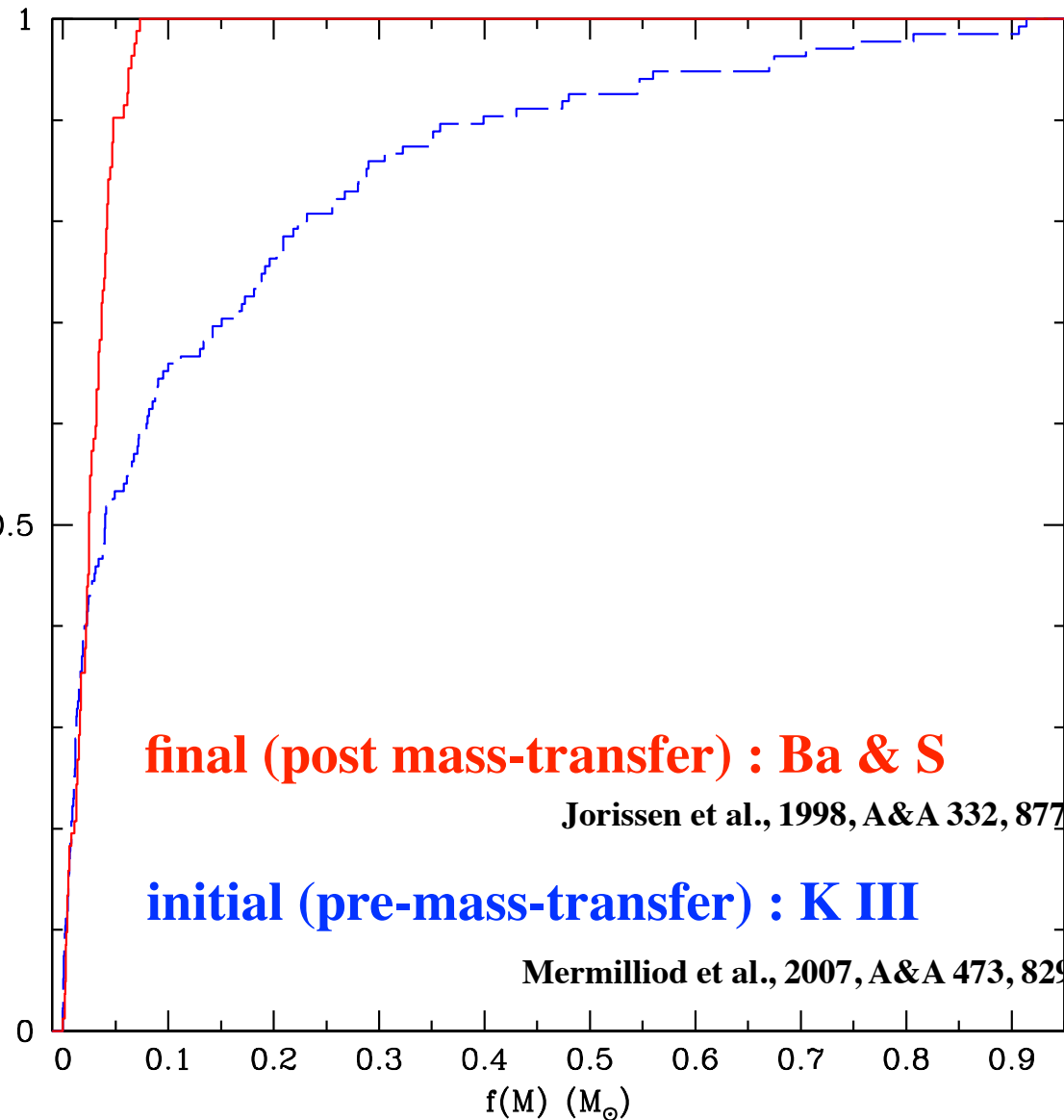
Mass functions for SB1:

[→ Mazeh]

$$f(M) = \frac{(M_{\text{comp}} \sin i)^3}{(M_{\text{primary}} + M_{\text{comp}})^2}$$



Cumulative frequency distribution



Another significant difference between
initial and **final** samples : the mass functions

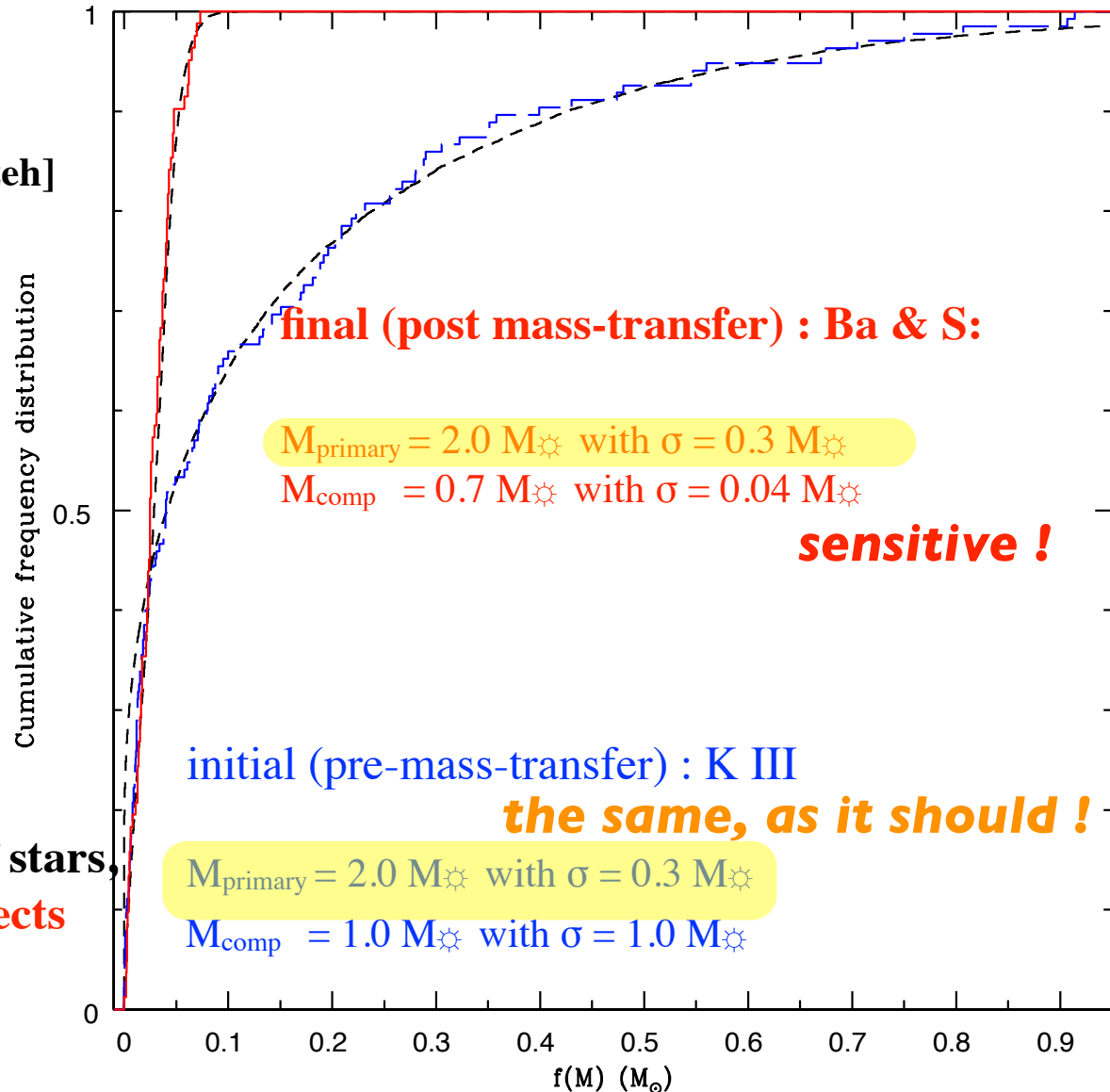
Mass functions for SB1:

[→ MazeH]

$$f(M) = \frac{(M_{\text{comp}} \sin i)^3}{(M_{\text{primary}} + M_{\text{comp}})^2}$$

Prob(*i*) di = sin *i* di

Hence, for a large sample of stars,
**the distribution of *f*(*M*) reflects
the distributions
of *M*_{primary} and *M*_{companion}**



final (post mass-transfer) : Ba & S:

*M*_{primary} = 2.0 *M*_☉ with σ = 0.3 *M*_☉
*M*_{comp} = 0.7 *M*_☉ with σ = 0.04 *M*_☉

sensitive !

initial (pre-mass-transfer) : K III

the same, as it should !

*M*_{primary} = 2.0 *M*_☉ with σ = 0.3 *M*_☉
*M*_{comp} = 1.0 *M*_☉ with σ = 1.0 *M*_☉

Another significant difference between
initial and **final** samples : the mass functions

Mass functions for SB1:

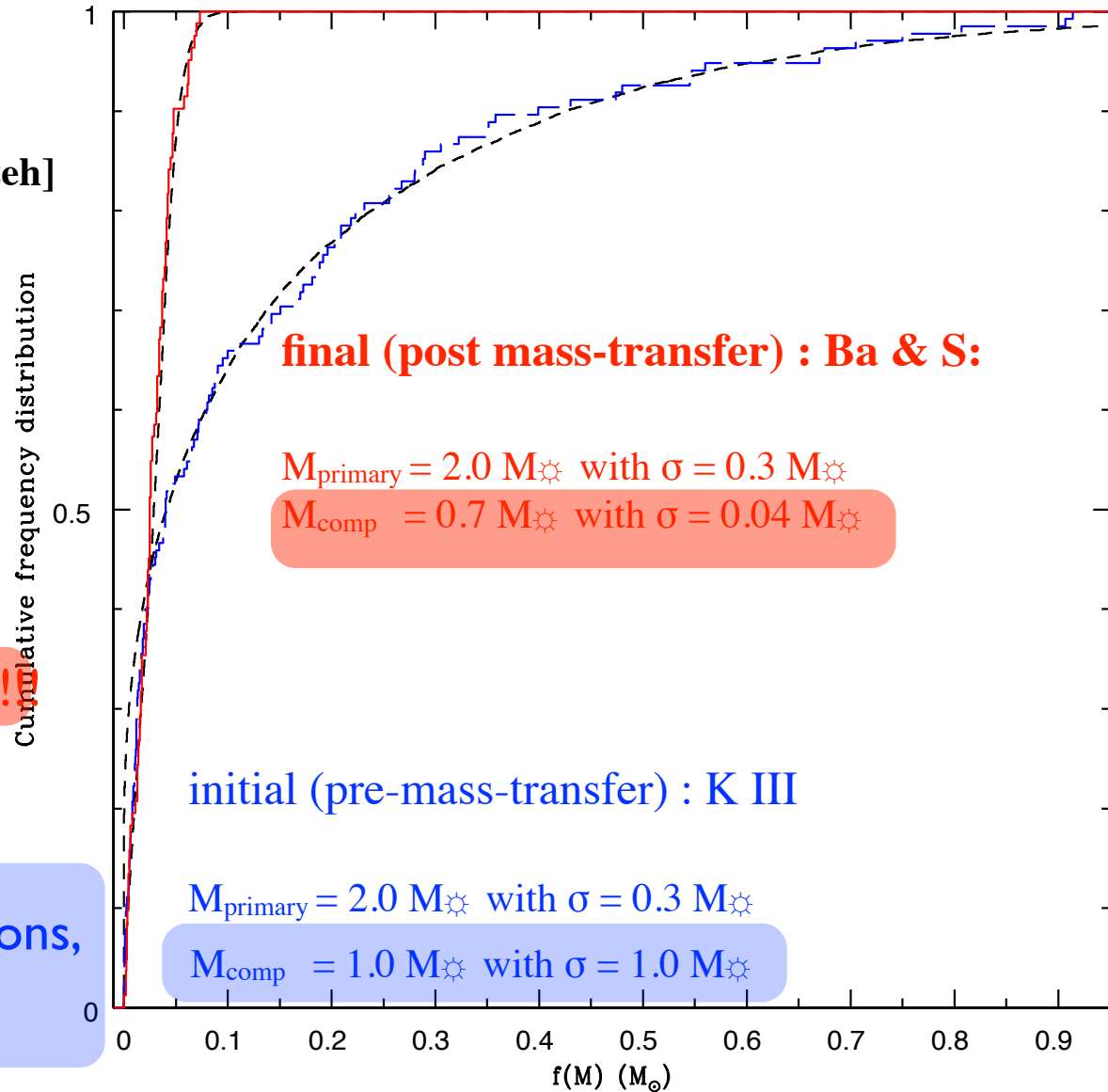
[→ MazeH]

$$f(M) = \frac{(M_{\text{comp}} \sin i)^3}{(M_{\text{primary}} + M_{\text{comp}})^2}$$

Prob(*i*) di = sin *i* di

white dwarf companions !

no constraint on companions,
 except $M_{\text{comp}} \leq M_{\text{primary}}$!!!



Evolutionary sequence involving KIII and Ba, S no-Tc binaries

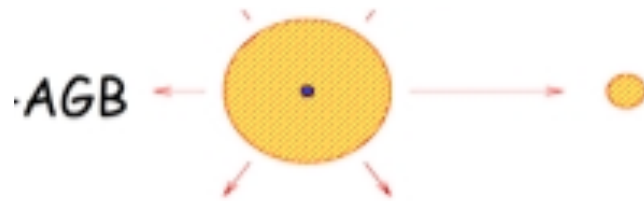
Main sequence



RGB: **KIII**



no constraint on companions,
except $M_{\text{comp}} \leq M_{\text{primary}}$!!!



mass transfer

WD



white dwarf companions
mandatory !!!

Ba stars

Tc-no S stars

Evolutionary sequence involving KIII and Ba, S no-Tc binaries

Main sequence

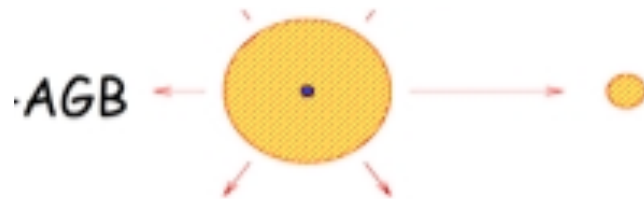


RGB: **KIII**



no constraint on companions,
except $M_{\text{comp}} \leq M_{\text{primary}} !!!$

(because the more massive
component evolves faster)



mass transfer

WD



white dwarf companions
mandatory !!!

Ba stars

Tc-no S stars

Evolutionary sequence involving KIII and Ba, S no-Tc binaries

Main sequence



RGB : KIII



no constraint on companions,
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(because the more massive
component evolves faster)

less massive

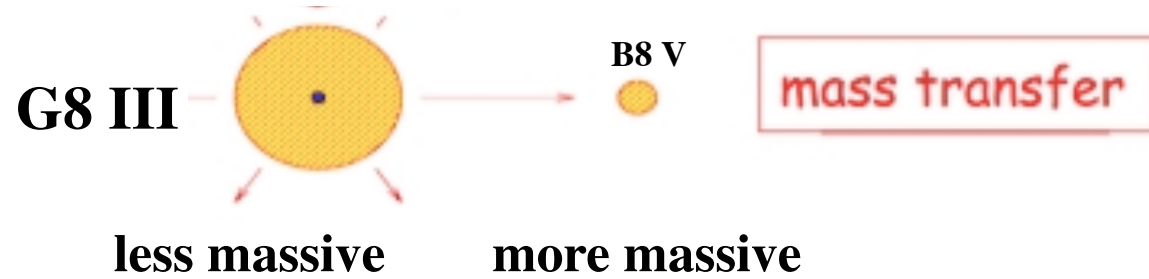
more massive



One exception:

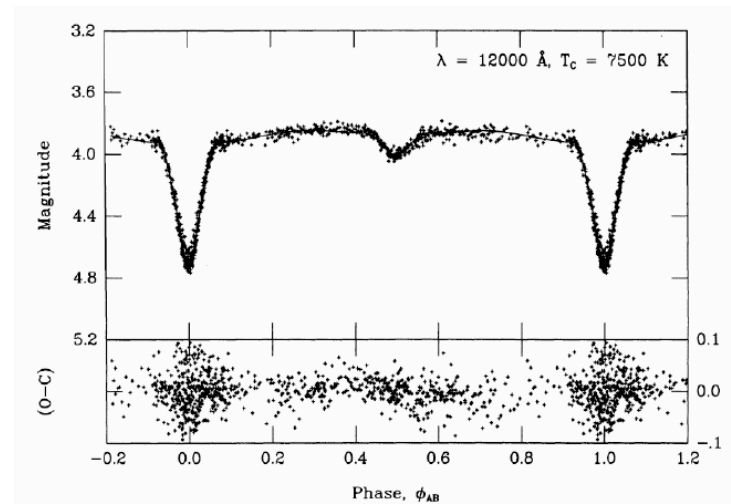
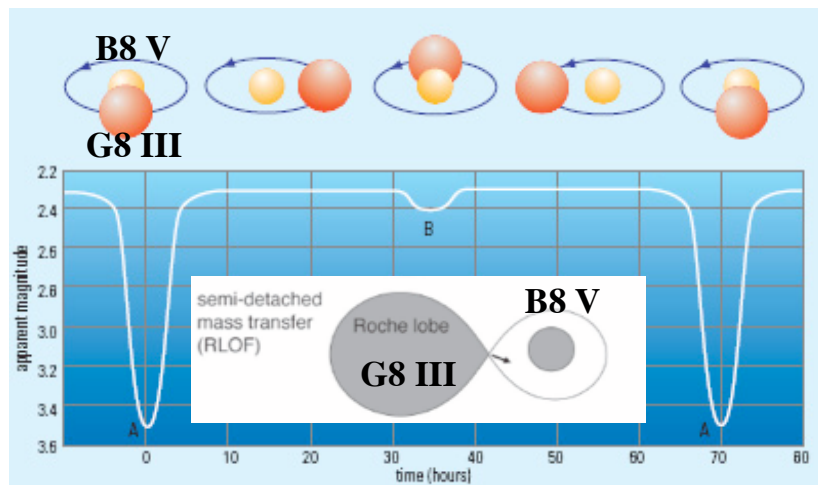
the **Algol paradox** : on-going mass transfer...

The Algol paradox : on-going mass transfer...

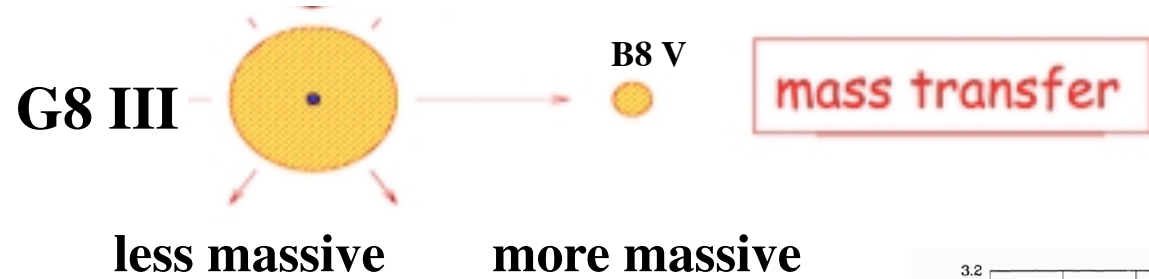


The defining properties of Algols are

- initially empirical: eclipsing lightcurve

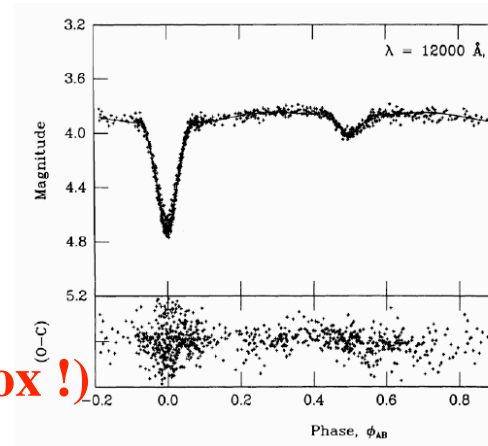


The Algol paradox : on-going mass transfer...



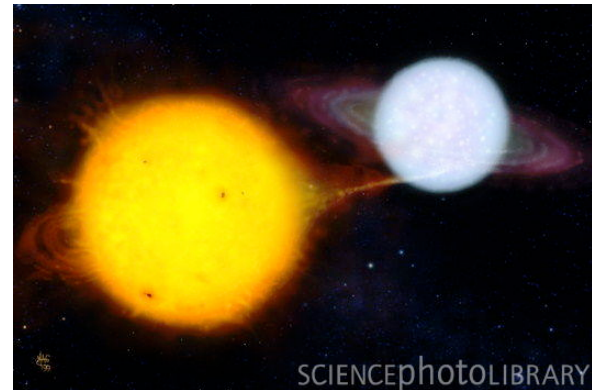
The defining properties of Algols are

- initially empirical: eclipsing lightcurve
- then theory/evolution : giant is the less massive (paradox !)



name	spectra	P (d)	M_1	M_2	R_1	R_2	$\log L_1$	$\log L_2$
β Per (Algol)	G8III + B8V	2.87	0.8	3.7	3.5	2.9	0.65	2.27

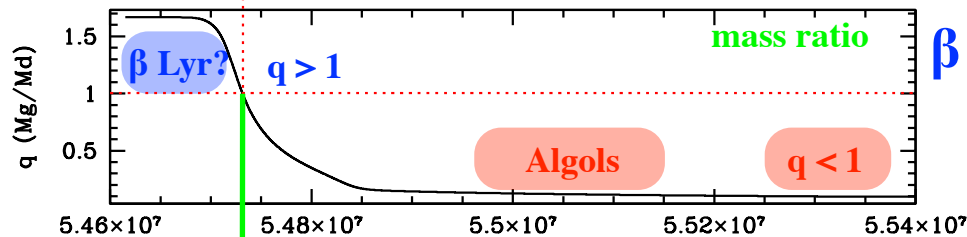
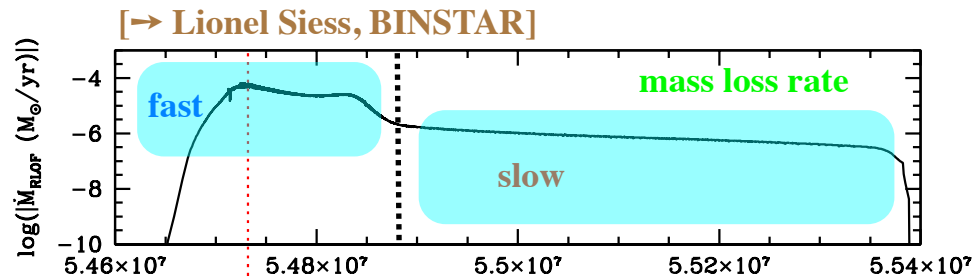
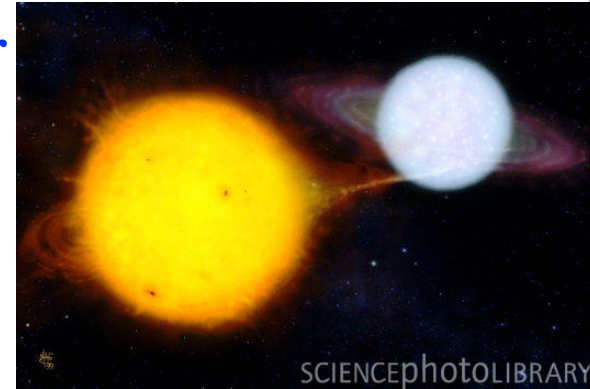
- finally theory/binary : on-going, slow mass transfer (case A, slow - nuclear - time scale)



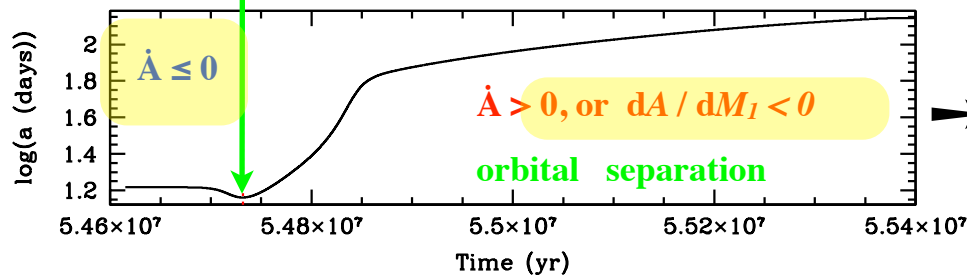
The Algol paradox : on-going mass transfer...

The defining properties of Algols are

- finally theory/binary : on-going, slow mass transfer (case A, nuclear time scale)



β Lyr : on-going, fast mass transfer precursors of Algols ?

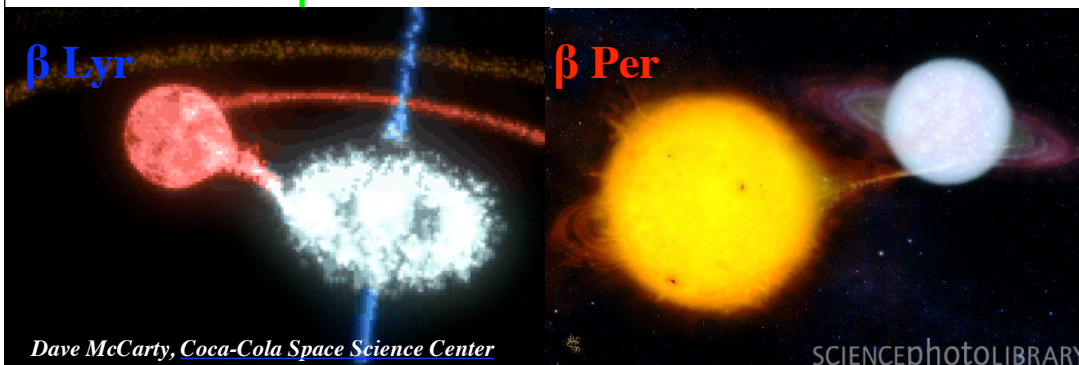
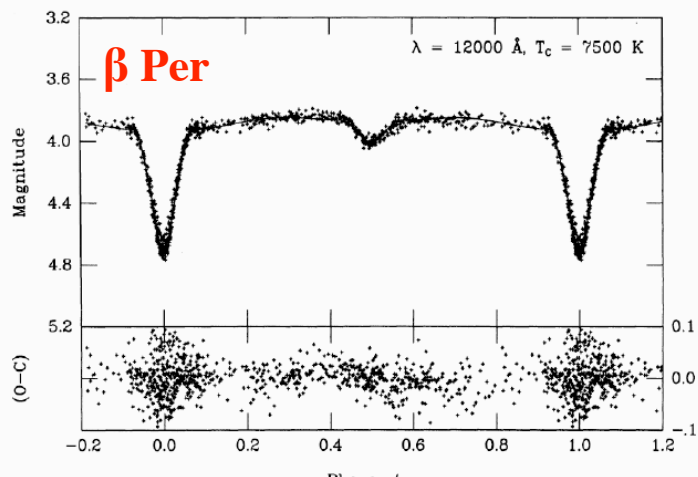
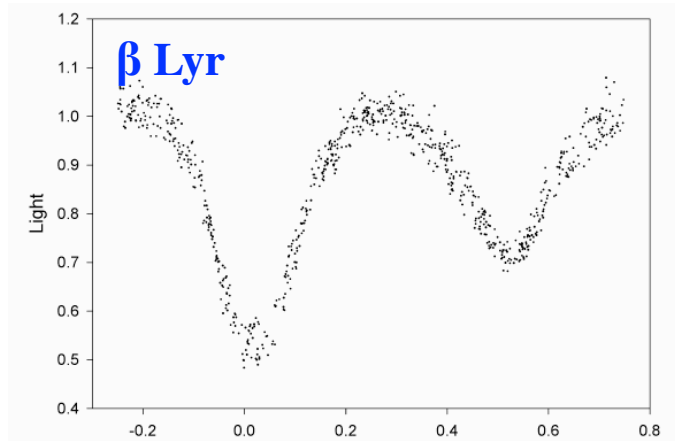
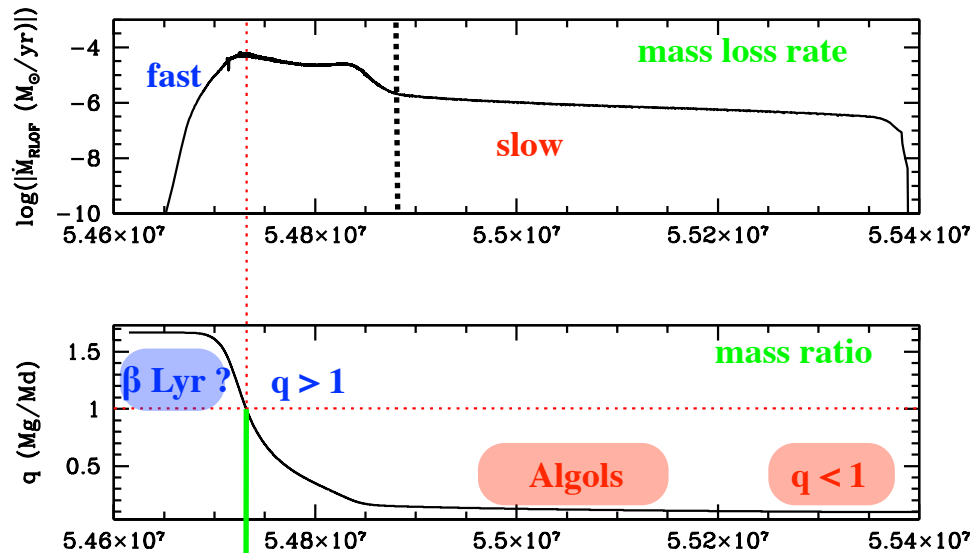


$$\zeta_R = \frac{\partial \ln R_R}{\partial \ln M_2} = \frac{d \ln A}{d \ln M_2} + \frac{d \ln f_2(q)}{d \ln q} \frac{d \ln q}{d \ln M_2}$$

governs the stability of the mass transfer

The Algol paradox : Algols vs β Lyr...

- Algols : on-going, slow mass transfer
- β Lyr : on-going, fast mass transfer precursors of Algols ?



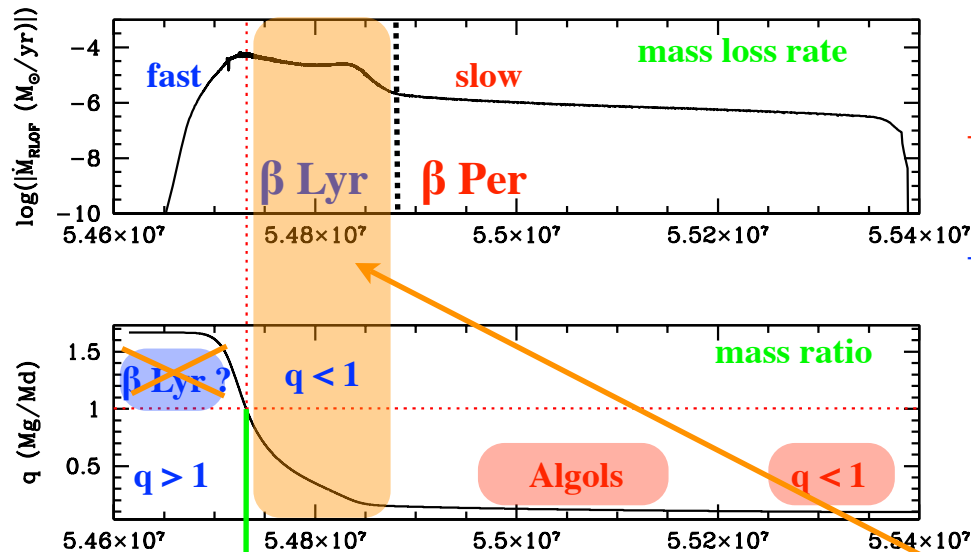
Dave McCarty, Coca-Cola Space Science Center

SCIENCEPHOTOLIBRARY

The Algol paradox : Algols vs β Lyr...

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β Per (Algol)	G8III + B8V	2.87	0.8	3.7	3.5	2.9	0.65	2.27
β Lyr	B8 II + BV? + disk	12.9	4 ?	14 ?				

Van Rensbergen et al., A&A 528, A16, 2011



- Algols : on-going, slow mass transfer

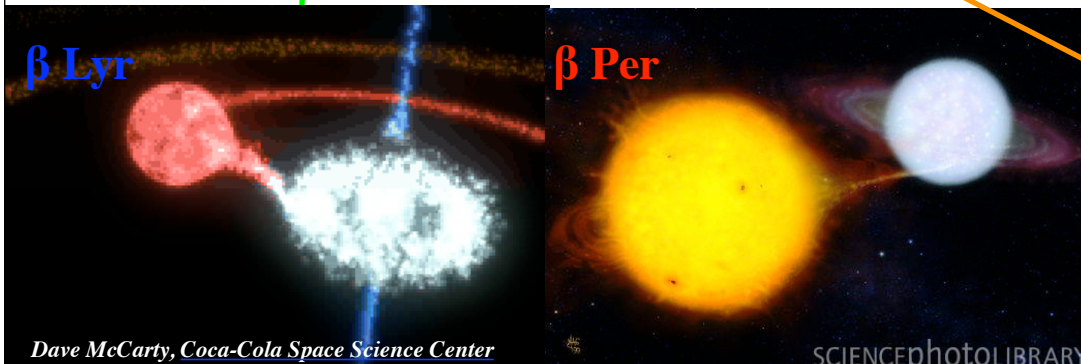
- β Lyr : on-going, fast mass transfer
precursors of Algols ?

β Lyr itself:

fast mass transfer, \dot{P} , disc, jet : OK !

$$T_{\text{prim.eclipse}}(\text{d}) = \text{JD}2408247.966 + 12.913780 \text{ E} + 3.87196 \cdot 10^{-6} \text{ E}^2$$

BUT: $q < 1$! with fast mass transfer

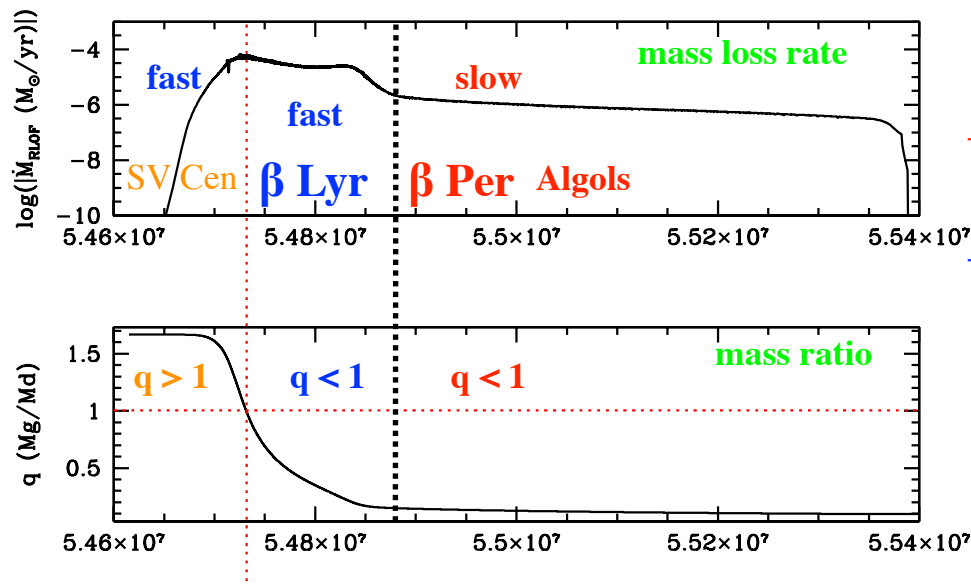


The Algol paradox : Algols vs β Lyr...

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β Per (Algol)	G8III + B8V	2.87	0.8	3.7	3.5	2.9	0.65	2.27
β Lyr	B8 II + BV? + disk	12.9	4 ?	14 ?				
SV Cen	B3 II + B1V	1.66	11	9	$\dot{M} = 1.6 \cdot 10^{-4}$			

Van Rensbergen et al., A&A 528, A16, 2011

Van Rensbergen et al., 2011



- Algols : on-going, slow mass transfer

- β Lyr : on-going, fast mass transfer

precursors of Algols ?

SV Cen better candidate ?

Evolutionary sequence ?

SV Cen \rightarrow β Lyr \rightarrow Algols

W Ser

A technical parenthesis is needed about **how to derive stellar masses...**

(later on !)

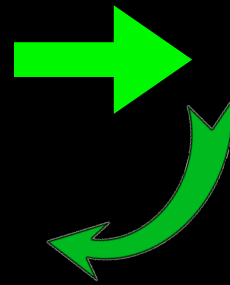
The binary zoo

Classification of binary stars:

There are three possible ways to classify binary stars, based on:

i) **Mass transfer:**

- a. Detached system
- b. Semi-detached system
- c. Contact system



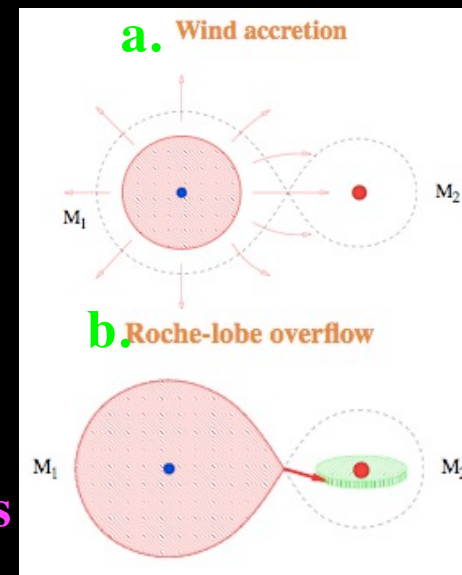
- a. wind accretion
- b. Roche-lobe overflow

ii) **Observational properties**

- a. photometric binary
- b. [peculiar] 'abundance' binary
- c.



iii) **Evolutionary stage**



Knowing the location of the binary in all 3 schemes often is the goal of binary-star research !

The binary zoo

Classification of binary stars:

There are three possible ways to classify binary stars, based on:

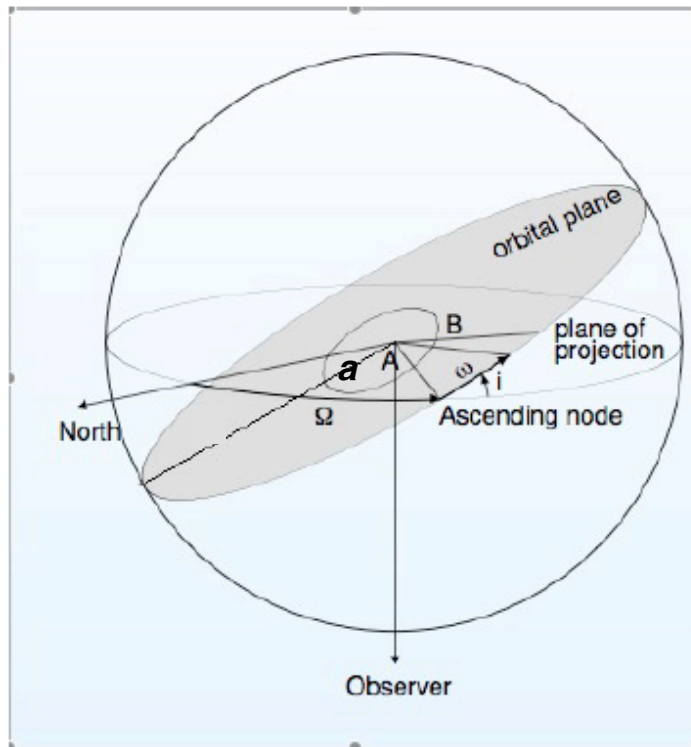
- i) Mass transfer
- ii) Evolutionary stage
- iii) **Observational properties**

We now go through every class of ‘observational properties’

But first, some definitions about orbital elements... [-> **Mazeh, Marsh**]

Orbital elements

Relative orbit (B with respect to A)



Kepler third law
(in relative orbit):

$$a^3 / P^2 = G (M_A + M_B) / 4\pi^2$$

Orbital elements

Size of orbit:

a semi-major axis (B wrt A)

e eccentricity

$$= \sqrt{a^2 - b^2} / a$$

(b = semi-minor axis)

Orientation in plane:

ω argument of periastron

Orientation of plane wrt sky:

Ω Position angle of ascending node

i inclination on the plane of the sky

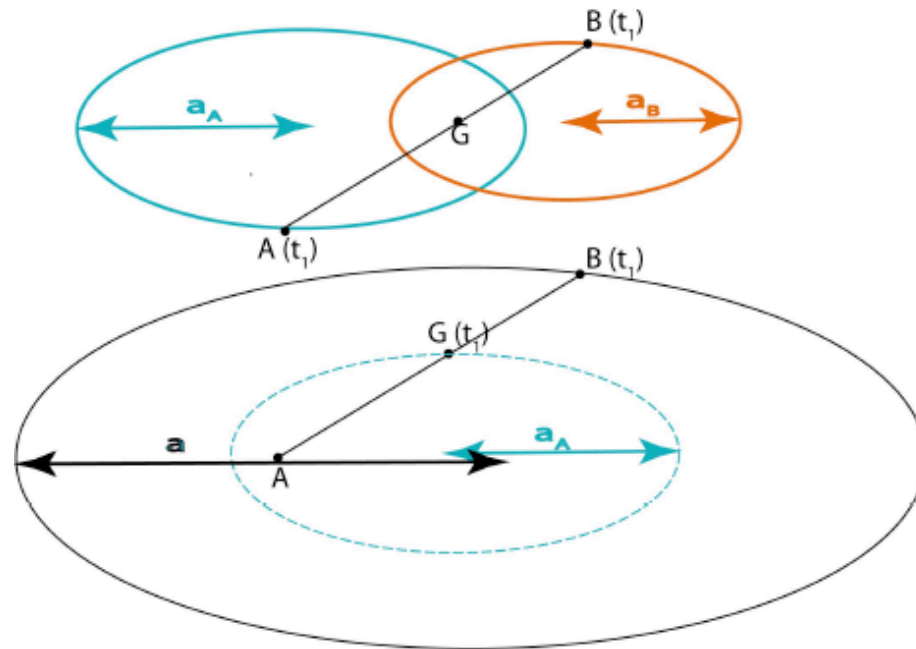
Time:

P orbital period

T Epoch of passage (usually at periastron)

Absolute and relative orbits

G: center-of-mass; A, B components



Absolute orbits
(A, B wrt G): a_A, a_B

Relative orbit
(B wrt A): a

A moves on an ellipse around G \rightarrow G moves on an ellipse around A (a_A)

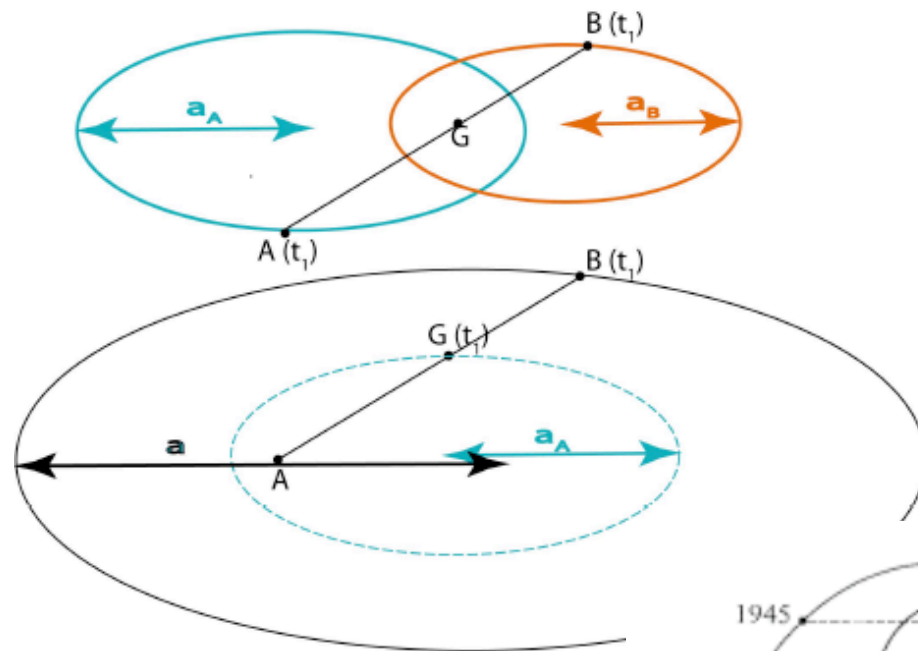
B is always further out, on the same AG ($\equiv r_A$) segment

At all times: $r_A M_A = r_B M_B$ (definition of G) $\rightarrow r_B = r_A M_A / M_B \rightarrow r_{AB} = r_A + r_B = r_A (M_A + M_B) / M_B$.

Since motion of G around A is an ellipse, then motion of B around A will be an ellipse as well, with a semi-major axis scaled by the same factor $(M_A + M_B) / M_B$: $a_{AB} = a_A + a_B = a_A (M_A + M_B) / M_B$

Absolute and relative orbits

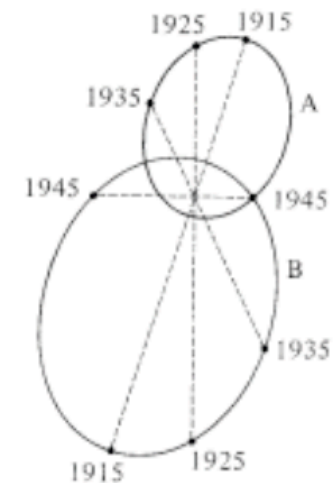
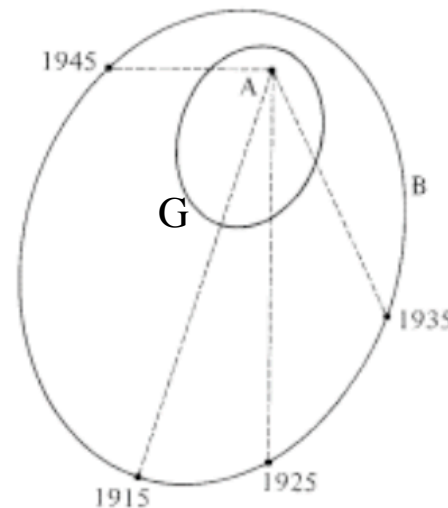
G: center-of-mass; A, B components



Absolute orbits
(A, B wrt G): a_A, a_B

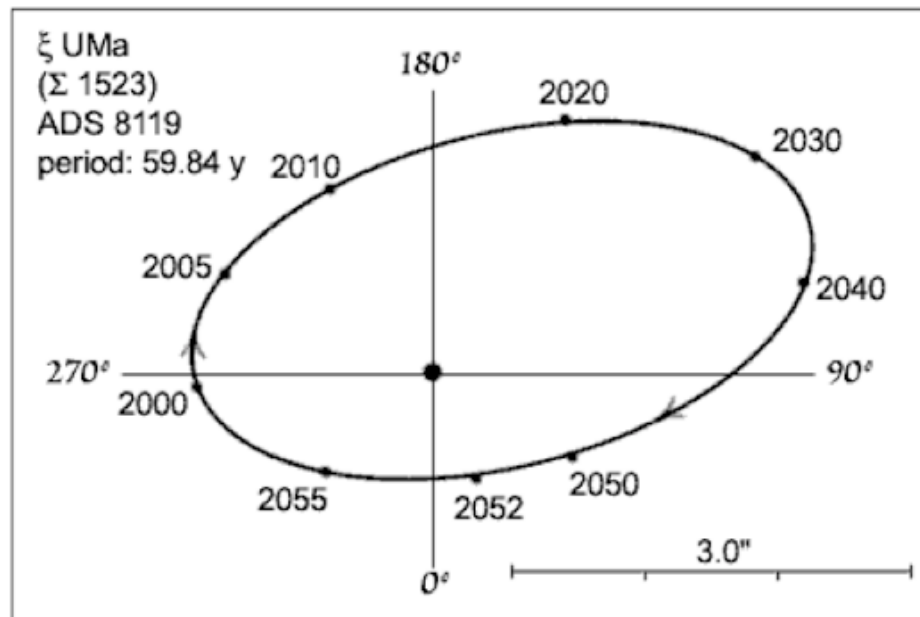
Relative orbit
(B wrt A): a

Example:
99 Her
P = 56.4 yr,
a = 1.0 arcsec



The various kinds of binaries

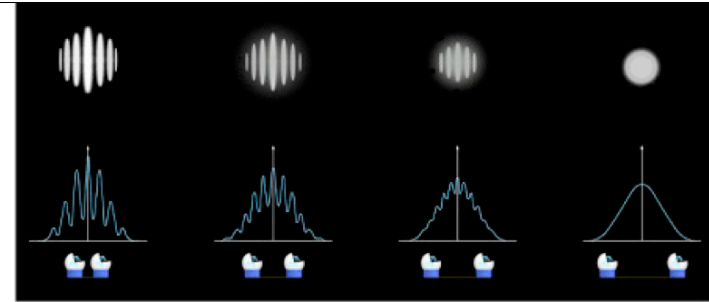
Type	Notation	Two stars visible?	orbit	dimension
visual and interferometric	VB	yes	relative	angular



The two stars are resolved and we can see them orbit each other

Orbit of ξ UMa, the first visual orbit ever computed in 1827

The various kinds of binaries

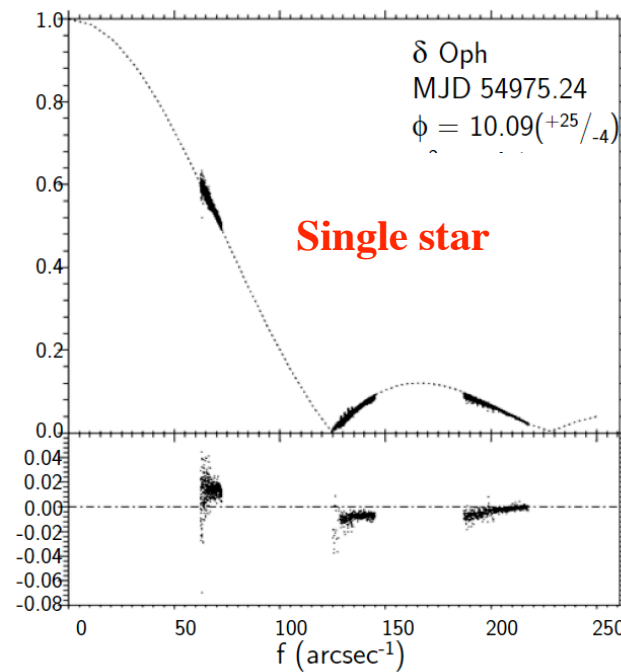
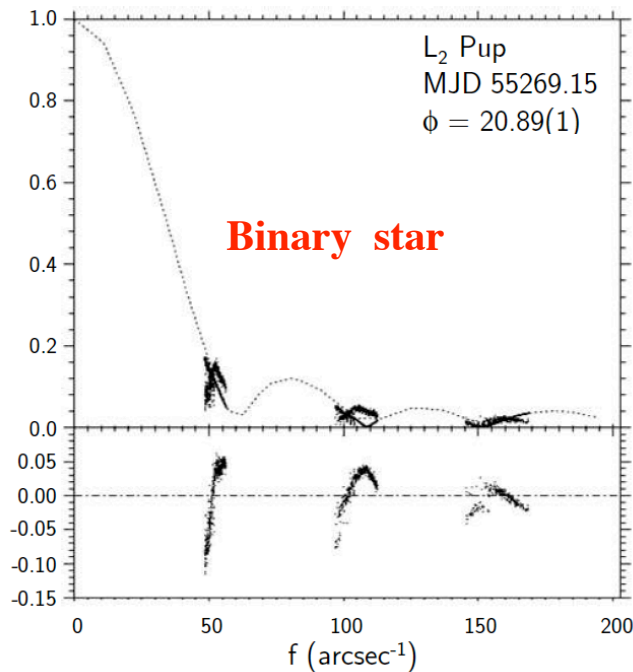


Interferometric Fringes at Different Telescope Baselines (Simulation)

ESO PR Photo 10e/01 (18 March 2001)

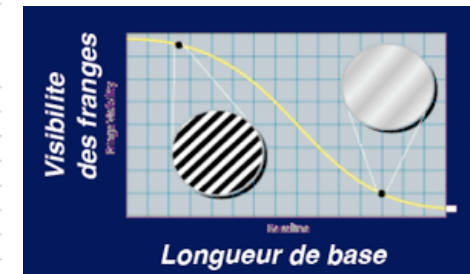
© European Southern Observatory

Type	Notation	Two stars visible?	orbit	dimension
visual and interferometric	VB	yes	relative	angular



Use the fringe visibility as a function of telescope baseline

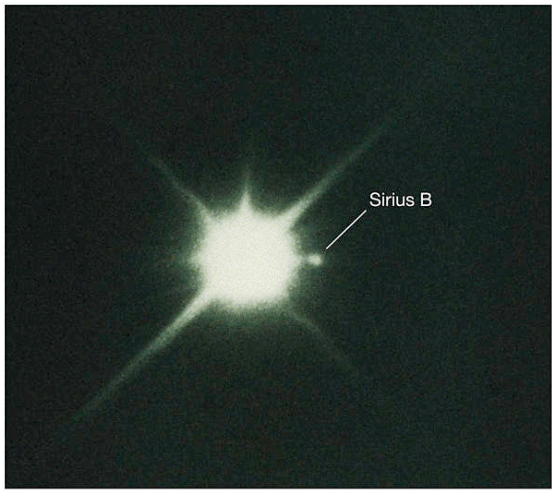
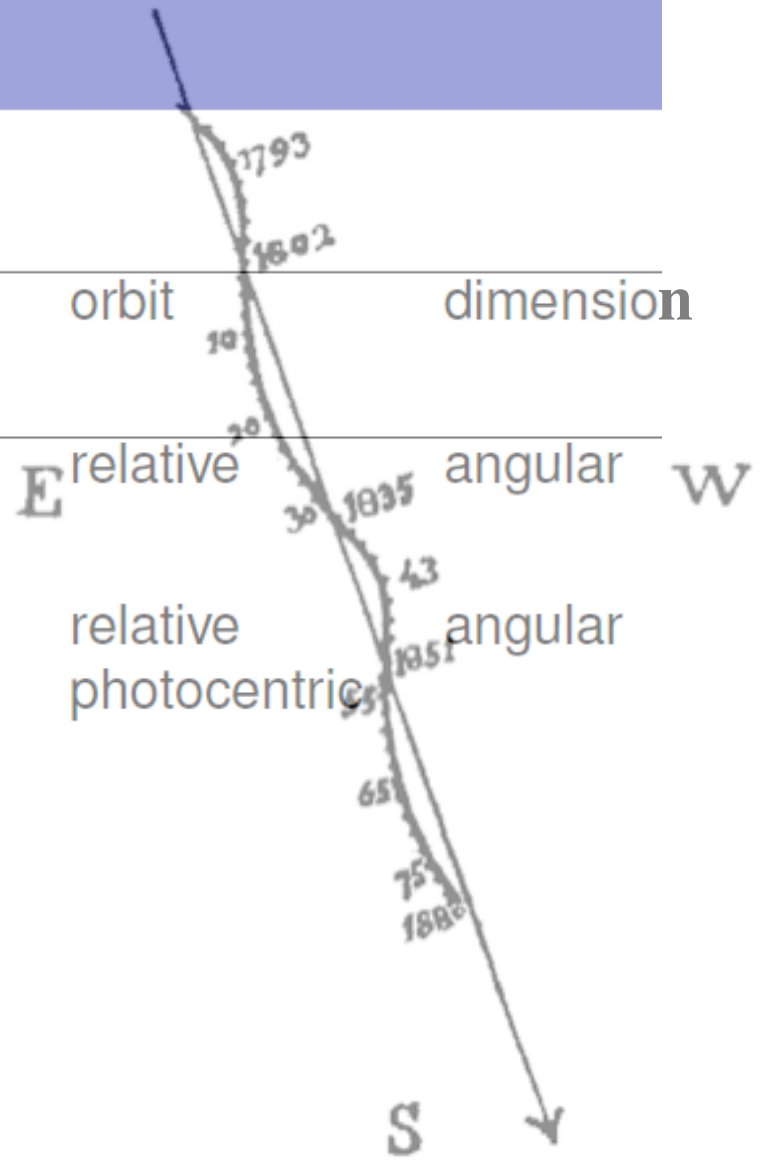
Fringe visibility



The various kinds of binaries

N

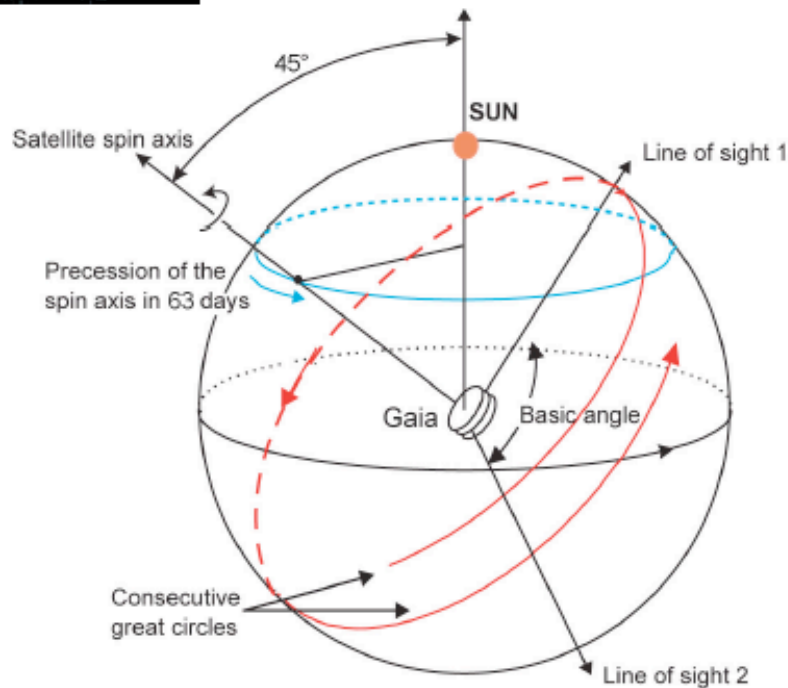
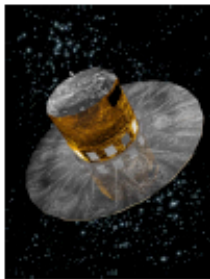
Type	Notation	Two stars visible?	orbit	dimension
visual and interferometric	VB	yes	relative	angular
astrometric	AB	yes no	relative photocentric	angular



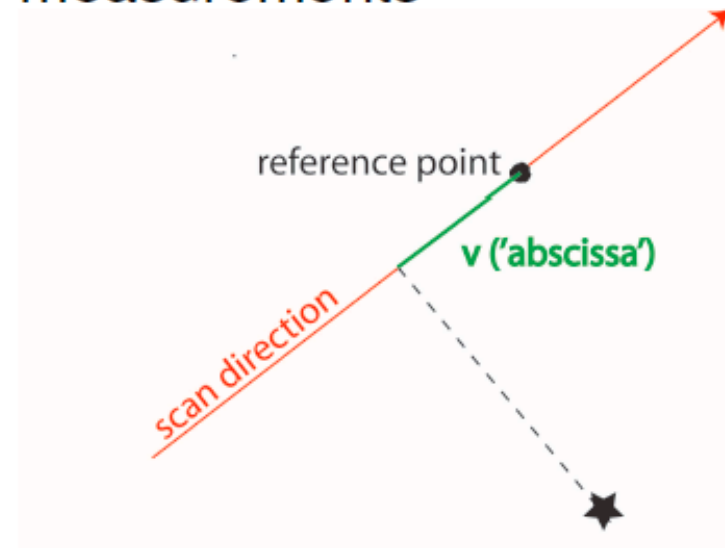
Non-linear motion on the sky

Astrometric binaries (I)

Basic principles

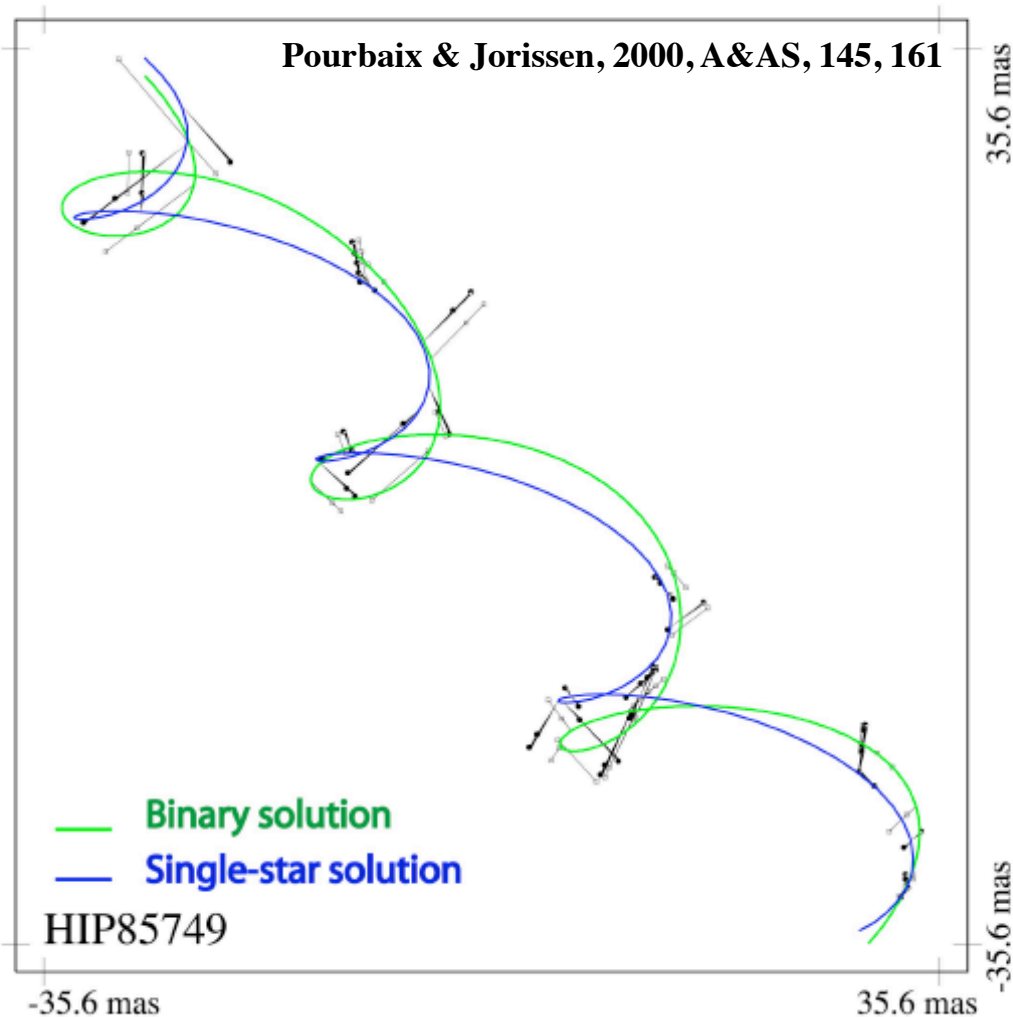


The Hipparcos and Gaia satellites scan the sky and perform 1D positional measurements



Astrometric binaries(II)

Basic principles



Comparison of the
parallactic motion of the
center of mass

(more precisely **photocenter**)

with the **true motion of
the star, after addition of
the orbital motion**

$$a_{\text{photocentre}} = (a_A + a_B) \\ \times \left(\frac{M_B}{M_A + M_B} - \frac{1}{1 + 10^{0.4\Delta m}} \right)$$

In case of perfect twins
(SB2 with $\Delta m = 0$, $M_A = M_B$):

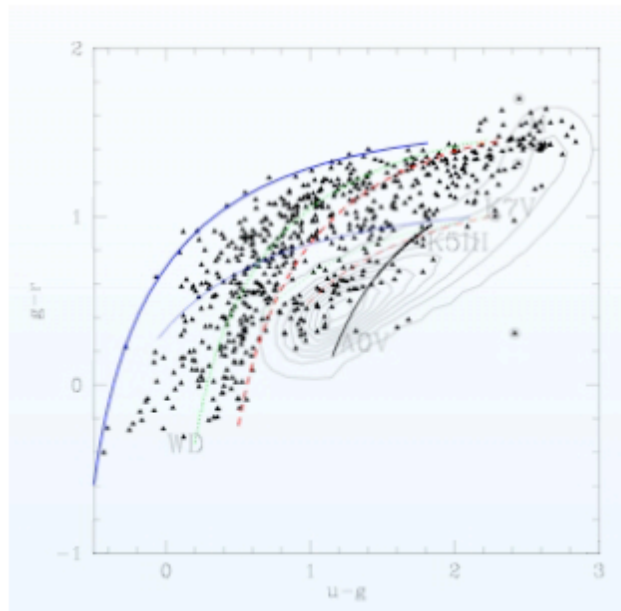
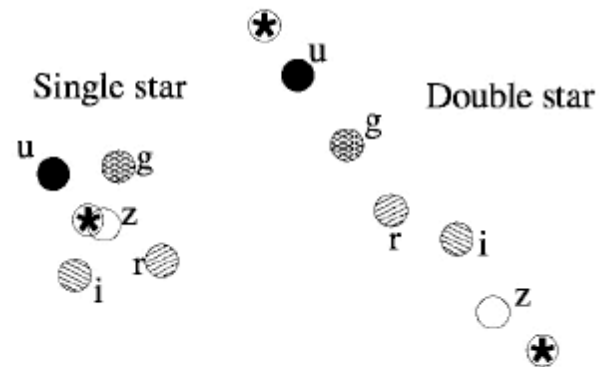
$$a_{\text{photocentre}} = 0$$

For SB1 ($\Delta m = \infty$):

$$a_{\text{photocentre}} \sim a_A$$

Astrometry (V)

Color-induced displacement - Application to SDSS



The position of the photocentre of two stars with different colours is a function of wavelength (e.g., Gunn u, g, r, i, z) but is always located on the segment joining the two stars.

Look for stars with $d(u, z) > 0.2''$
[and exclude asteroids !]

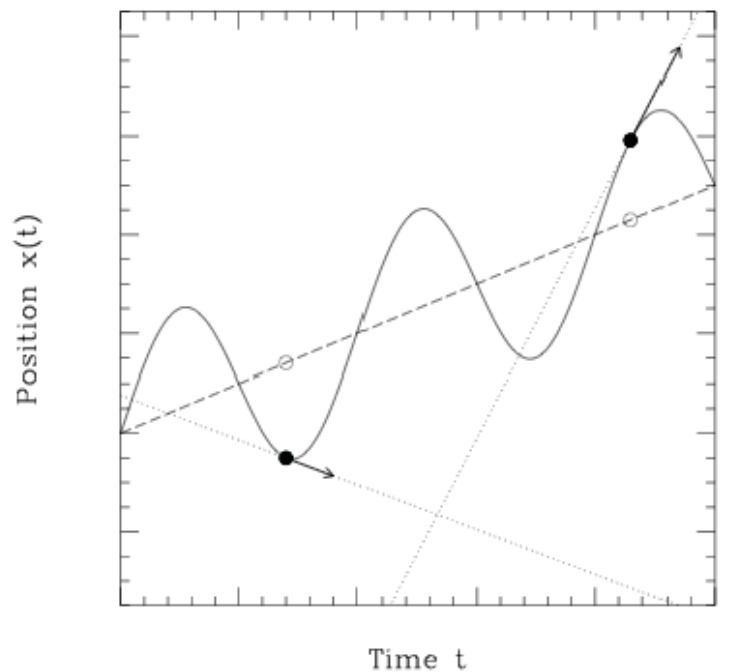
These stars are binaries (mostly WD + MV pairs) because they also exhibit composite colors

Pourbaix et al. 2004, A&A 423, 755

Astrometry (VI)

$\Delta\mu$ binaries (I)

Proper motion measured on short time scale (e.g. Hipparcos: 3 y) with respect to orbital period will contain a strong orbital component and will differ from **true** proper motion measured on long time scale (e.g. Tycho-2: 100 y)

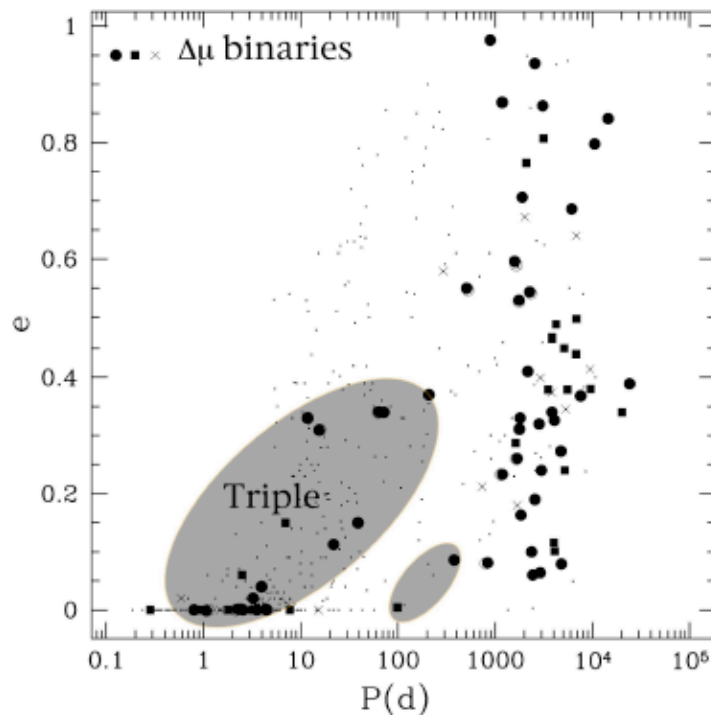


Astrometry (VI)

$\Delta\mu$ binaries (II)

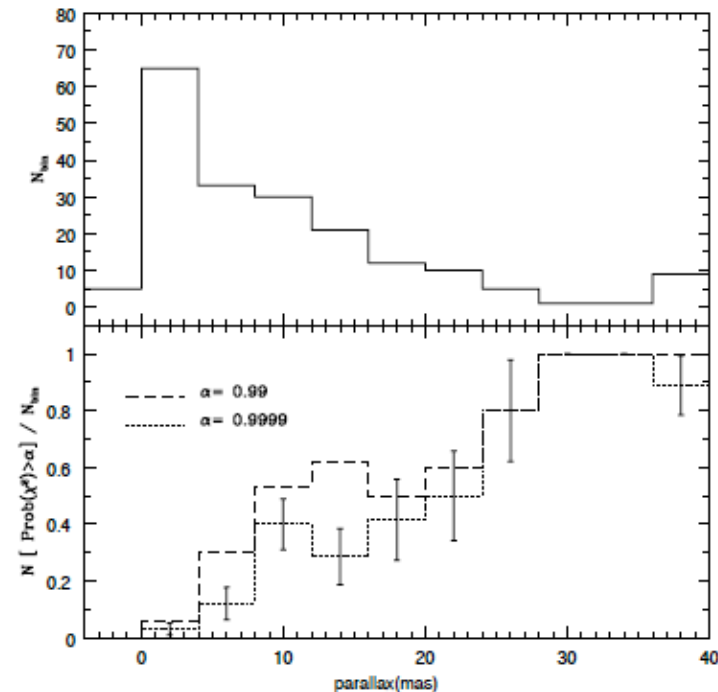
$\Delta\mu$ binaries found among spectroscopic binaries with known P :

- expected at $P > \sim 1500$ d
- triple systems at $P < \sim 400$ d



Frankowski et al. 2007, A&A 464, 377

Detection efficiency of $\Delta\mu$ binaries rises to 100% at parallaxes > 30 mas



The various kinds of binaries

Type	Notation	Two stars visible?	orbit	dimension
visual and interferometric	VB	yes	relative	angular
astrometric	AB	yes no	relative photocentric	angular
spectroscopic	SB2 SB1	yes no	absolute absolute	linear

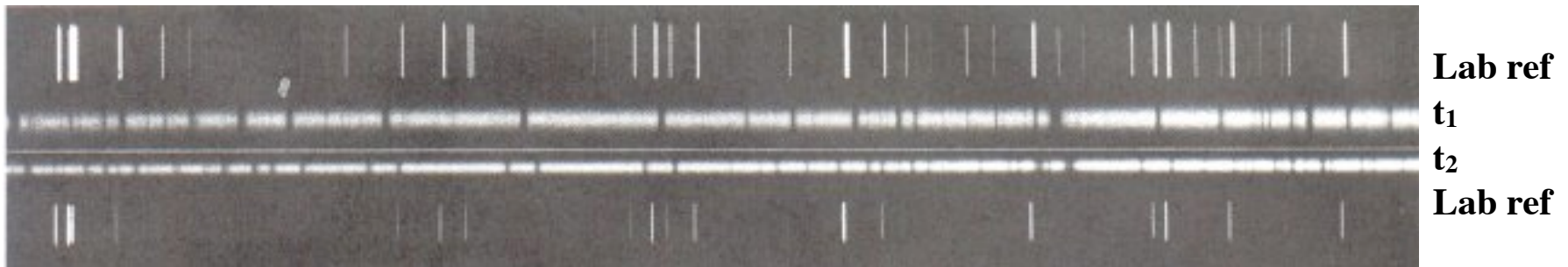
Spectroscopic binaries (I)

Spectral lines of one (SB1) or both (SB2) stars show Doppler shifts

Example: α Gem (SB1)

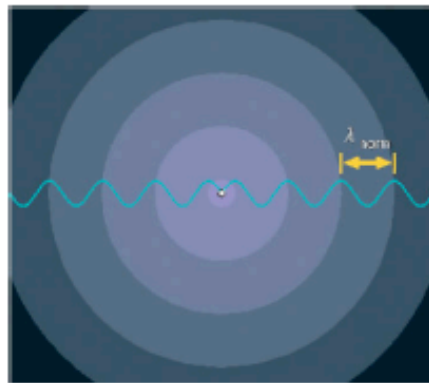


Example: α Ari (SB2)

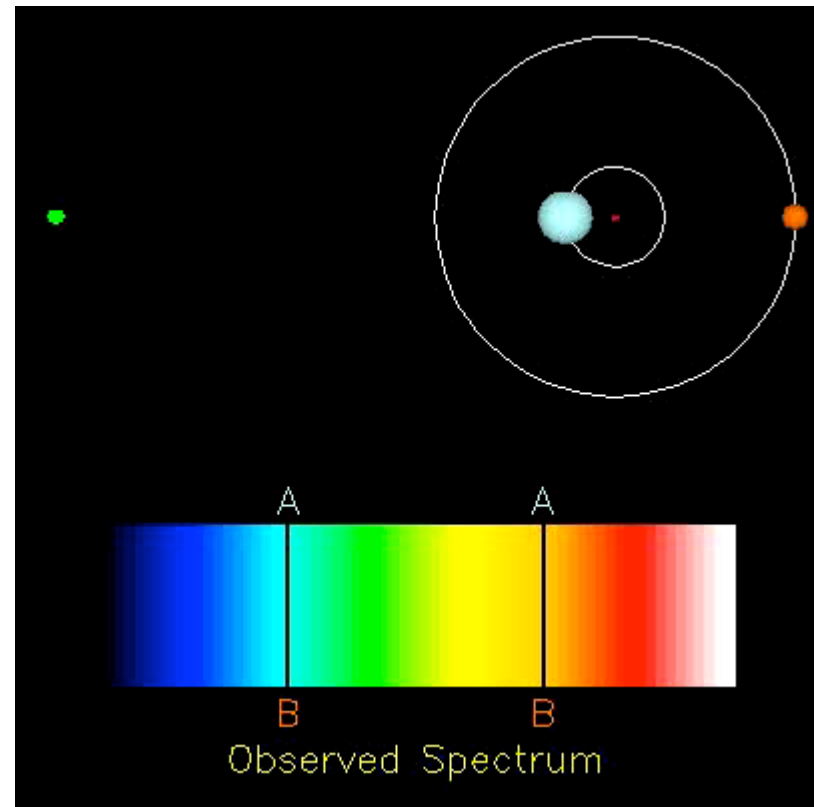
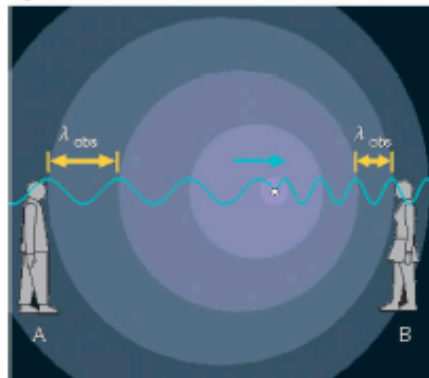


Spectroscopic binaries (I)

Detection (of **absolute** orbit) based on the Doppler effect:

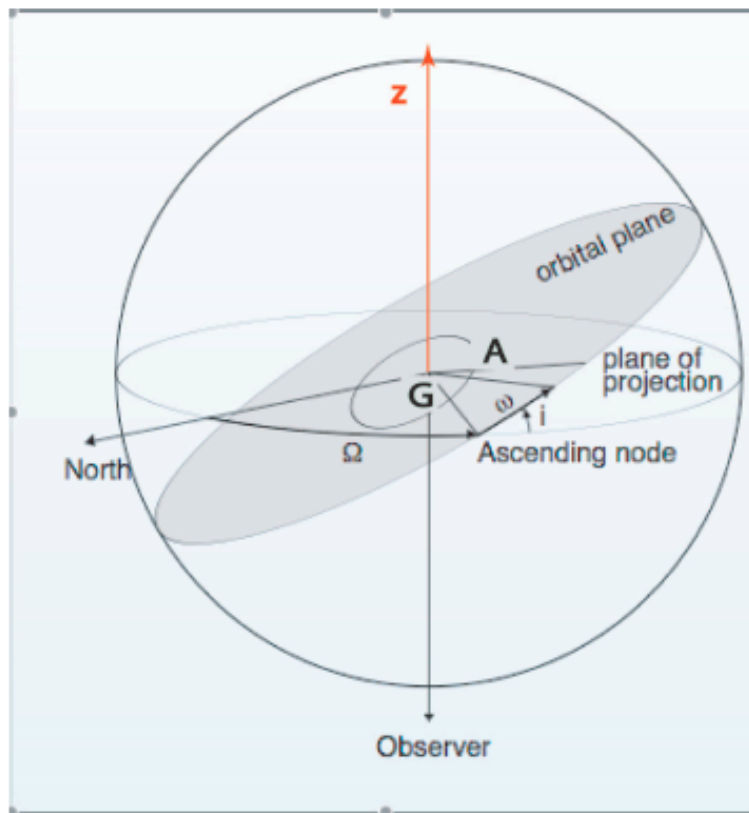


b)



Spectroscopic binaries (II)

The radial-velocity curve



G : center of gravity of the A+B components
A : visible component
B : invisible component

$$V_r(A)$$

$$= V_r(G) + dz(A)/dt$$

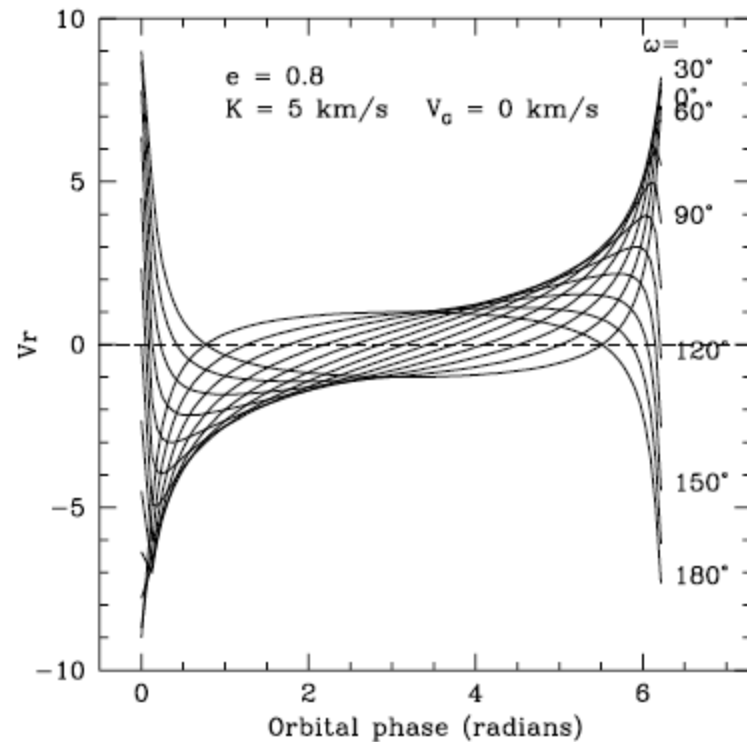
$$= V_r(G) + K_A (e \cos \omega + \cos(\omega + \nu(t)))$$

where

$$K_A = \frac{2\pi}{P} \times \frac{a_A \sin i}{(1 - e^2)^{1/2}}$$

Spectroscopic binaries (III)

The radial-velocity curve



$$V_r(A)$$

$$= K_A (e \cos \omega + \cos (\omega + \nu(t)))$$

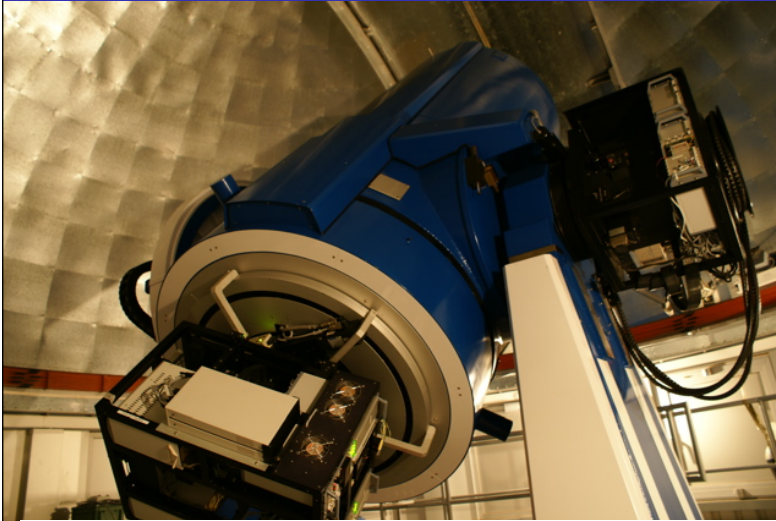
where

$$K_A = \frac{2\pi}{P} \times \frac{a_A \sin i}{(1 - e^2)^{1/2}}$$

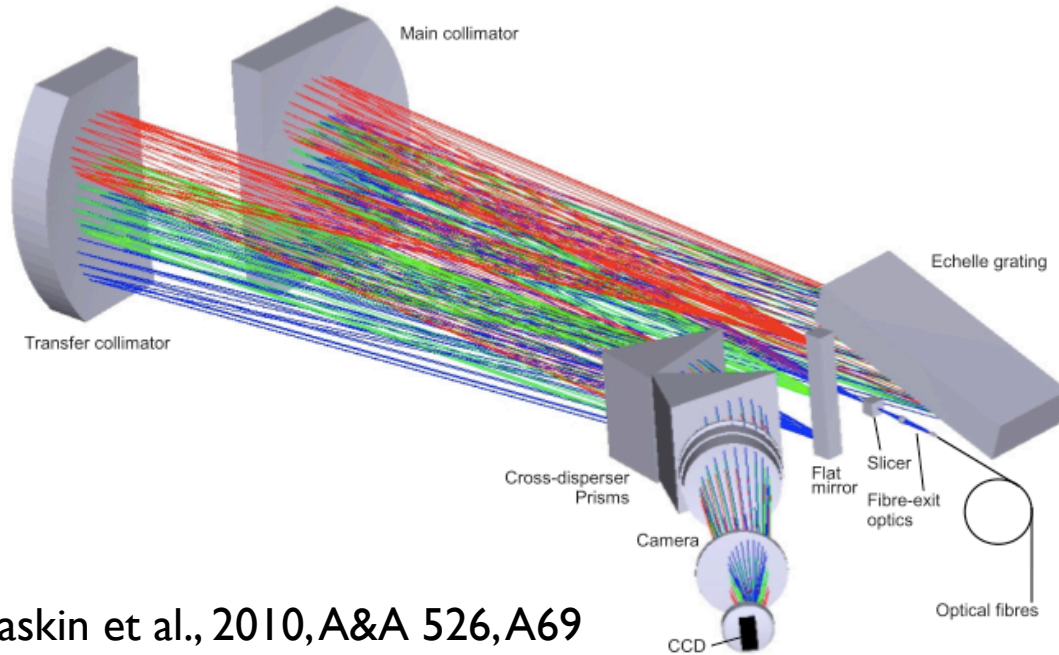
(see also the radial-velocity curve generator at

<http://www.astro.cornell.edu/academics/courses/astro1101/java/binary/binary.htm>

Spectroscopic binaries: HERMES/Mercator spectrograph



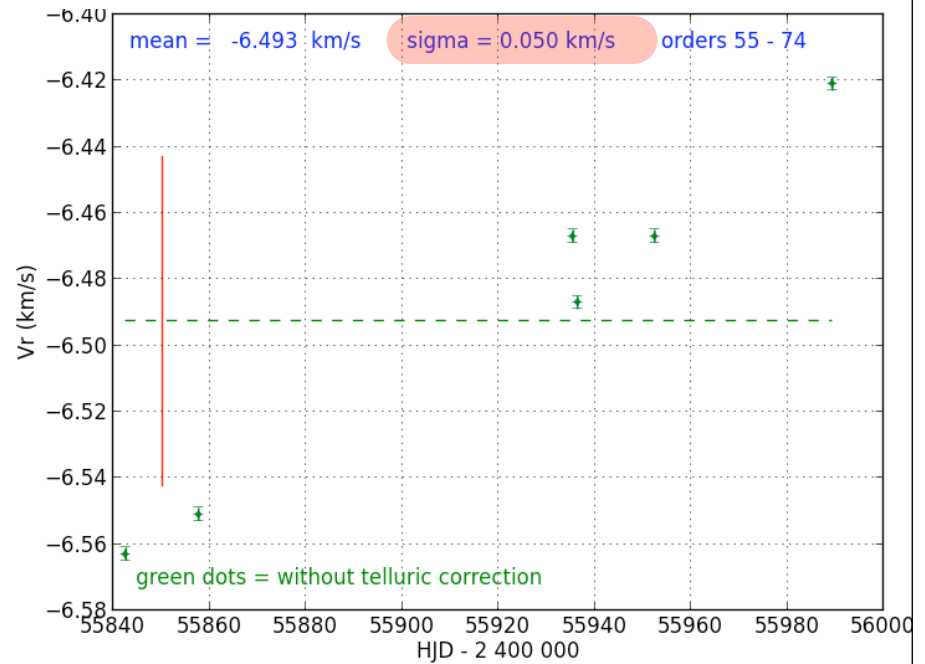
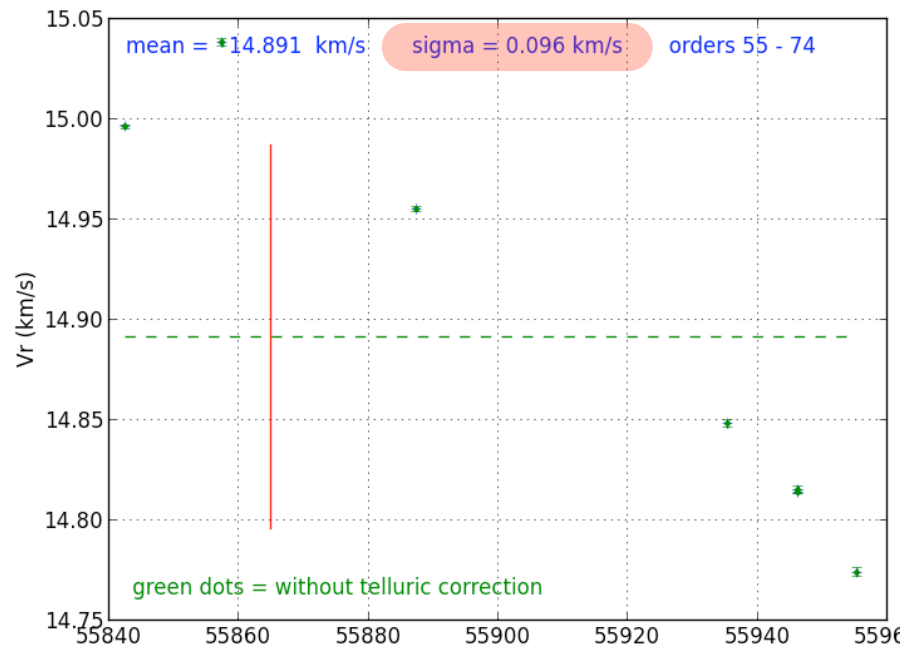
Mercator 1.2m telescope
operated by KULeuven
at Roque de los
Muchachos Observatory
(La Palma, Canary Islands)



Raskin et al., 2010, A&A 526, A69

Spectroscopic binaries (III)

The radial-velocity curve



Spectroscopy: Difficulties (I)

- A **one-dimensional measurement**:
only partial access to orbital elements
- **Pulsation of atmosphere** (Miras, Cepheids, RV Tau...)
causes **intrinsic velocity variations**
and make binary detection difficult/impossible

Spectroscopy: Difficulties (III)

Only partial access to orbital elements

$$V_r(A) \\ = \\ K_A (e \cos \omega + \cos (\omega + \nu(t)))$$

where

$$K_A = \frac{2\pi}{P} \times \frac{a_A \sin i}{(1 - e^2)^{1/2}}$$

■ If **only one observable spectrum (A)** (because companion too faint: on the low MS or WD) :

■ **degeneracy between i and a_A :**
 $K_A \propto a_A \sin i$
(relative a cannot be derived)

Spectroscopy: Difficulties (III)

Only partial access to orbital elements

$$V_r(A) \\ = \\ K_A (e \cos \omega + \cos (\omega + \nu(t)))$$

where

$$K_A = \frac{2\pi}{P} \times \frac{a_A \sin i}{(1 - e^2)^{1/2}}$$

- If only one observable spectrum (A) (because companion too faint: on the low MS or WD) :

- degeneracy between i and a_A :
 $K_A \propto a_A \sin i$
(relative a cannot be derived)

- only mass function $f(M)$ can be derived:

$$f(M) = \frac{(M_B \sin i)^3}{(M_A + M_B)^2} \\ = K_A^3 P (1 - e^2)^{3/2} / (2\pi G)$$

Spectroscopy: Difficulties (III)

Only partial access to orbital elements

$$V_r(A) \\ = \\ K_A (e \cos \omega + \cos (\omega + \nu(t)))$$

where

$$K_A = \frac{2\pi}{P} \times \frac{a_A \sin i}{(1 - e^2)^{1/2}}$$

Same for $V_r(B)$ and K_B

- If **only one observable spectrum (A)** (because companion too faint: on the low MS or WD) :

- **degeneracy between i and a_A** :
 $K_A \propto a_A \sin i$
(relative a cannot be derived)

- **only mass function $f(M)$ can be derived:**

$$f(M) = \frac{(M_B \sin i)^3}{(M_A + M_B)^2}$$

$$= K_A^3 P (1 - e^2)^{3/2} / (2\pi G)$$

- if **two observable spectra** (components of approx. equal L, aka 'composite spectra'):
only **$M_A \sin i, M_B \sin i, M_A/M_B$**

The various kinds of binaries and deriving masses

Binaries	Vis. and interf.	Astrometric AB1	AB2	Spectroscopic SB1	SB2	Eclipsing
Max $P \sim$ Min $P \sim$	200 y 1 y	100 y 1 y		30 y 1 d		~ 1 y 1 h
i ?	yes	yes	yes	no	no	yes
a ? (units)	$a_A + a_B$ (")	$a_{\text{photocentre}}$ (")	$a_{A,B}$ (")	$a_A \sin i$ (km)	$a_{A,B} \sin i$ (km)	a (R_*)
Masses	$(M_A + M_B)d^3$		$M_{A,B}$	$\frac{(M_B \sin i)^3}{(M_A + M_B)^2}$	$M_{A,B} \sin^3 i$	

AB2 systems are rare (Sirius, α Cen: Demarque et al. 1986)

Ecl + SB2 (Ex: HD 35155): individual masses may be derived or Vis + SB2 or Astrom. + SB2

Spectroscopy: Difficulties (I)

Despite the fact that the spectral Doppler shift is unavoidable in a binary, there are binary families however where it is hard, even impossible, to detect:

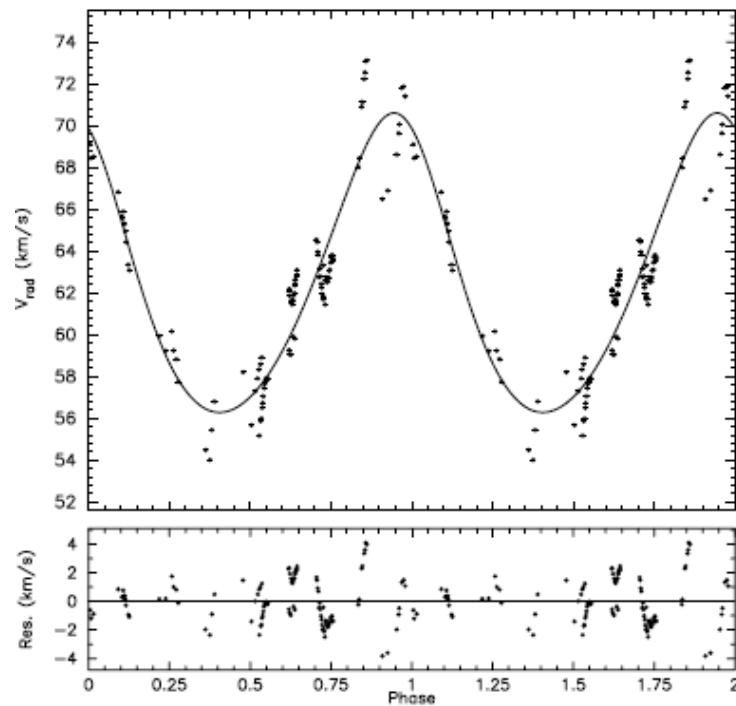
- **Pulsation of atmosphere** (Miras, Cepheids, RV Tau...) causes **intrinsic velocity variations** and make binary detection difficult/impossible

Spectroscopy: Difficulties (IV)

Intrinsic radial velocity variations: **RV Tau**

Binary post-AGB star IRAS 08544-4431

Orbital solution:



Orbital residuals due to pulsation

RV Tau variable:

$$P_{\text{orb}} = 499 \text{ d}, K_{\text{orb}} = 8 \text{ km/s}$$

Note that $K_{\text{puls}} < K_{\text{orb}}$

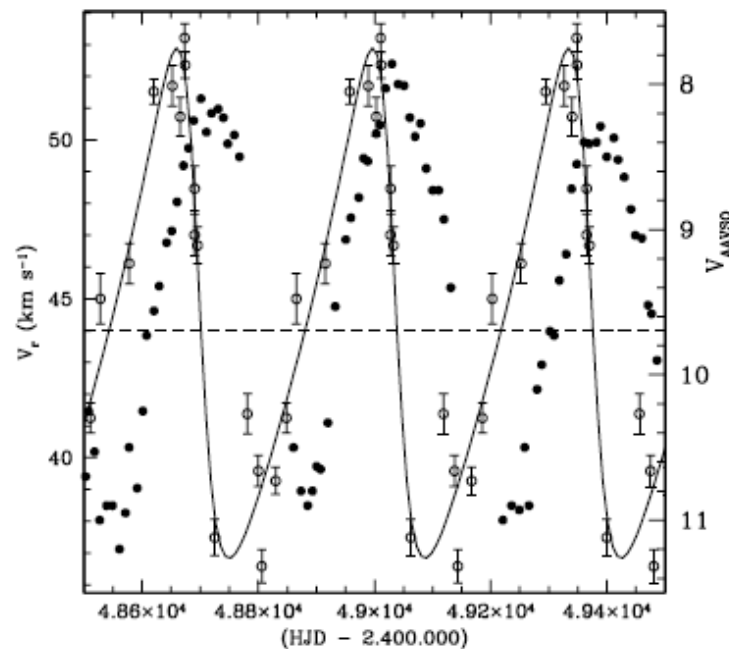
→ Orbit could be derived !

$$P_{\text{puls}} \sim 90 \text{ d}, K_{\text{puls}} = 4 \text{ km/s}$$

(Maas et al., 2003, A&A 405, 271)

Spectroscopy: Difficulties (V)

Intrinsic radial-velocity variations: **Miras**



(Jorissen, 2003, AGB Stars, eds. Habing & Olofsson, Springer)

The radial-velocity curve (○) of the **Mira** star **R CMi** is strongly correlated with its light curve (●)

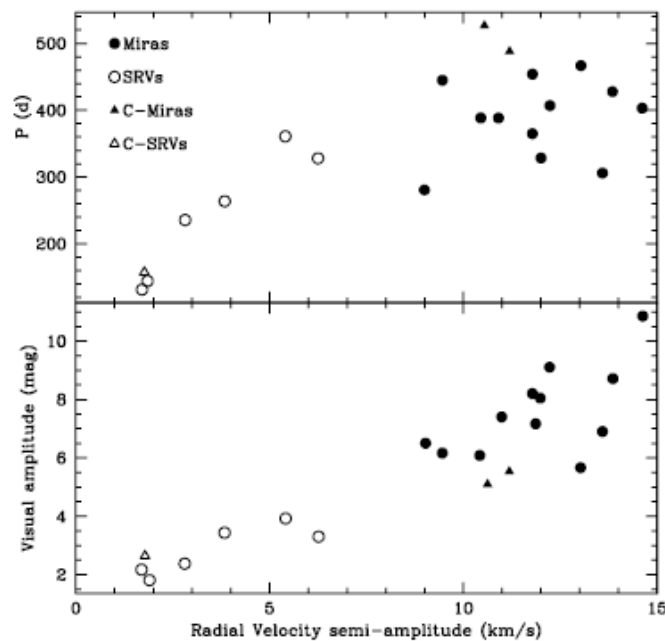
$$P_{\text{puls}} = 337.8 \text{ d};$$

$$K_{\text{puls}} = 8 \text{ km/s}$$

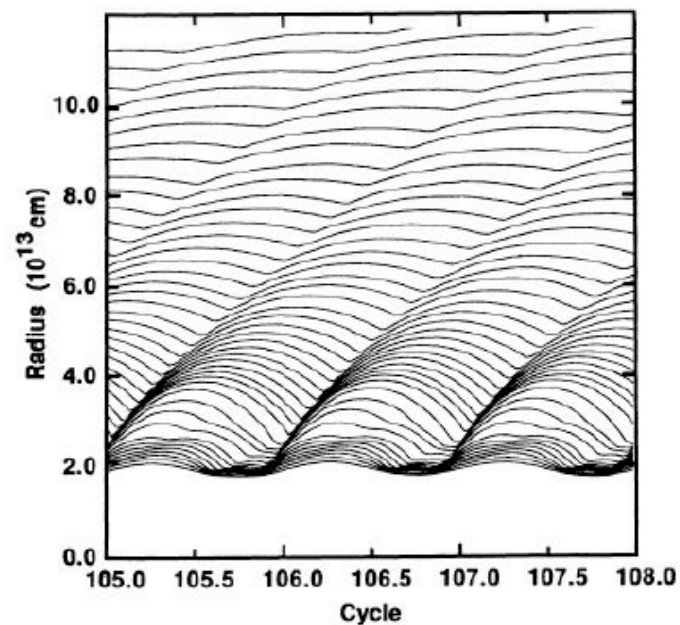
→ intrinsic V_r variations due to pulsation

Spectroscopy: Difficulties (VII)

Intrinsic radial-velocity variations: **Miras**



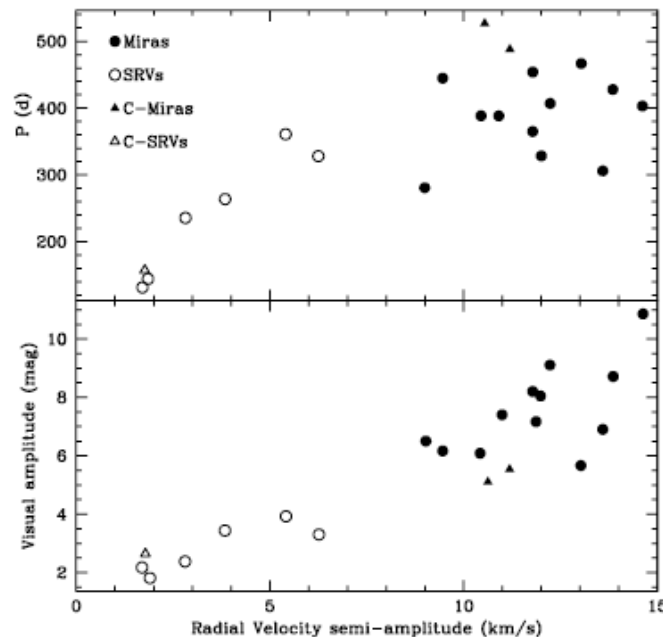
Vr semi-amplitude $K_{\text{puls}} \geq 10$ km/s
due to pulsation for Mira variables



(Jorissen, 2003, AGB Stars, eds. Habing & Olofsson, Springer)

Spectroscopy: Difficulties (VIII)

Intrinsic radial-velocity variations: **Miras**



(Jorissen, 2003, AGB Stars, eds. Habing & Olofsson, Springer)

Not many spectroscopic binaries are known among Mira variables because $K_{\text{orb}} \leq K_{\text{puls}}$
Other detection methods must be used!

Vr semi-amplitude $K_{\text{puls}} \geq 10$ km/s
due to pulsation for Mira variables

$$K_{\text{orb}} \text{ (km/s)} = 213 f(M_A, M_B)^{1/3} P^{-1/3} \text{ (d)} (1 - e^2)^{-1/2}$$

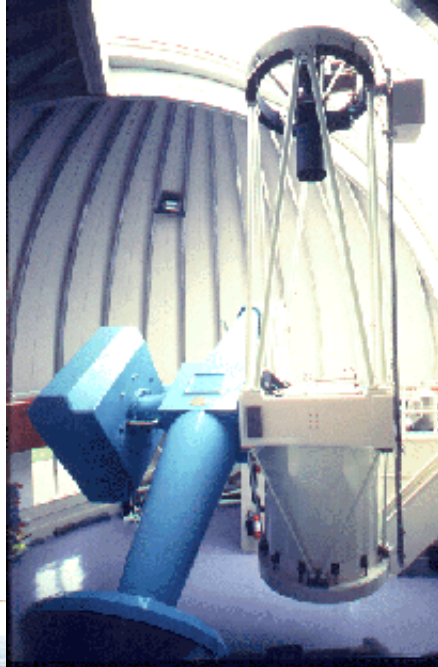
Adopting

$$P = 1000 \text{ d}, e = 0, M_A = 1.5 M_{\odot}, M_B = 0.5 M_{\odot}$$

yields $K_{\text{orb}} = 6.7 \text{ km/s} < K_{\text{puls}}$

Photometry: MACHO (I)

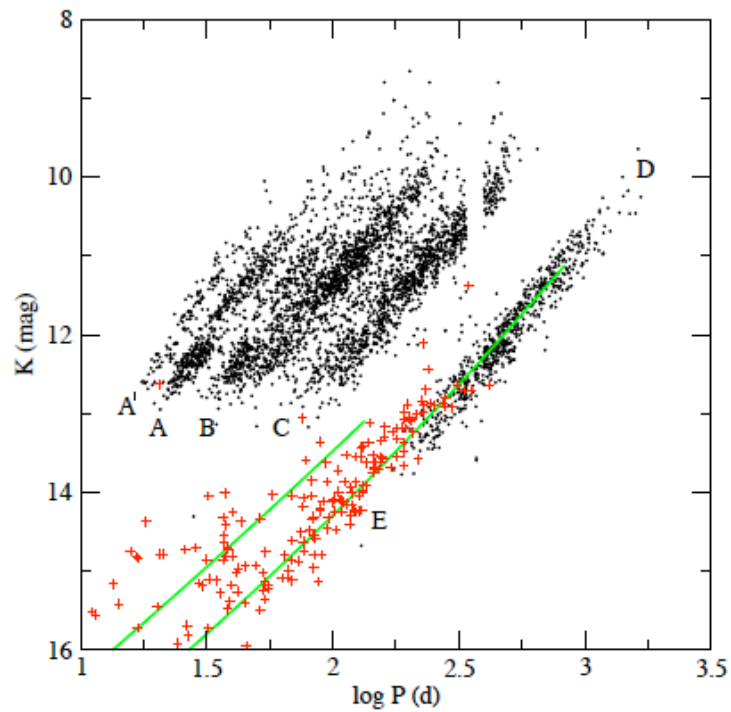
**Originally, a survey for micro lensing events
in the LMC with Mount Stromlo 50" telescope**



Photometry: MACHO (II)

A survey of long-period variables in the LMC

P-L relationship for LPVs in LMC



C Mira fundamental mode

A, B higher overtones

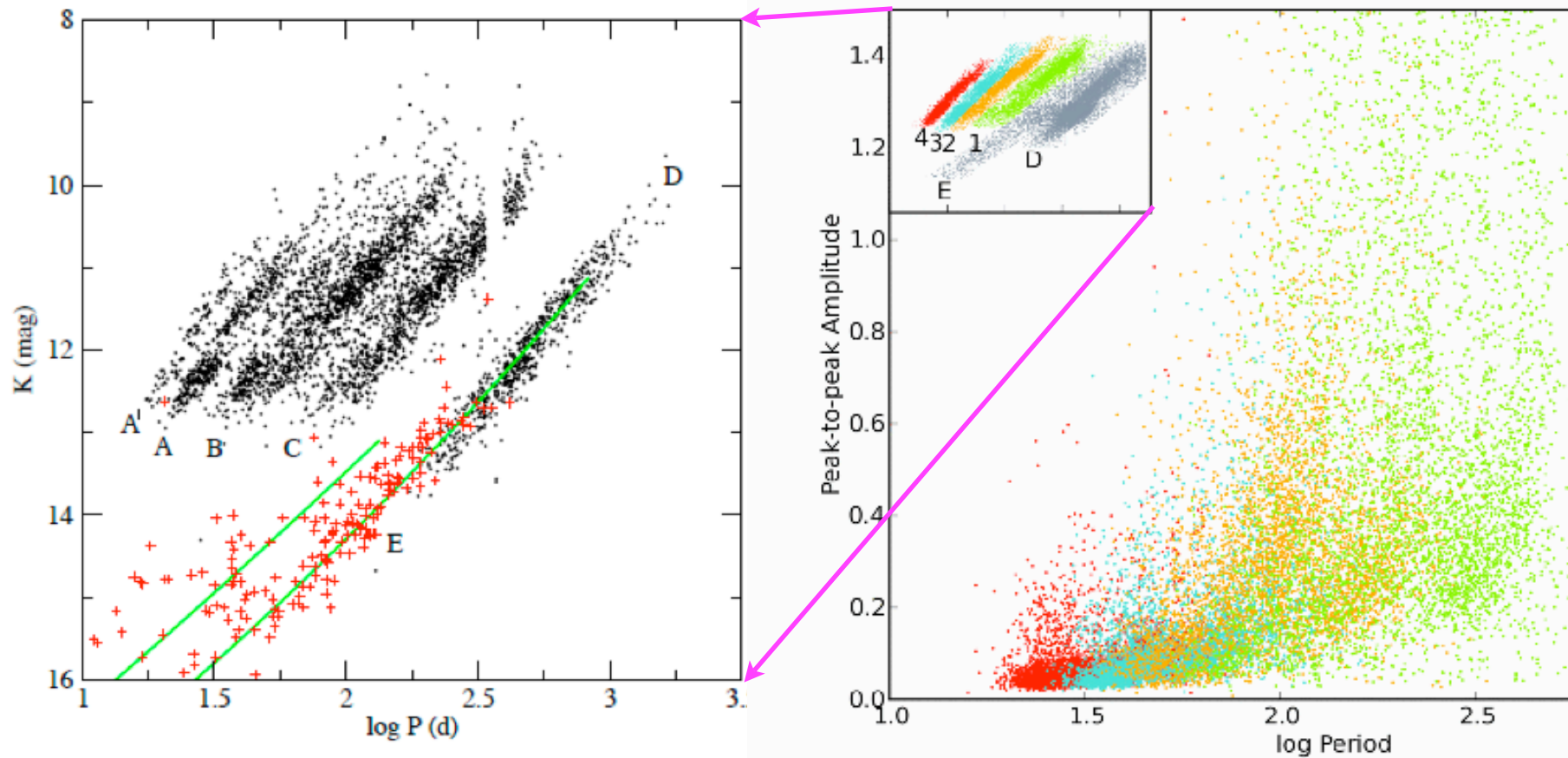
The enigmatic D and E sequences

Wood 2000, PASA 17,18; Derekas et al., 2006, ApJ 650, L55

Photometry: MACHO (III)

A survey of long-period variables in the LMC

1 = C = fundamental Mira pulsators
2, 3, 4 = A', A, B = overtone pulsators

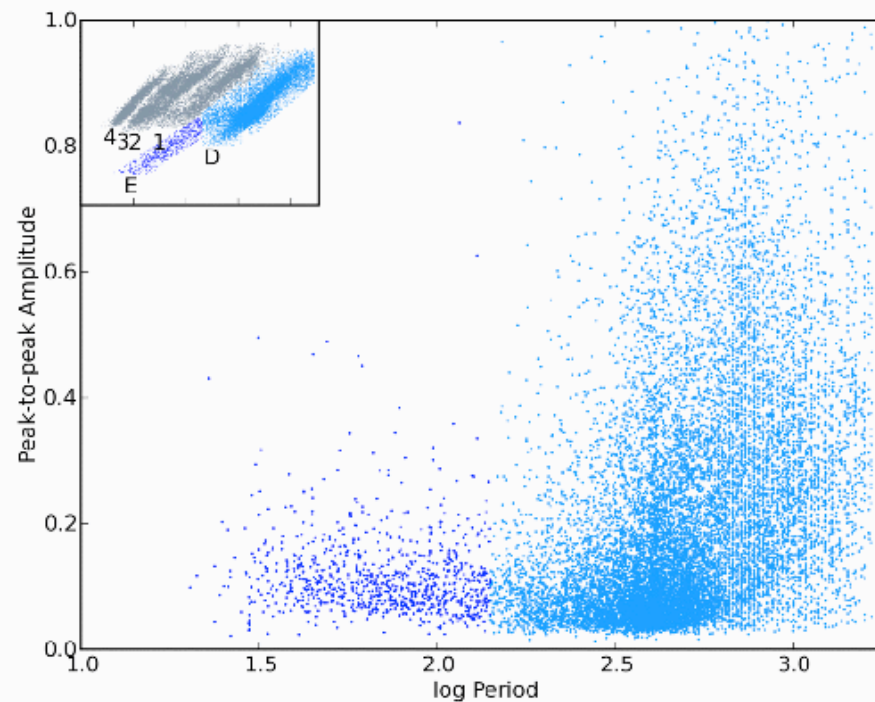
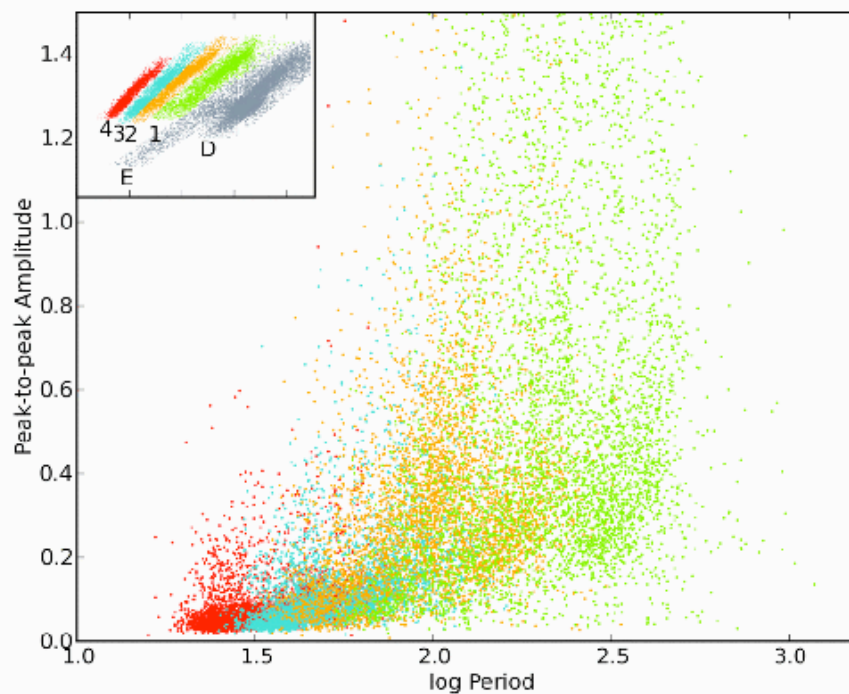


Photometry: MACHO (IV)

A survey of long-period variables in the LMC

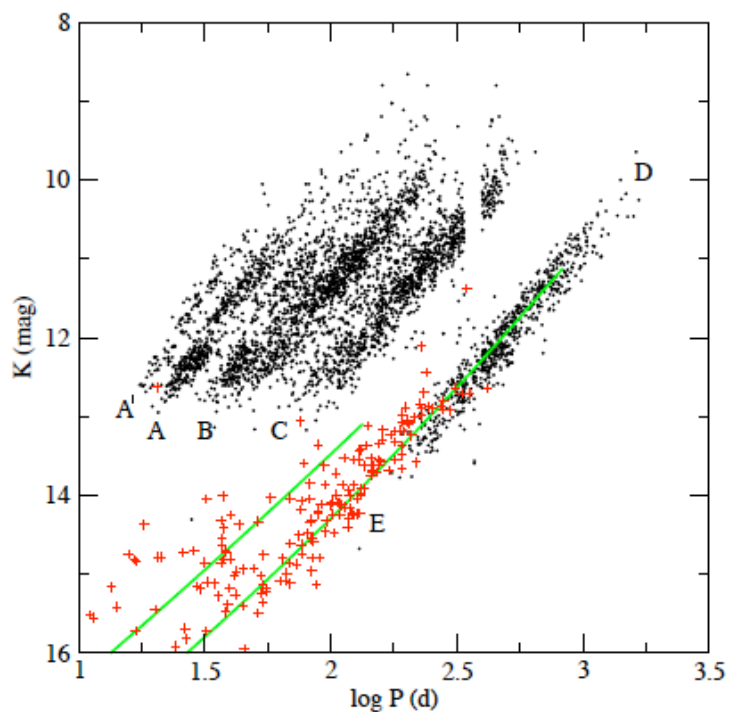
1 = C = fundamental Mira pulsators
2, 3, 4 = A', A, B = overtone pulsators

The enigmatic **D** and **E** sequences



Photometry: MACHO (V)

P-L relationship for LPVs in LMC



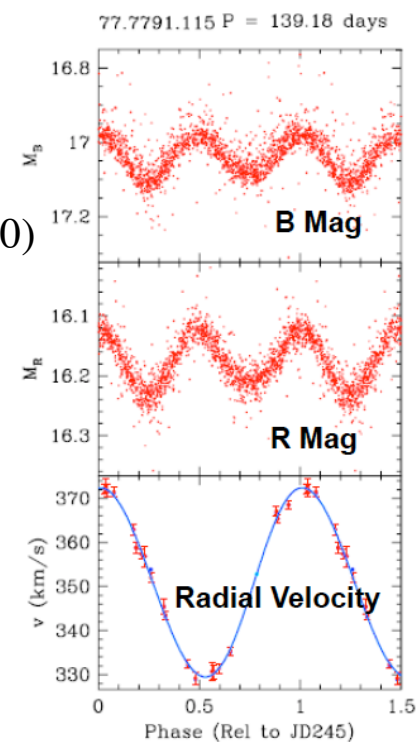
Wood 2000, PASA 17,18; Derekas et al., 2006, ApJ 650, L55

C Mira fundamental mode

A, B higher overtones

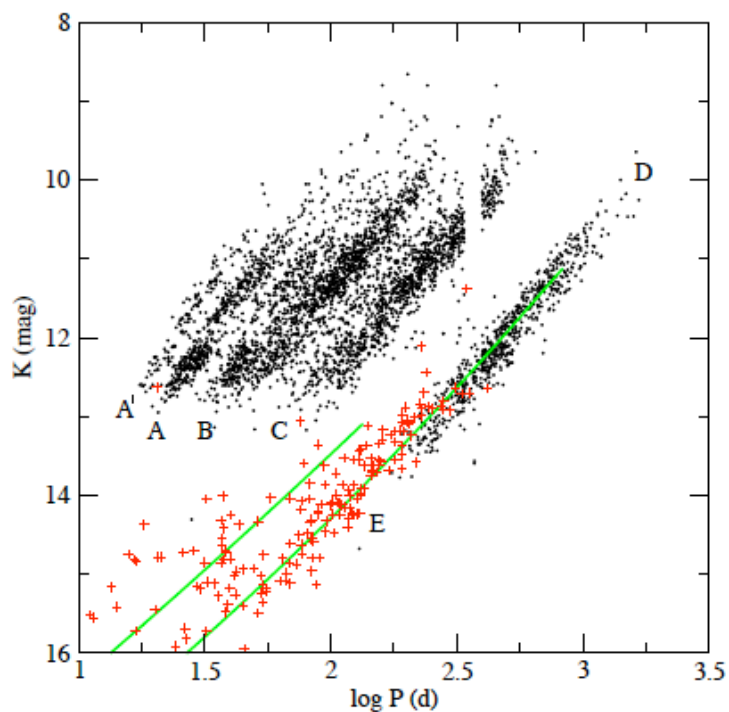
E eclipsing & ellipsoidal (+)

Nicholls et al.
(2010 MNRAS 405, 1770)
from radial velocities
confirm that sequence E
stars are binaries



Photometry: MACHO (V)

P-L relationship for LPVs in LMC



Wood 2000, PASA 17,18; Derekas et al., 2006, ApJ 650, L55

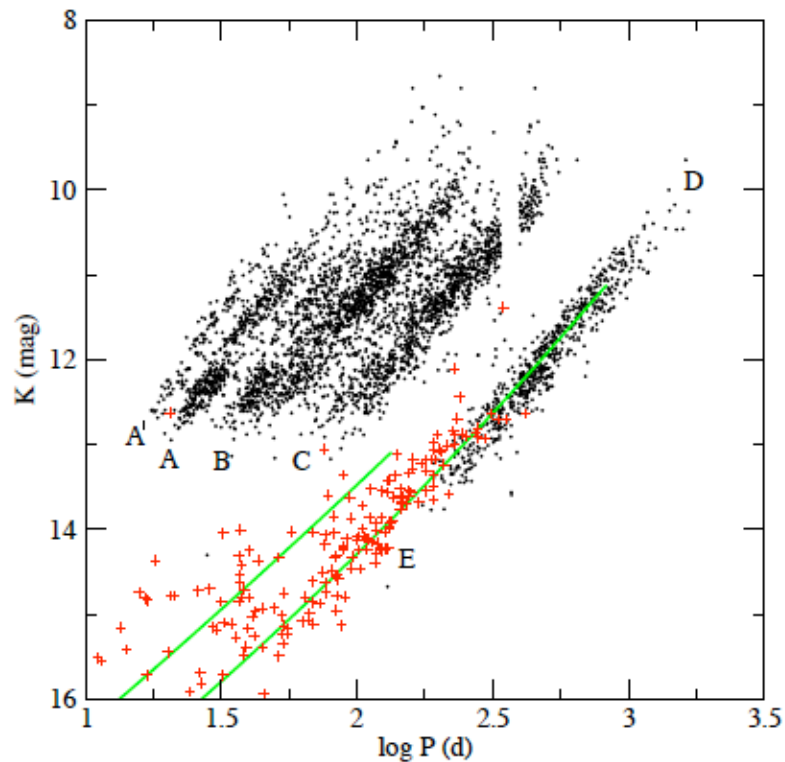
- C Mira fundamental mode
- A, B higher overtones
- E eclipsing & ellipsoidal (+)
- D ??
(also called 'LSP': 'long secondary periods')

25% of LMC LPV are on sequence D (!),

Can they all be binaries ?

For comparison, among M giants, the frequency of spectroscopic binaries with periods in the range 200 - 10000 d is between 16 and 21%

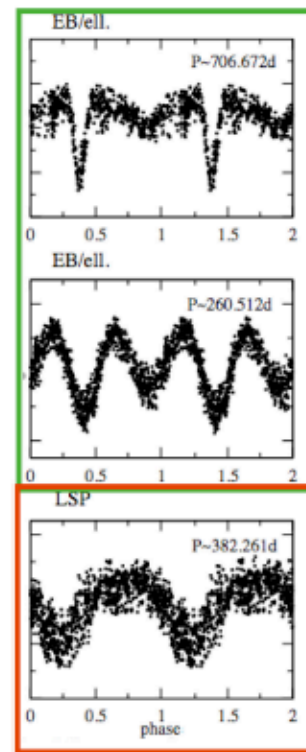
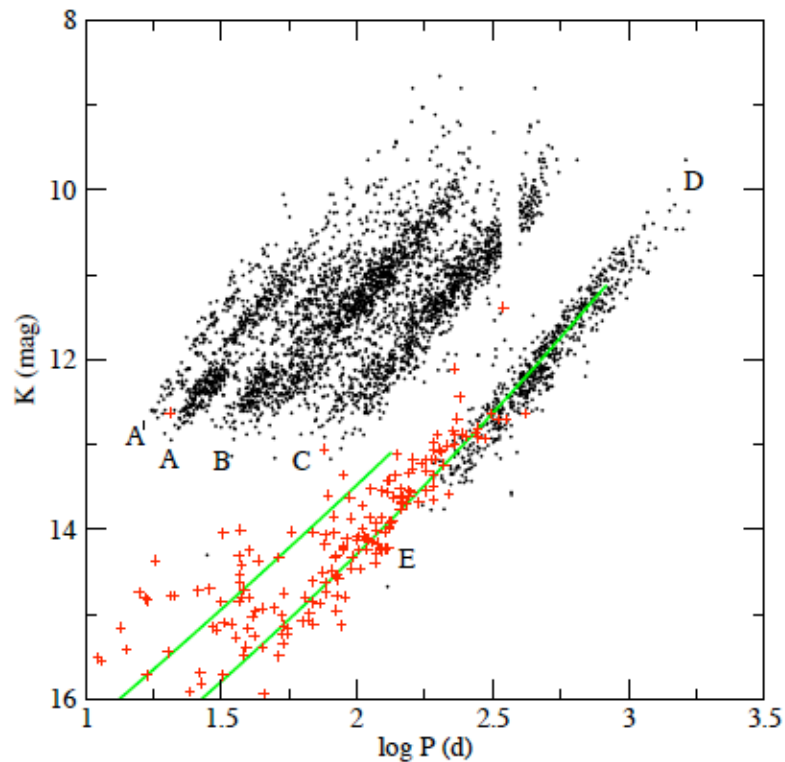
Photometry: MACHO (VII)



Green lines = P for RLOF Derekas et al., 2006, ApJ 650, L55

→ 25% of LMC LPVs fill their Roche lobe if all sequence D stars are binaries !?

Photometry: MACHO (VII)



Only 5%
among D sequence
show clear eclipsing
or ellipsoidal behaviour

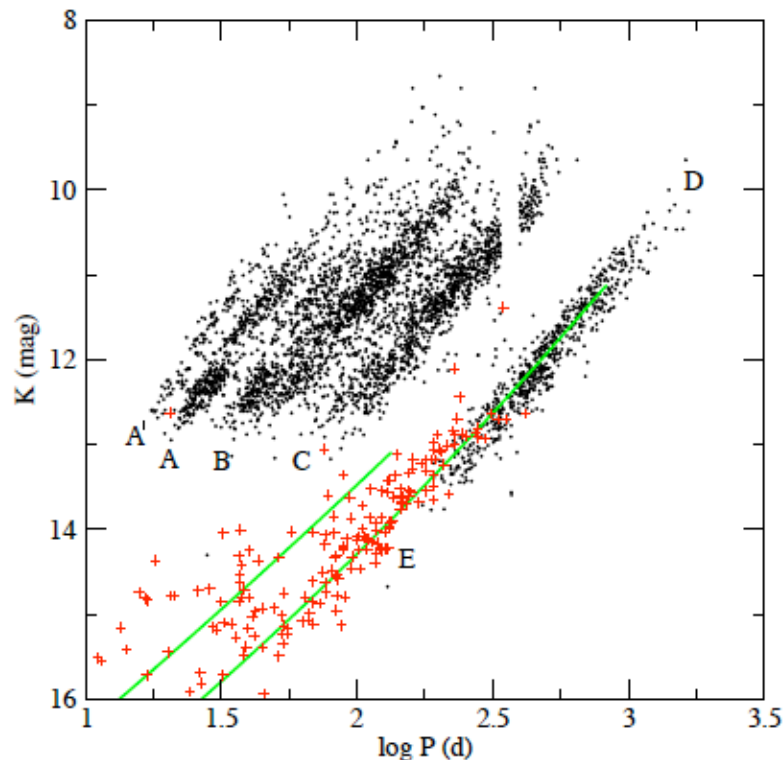
What is the nature of the
other D stars ?

Green lines = P for RLOF Derekas et al., 2006, ApJ 650, L55

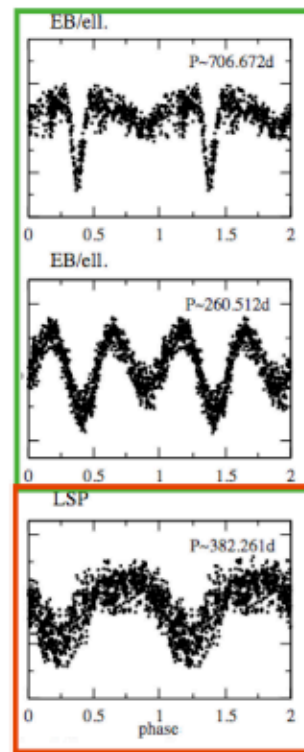
Photometry: MACHO (VII)

Binaries among LPVs: none from spectroscopy, too many from MACHO!

25% of LMC LPVs fill their Roche lobe if all sequence D stars are binaries !?



Green lines = P for RLOF Derekas et al., 2006, ApJ 650, L55



Only 5% among D sequence show clear eclipsing or ellipsoidal behaviour

What is the nature of the other D stars?

D sequence caused by dust obscuration in Roche-lobe-filling AGB stars?

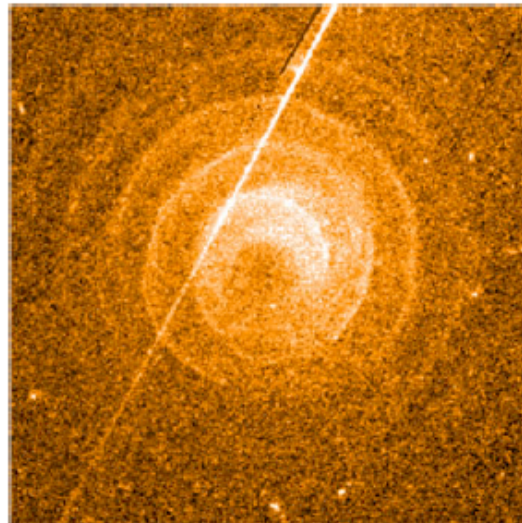
(Soszynski 2007, ApJ, 660, 1486)

Dust in spiral wave forming around binary LPVs,

as predicted by SPH simulations

Direct imaging of circumstellar shell:

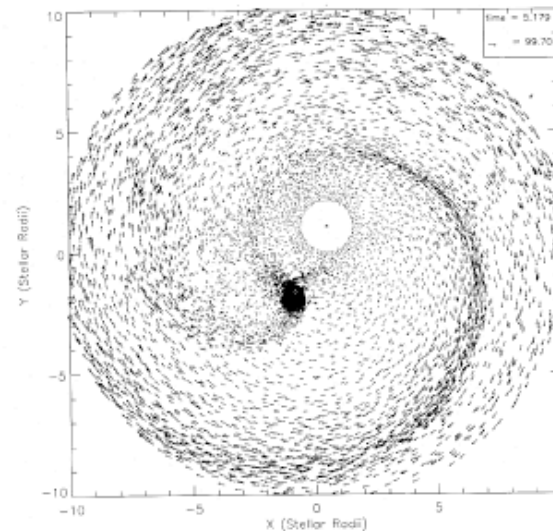
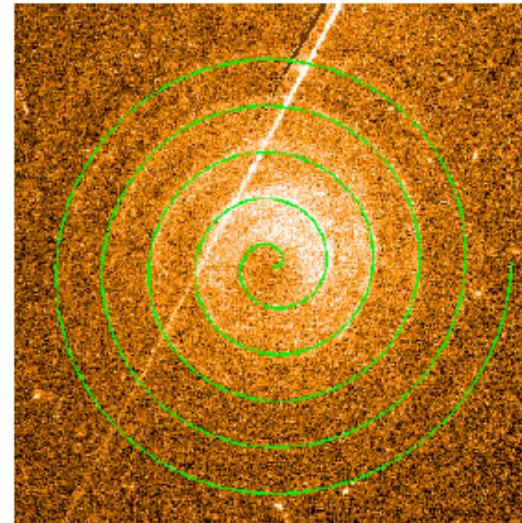
The proto PN AFGL 3068



Mauron & Huggins, 2006, A&A 452, 257

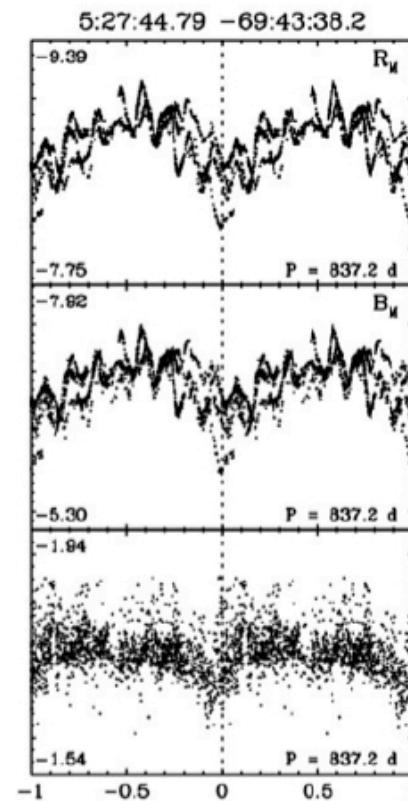
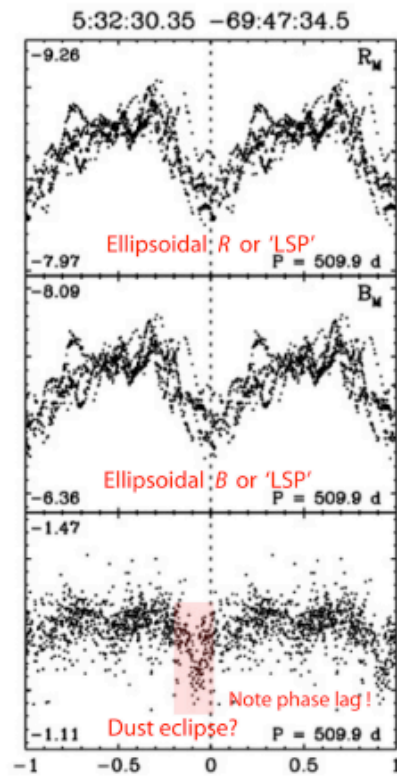
Periodic dust obscuration
from this spiral wave is
probably what causes
variability along D sequence

Theuns & Jorissen 1993, MNRAS 265, 946
Mastrodemos & Morris 1998, ApJ 497, 303
Nagae et al. 2004, A&A 419, 335



More on photometry

Eclipses by dust: stars on sequence D



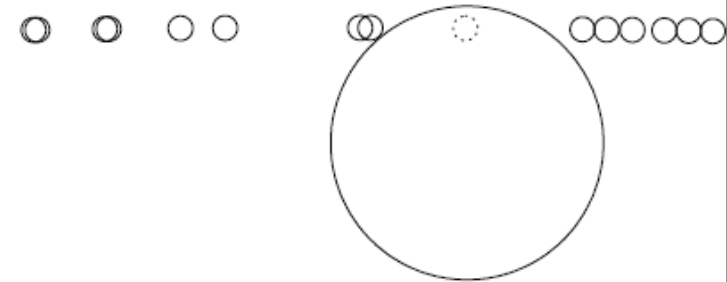
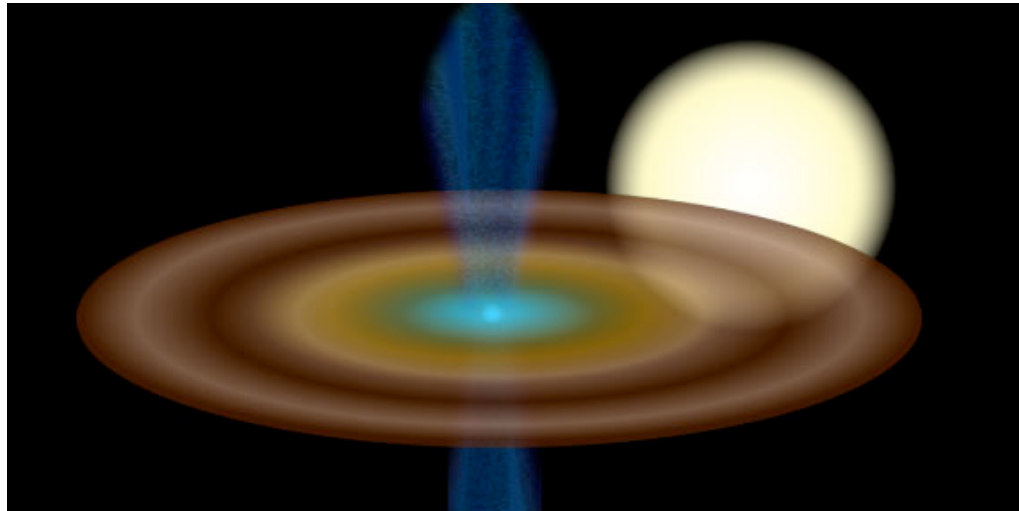
R band

B band

R-B : low-amplitude eclipses show up

Note the phase lag

Photometric binaries: Eclipsing



Other classes of eclipsing binaries :

- **ϵ Aur** : eclipses by an inclined disk, with a 27-yr period

- **ζ Aur** and **VV Cep** : eclipses of a hot main-sequence star by the atmosphere of a giant or supergiant : eclipses probe the wind from the hot star

Carpenter, 1992, IAU Symp 151, 51

The various kinds of binaries

Type	Notation	Two stars visible?	orbit	dimension
visual and interferometric	VB	yes	relative	angular
astrometric	AB	yes no	relative photocentric	angular
spectroscopic	SB2 SB1	yes no	absolute absolute	linear
photometric (eclipsing, ellipsoidal)	EB	'yes' (composite)	relative	relative (radius *)

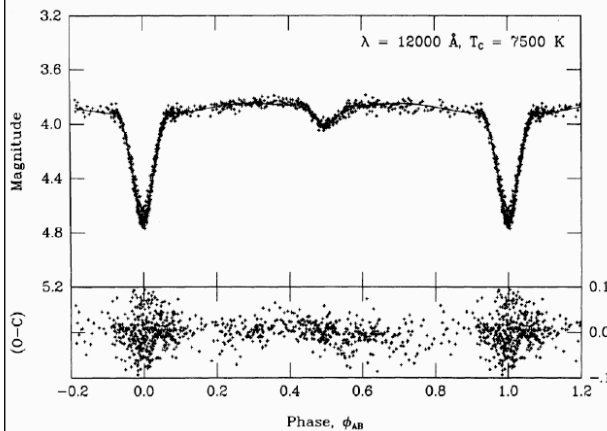
A given system may belong to more than one category!

Photometric binaries: Eclipsing, ellipsoidal

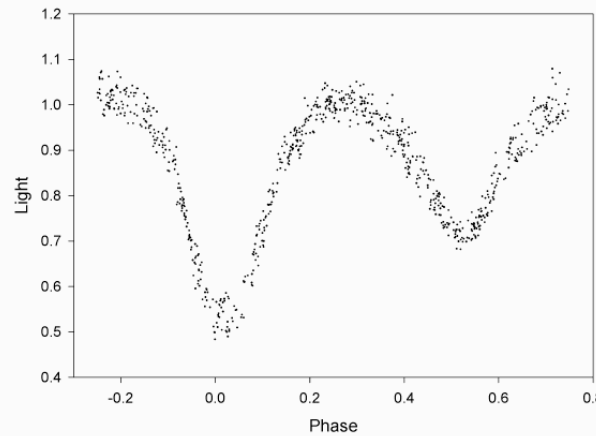
a. Detached system

**b. Semi-detached system
aka ellipsoidal**

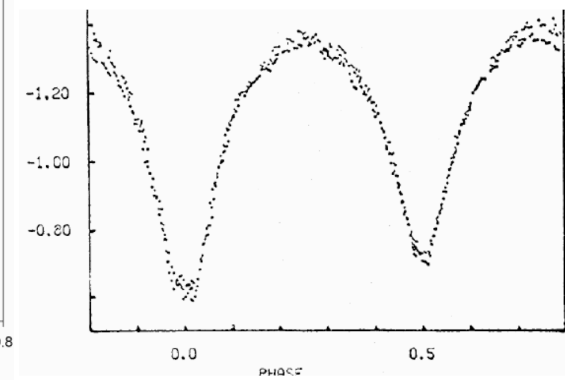
c. Contact system



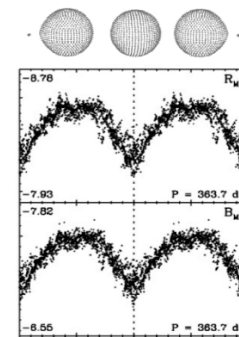
β Per / β Lyr / W Ser / SV Cen



W UMa



For semi-detached
and contact systems,
the photometric
variations must be
(close to) **achromatic**



R band

B band

Photometric binaries

These are the binaries we just discussed :

- *Algols*
 - Semidetached systems with main sequence primary and evolved secondary
 - Slow phase of mass transfer
 - Rapid rotators are a sub-class that may connect W Ser systems with normal Algols
- *W UMa Systems*
 - Overcontact systems with components of different mass but very similar temperatures
 - Details of structure not well-understood
 - Asymmetries in light curves that change on short timescales
- *W Ser Systems*
 - Semidetached systems in or just past the rapid phase of mass transfer
 - Strong emission lines in the UV
 - Precursors of Algols?

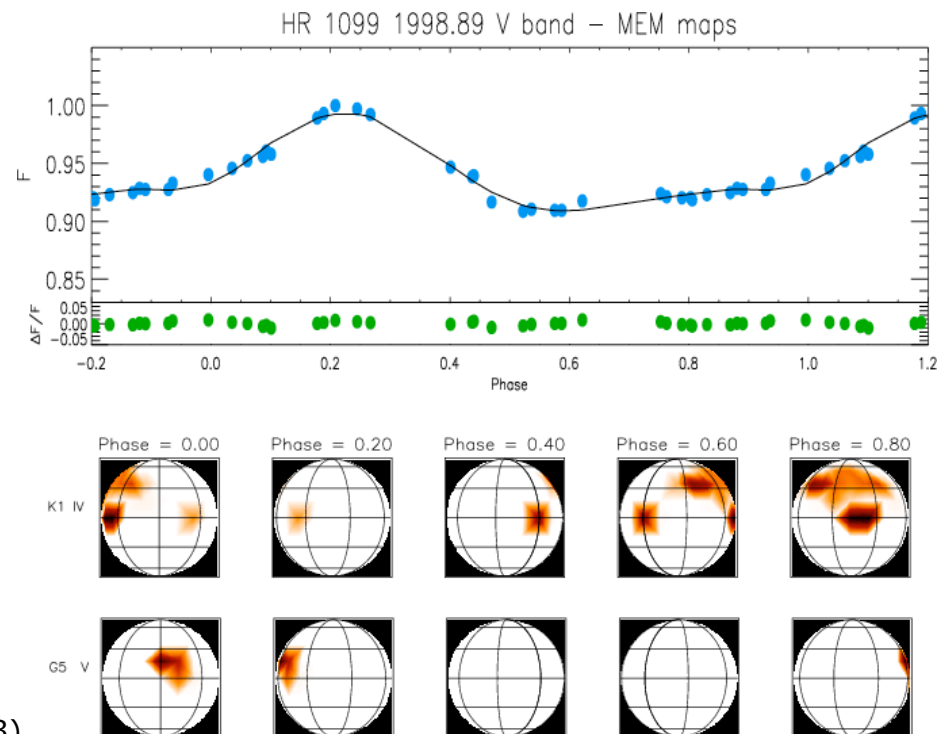
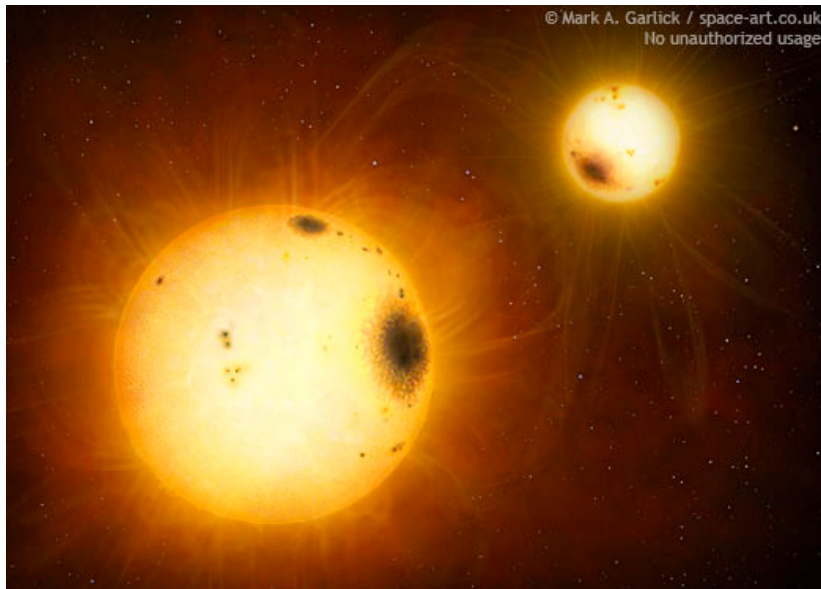
Other classes of eclipsing binaries :

- **ϵ Aur** : eclipses by an inclined disk
- **ζ Aur** and **VV Cep** : eclipses of a hot main-sequence star by the atmosphere of a giant or supergiant

Photometric binaries: Spotted

- ***RS CVn Systems***

- **Detached systems with F or G-type primary and K subgiant secondary**
- **Enormous cool spots that migrate on a yearly timescale**
- **The binary system is close enough ($P < 100$ d) for the stars to be spun up by tidal locking, which then causes a dynamo effect, magnetic field, and spots**

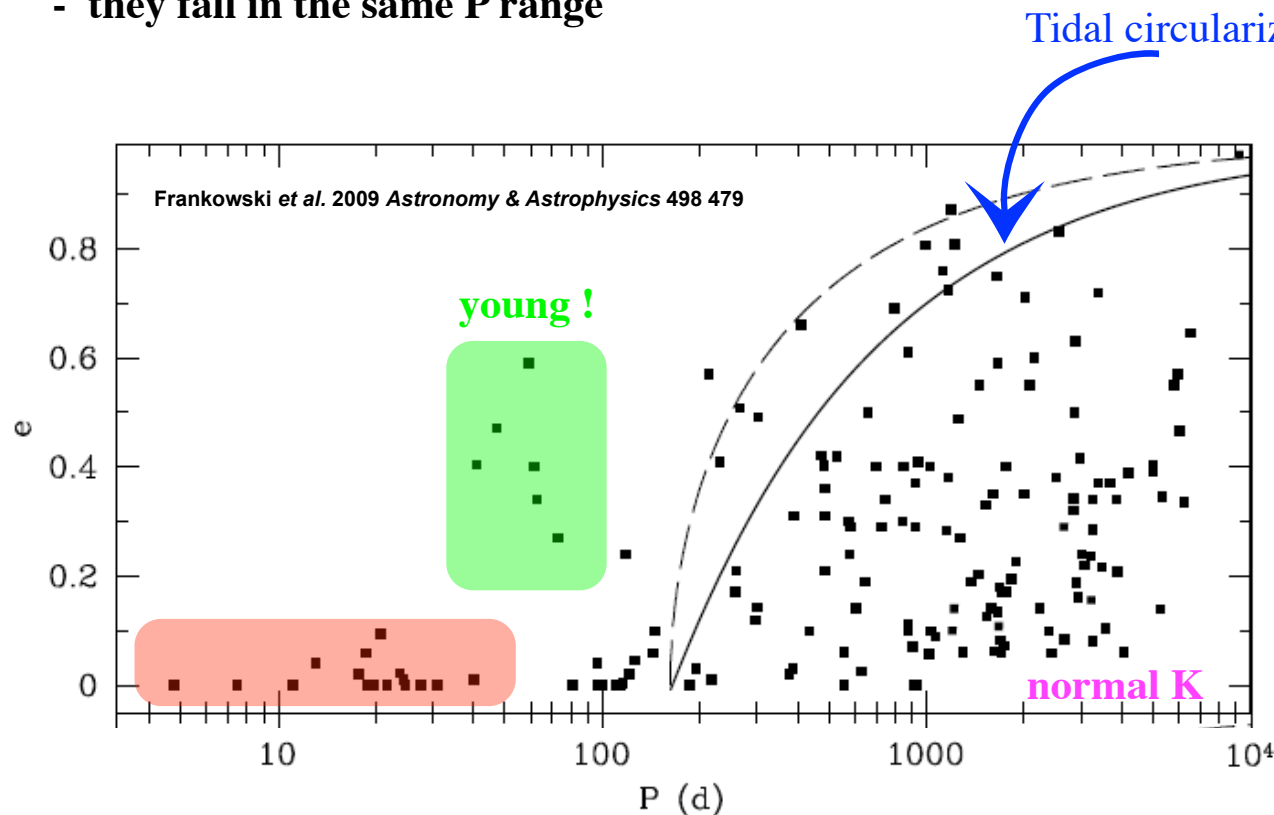


Garcia-Alvarez et al., A&A 397, 285-303 (2003)

Eccentricity - period diagrams

RS CVn often confused with **pre-MS binaries**,
because

- both have spectral type K
- they fall in the same P range

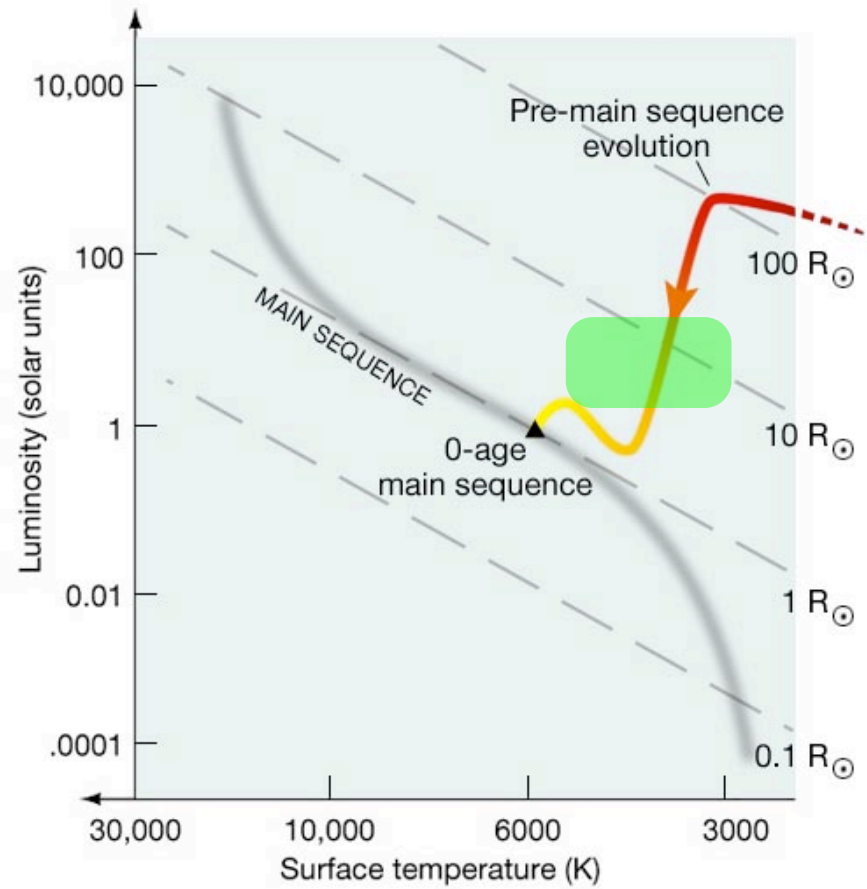
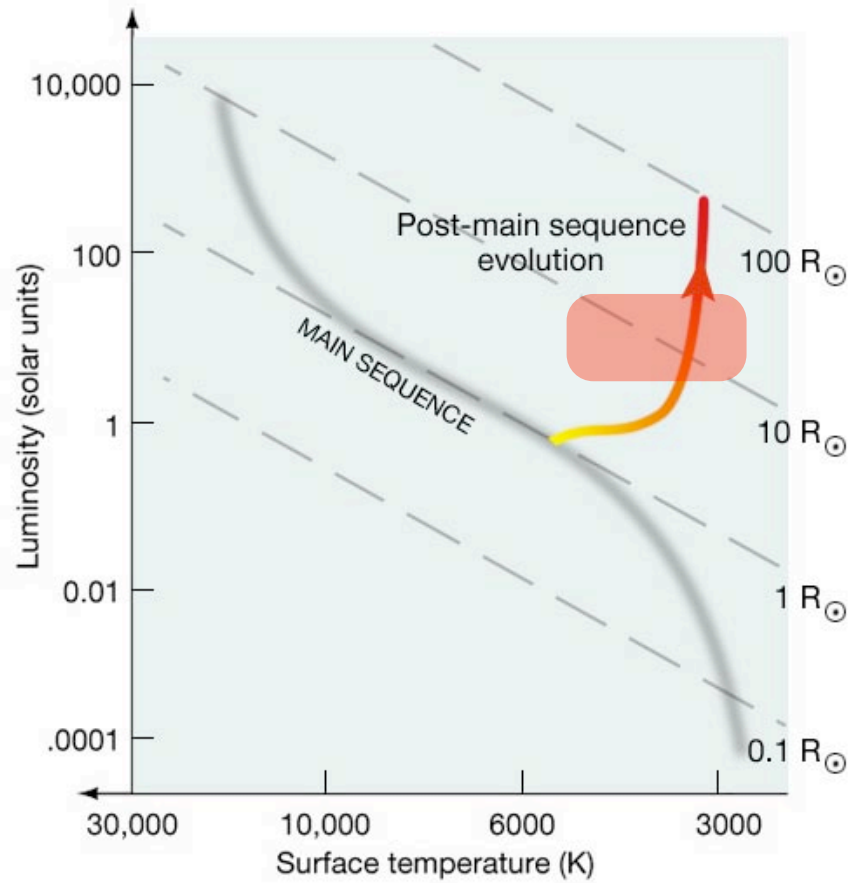


e - P diagram for systems with KIII primaries from SB9

[The 9th Catalogue of Spectroscopic Binary Orbits]

<http://sb9.astro.ulb.ac.be>

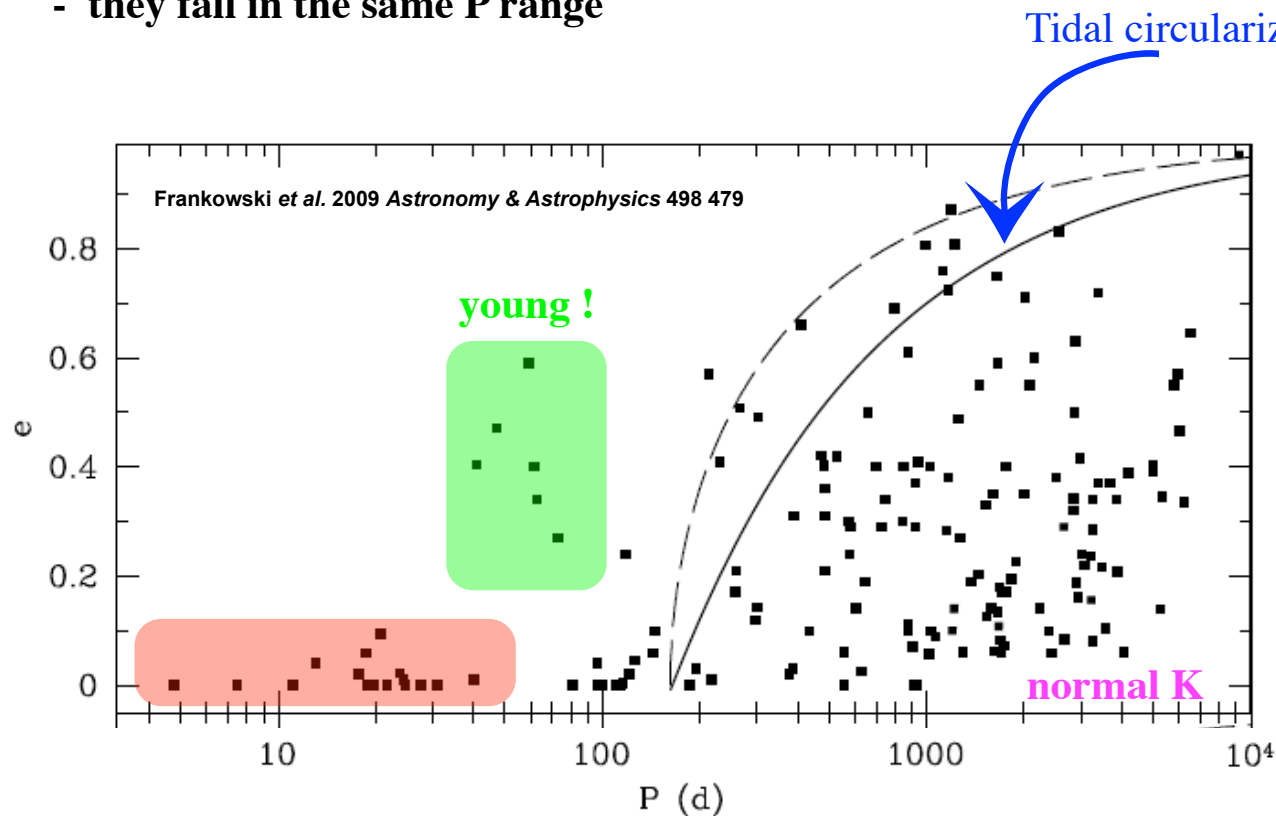
RS CVn versus pre-main-sequence



Eccentricity - period diagrams

RS CVn often confused with **pre-MS binaries**,
because

- both have spectral type K
- they fall in the same P range



e - P diagram for
systems with **KIII**
primaries from
SB9

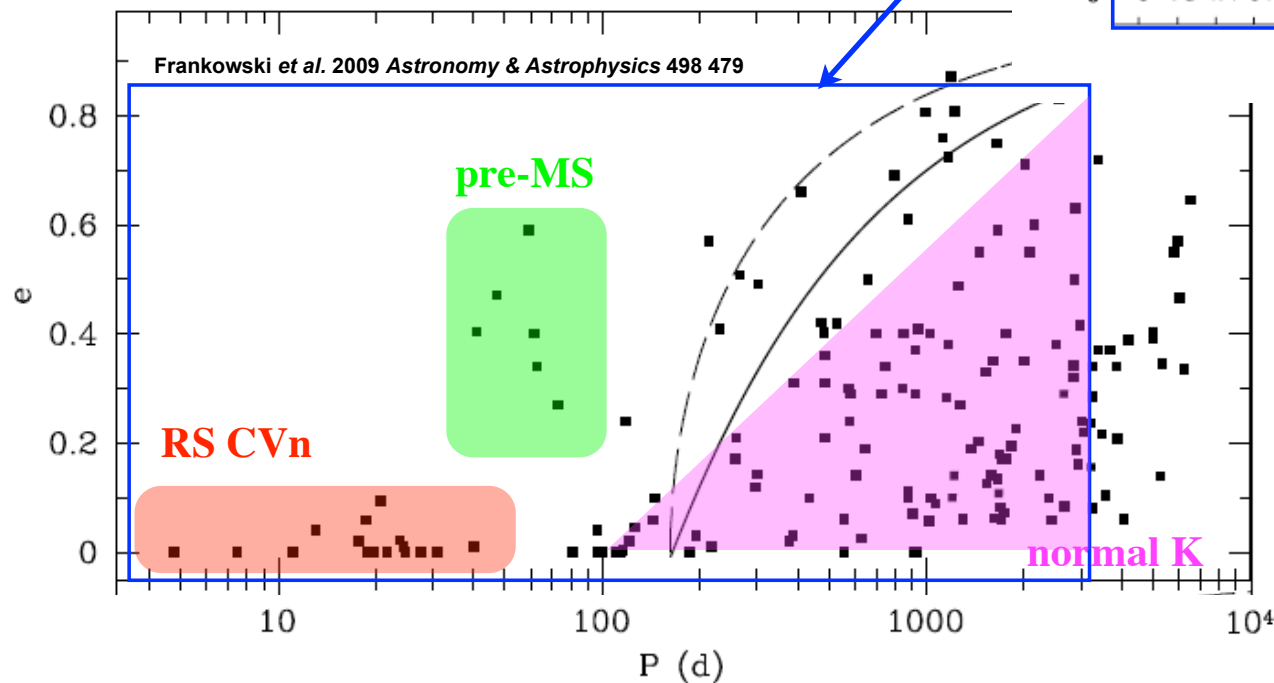
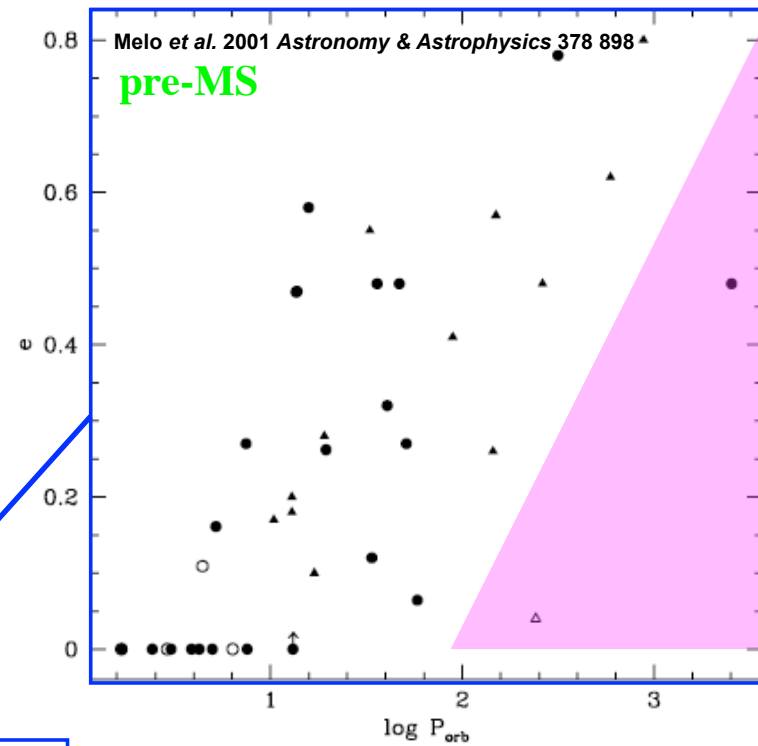
[The 9th Catalogue
of Spectroscopic
Binary Orbits]

[http://
sb9.astro.ulb.ac.be](http://sb9.astro.ulb.ac.be)

Eccentricity - period diagrams

RS CVn often confused with **pre-MS binaries**,
because

- both have spectral type K
- they fall in the same P range

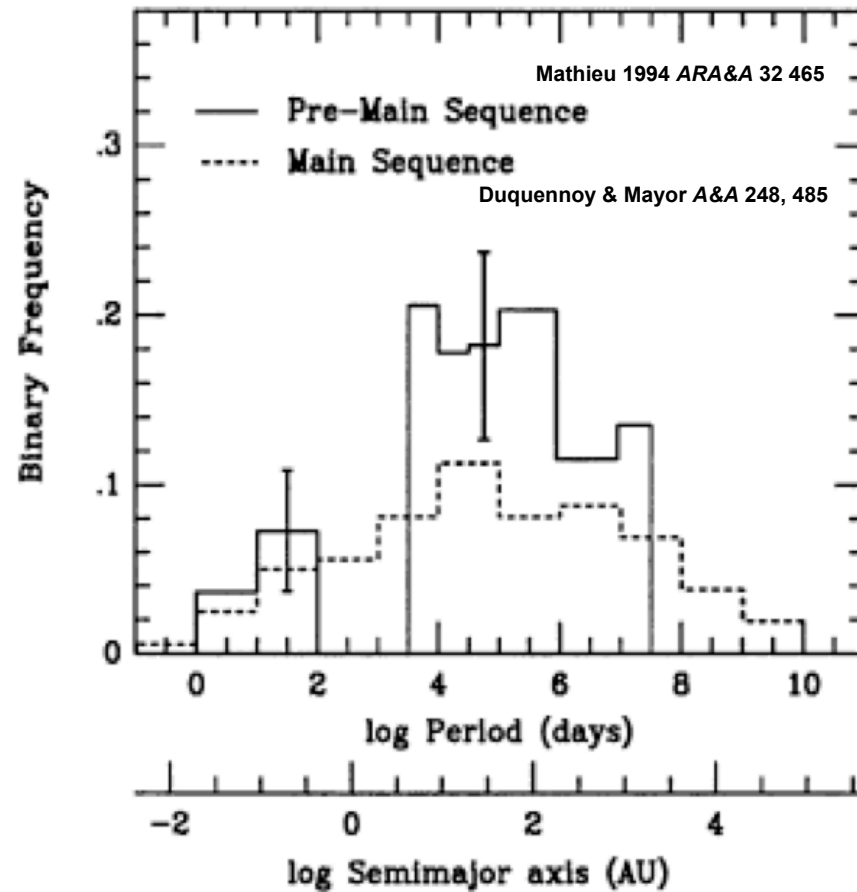


e - P diagram for systems with KIII primaries from SB9

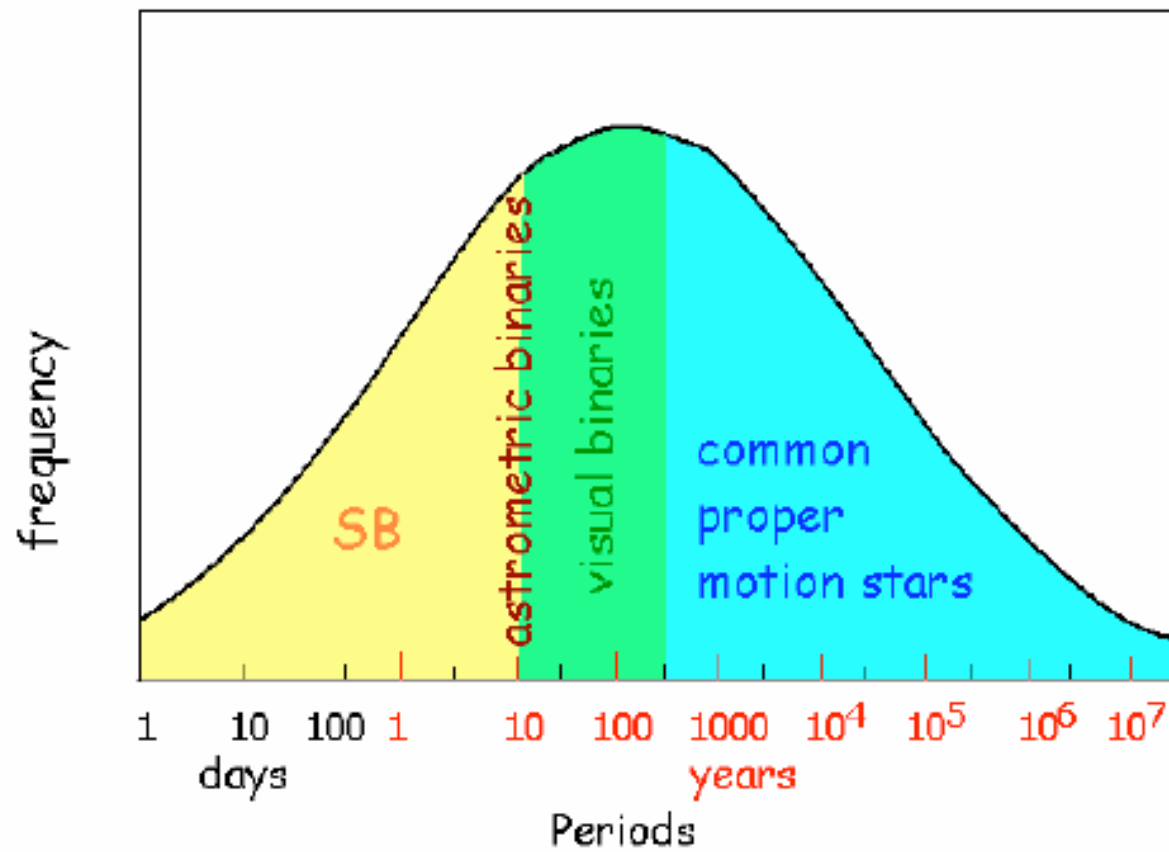
[The 9th Catalogue of Spectroscopic Binary Orbits]

<http://sb9.astro.ulb.ac.be>

pre-main-sequence versus main-sequence period distribution



period distribution for all kinds of binaries



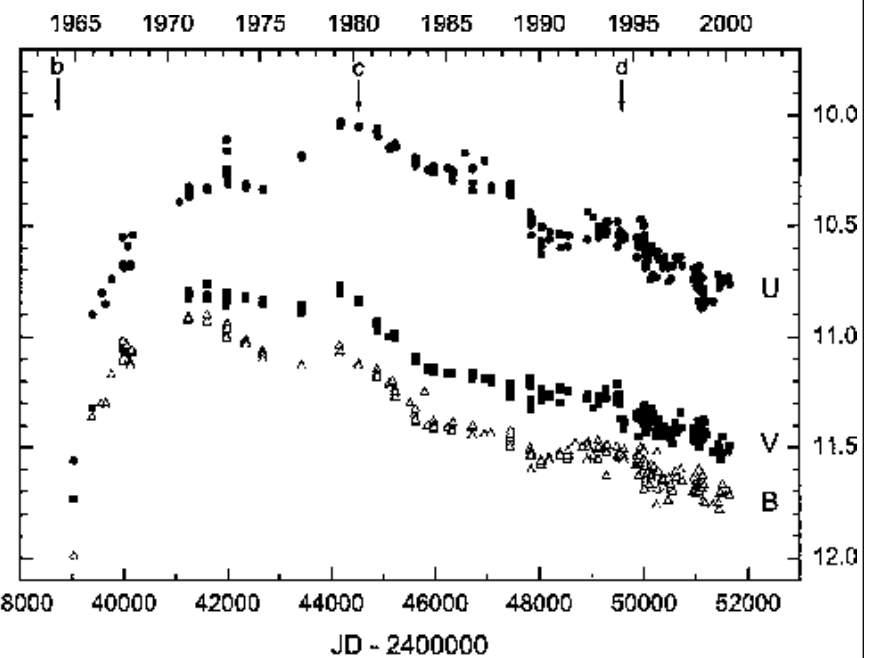
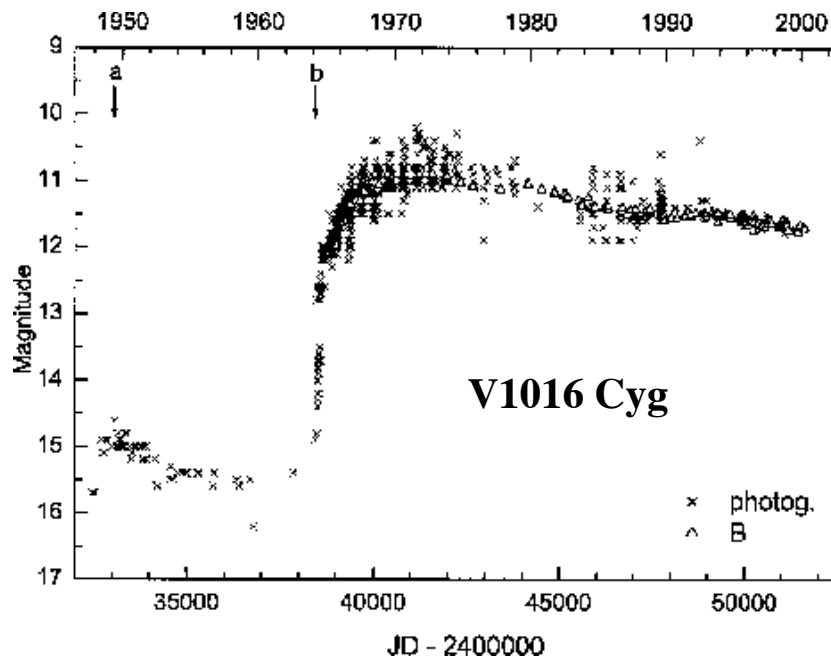
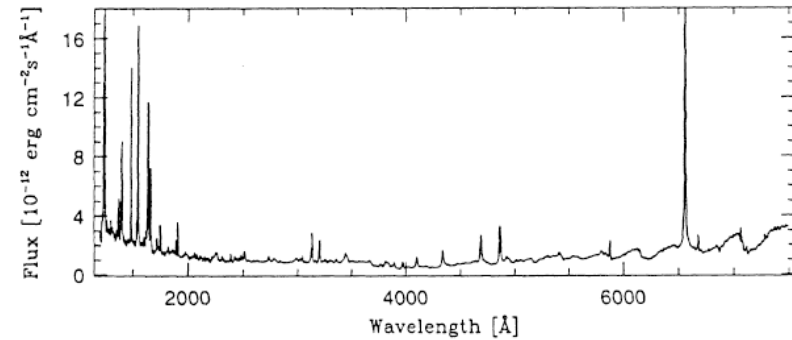
Photometric binaries: eruptive

- novae :** dwarf + WD (low accretion rate)
a few: giant + WD ('symbiotic nova')
thermonuclear outbursts (non-destructive explosive H-burning on the WD)
- cataclysmic variables:** dwarf + WD (high accretion rate with accretion disk):
- dwarf novae
- AM Her (highly magnetic, no accretion disc)
- DQ Her (moderately magnetic, accretion disc)
accretion or disc instabilities
- Symbiotic :** giant + WD (neutron star in one case)
sometimes accretion disc (Z And, X-ray flickering)
most often no X-ray flickering (-> X-ray origin ?)
accretion or disc instabilities
- supernovae type Ia :** WD + WD
thermonuclear outbursts (destructive explosive C-burning in merging WDs ?)

Photometric binaries: eruptive

Symbiotic :

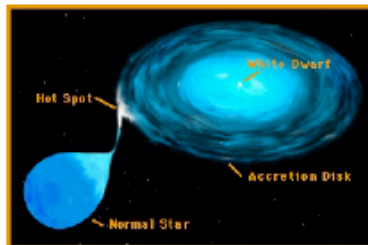
eruptions + composite spectrum
(hot + cool + nebula)



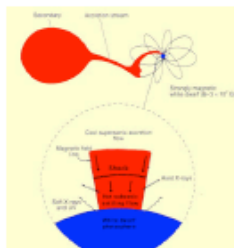
X-rays

Basics on X-ray binaries (III)

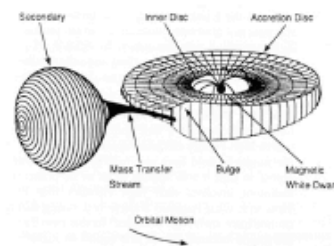
CVs = dwarf star + white dwarf in a short P, semi-detached system



Dwarf novae



Polars (AM Her systems):
Highly magnetized white dwarfs



Intermediate Polars
(DQ Her systems)
longer P and wider separation: there is
room for an accretion disk

X-rays

Basics on X-ray binaries (IV)

X-rays (photons with $h\nu > 0.1$ keV requiring $T > 10^6$ K) may come from:

- **hot stellar coronae** (either single star or RS CVn binary)

RS CVn: dynamo caused by fast, synchronous rotation

- **nuclear fusion** (nova or symbiotic star)

- Classical novae: explosive H-burning ($10^{33} - 10^{34}$ ergs/s)
- Super soft sources : quiescent H-burning ?

- **accretion**

- CVs = dwarf star + white dwarf in a short P, semi-detached system
 - Dwarf novae
 - Polars (AM Her systems)
 - Intermediate Polars (DQ Her systems)
- Algols = subgiant (less massive) + main sequence (more massive) in a semidetached system
- Symbiotics = giant star + white dwarf in a long P system but accretion-driven X-rays challenged !

- **wind collision**

- Symbiotics

X-rays from binaries :

The case of symbiotic stars

Origin of X-rays not clear:

accretion disk, nuclear fusion, wind collision or fast rotation ?

Accretion-driven X-rays are accompanied by flickering with periods of minutes to days, as observed in Z And

Sokoloski 2003, ASP Conf. Ser. 303, p. 202

but flickering not often observed in symbiotic X rays!

→ fast rotation as for RS CVn, with X-rays due to dynamo activity?

Soker 2002, MNRAS 337, 1038

Intriguing possibility, because it requires a high incidence of fast rotation !

The WIRRING stars, or 'Wind-Induced Rapidly RotatING',

Jeffries & Stevens, 1996, MNRAS 279, 180

are post-mass-transfer systems rotating fast, due to the accretion of spin angular momentum during the mass transfer !

Photometric binaries: X-rays

Low-mass X-ray binaries (related to dwarf novae and CVs)

High-mass X-ray binaries : neutron star or black hole companions

The bestiary

DQ Her, AM Her

RS CVn, pre-main sequence

Algols, β Lyr, SV Cen, W Ser

Z And (symbiotic)

VV Cep, zeta Aur, eps Aur, MACHO sequence D

CH (giants and subgiants), S (no-Tc), Ba, dwarf Ba, WIRRING, Abell 35

post-AGB

SN Ia

novae, dwarf novae

LMXRB, HMXRB

The concepts

cases A, B, C

RLOF, Bondi-Hoyle, common envelope

dynamical, thermal, nuclear time scales

astrometric, interferometric, spectroscopic (SB I, SB2)

eclipsing, ellipsoidal binaries

e - P, mass function, deriving masses

What should you have learned ?

